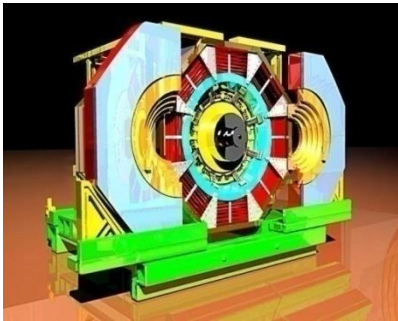


Rare Charm Decays

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**20th conference on Flavor Physics and CP violation
(FPCP 2022)**

May 23-27, 2022

Overview

➤ Introduction

Rare charm decays

➤ Physics highlights

Flavor Changing Neutral Current

Lepton Flavor Violation

Lepton Number Violation

Baryon Number Violation

➤ Summary

Rare Charm Decays

- Processes:

Standard Model is dominant (SM)

Standard Model contribution is highly suppressed (SM + New Physics)

Standard Model contribution is forbidden (New Physics)

- Branching ratios of about 10^{-9} or smaller

FCNC: Flavour Changing Neutral Current

BNV: Baryon Number Violation

LVN: Lepton Number Violation

LFV: Lepton Flavour Violation

$$D^0 \rightarrow \mu^+ e^-$$

$$D^0 \rightarrow pe^-$$

$$D_{(s)}^+ \rightarrow h^+ \mu^+ e^-$$

$$D_{(s)}^+ \rightarrow \pi^+ l^+ l^-$$

$$D_{(s)}^+ \rightarrow K^+ l^+ l^-$$

$$D^0 \rightarrow K^- \pi^+ l^+ l^-$$

$$D^0 \rightarrow K^0 l^+ l^-$$

$$D^0 \rightarrow \pi^- \pi^+ V (\rightarrow ll)$$

$$D^0 \rightarrow K^{*0} \gamma$$

$$D^0 \rightarrow \rho^- V (\rightarrow ll)$$

$$D^0 \rightarrow (\phi, \rho, \omega) \gamma$$

$$D^0 \rightarrow K^+ K^- V (\rightarrow ll)$$

$$D_s^+ \rightarrow \pi^+ \phi (\rightarrow ll)$$

$$D^0 \rightarrow \phi^- V (\rightarrow ll)$$

LFV, LVN, BNV	FCNC								VMD		Radiative	
0	10^{-15}	10^{-14}	10^{-13}	10^{-12}	10^{-11}	10^{-10}	10^{-9}	10^{-8}	10^{-7}	10^{-6}	10^{-5}	10^{-4}
$D_{(s)}^+ \rightarrow h^- l^+ l^+$												
$D^0 \rightarrow X^0 \mu^+ e^-$				$D^0 \rightarrow ee$	$D^0 \rightarrow \mu\mu$	$D^0 \rightarrow \pi^- \pi^+ l^+ l^-$	$D^0 \rightarrow \rho^- l^+ l^-$	$D^0 \rightarrow K^+ \pi^- V (\rightarrow ll)$	$D^+ \rightarrow \pi^+ \phi (\rightarrow ll)$			
$D^0 \rightarrow X^{--} l^+ l^+$						$D^0 \rightarrow K^+ K^- l^+ l^-$	$D^0 \rightarrow \phi l^+ l^-$	$D^0 \rightarrow \bar{K}^{*0} V (\rightarrow ll)$	$D^0 \rightarrow K^- \pi^+ V (\rightarrow ll)$			
								$D^0 \rightarrow \gamma\gamma$	$D^0 \rightarrow K^{*0} V (\rightarrow ll)$			

Rare Charm Decays

- Charm hadron: contains up-type heavy quark

complementary information to B and K sector in NP search

- Strong GIM mechanism in charm decays
- Constrain effects from New Physics
- Processes are forbidden at tree level in the SM, but allowed in loop and box diagrams
- Short distance contributions at one-loop level

GIM cancellation is almost exact

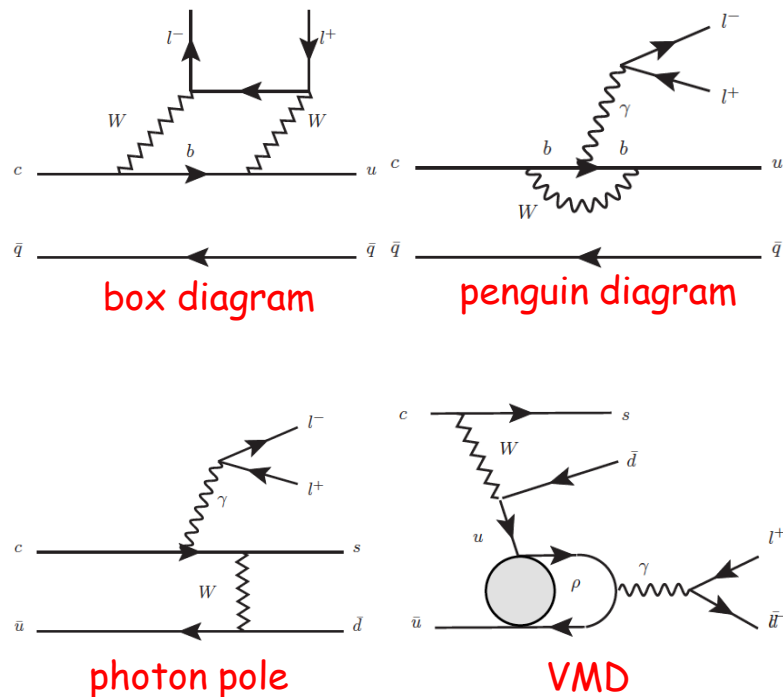
$$BF = O(10^{-9})$$

- Long distance contributions

Vector Meson Dominance (VMD)

$$BF = O(10^{-6})$$

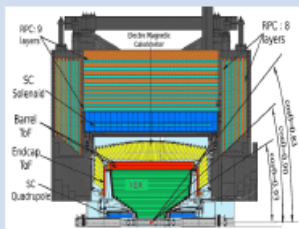
- Away from long-distance contributions, potential for New Physics to be visible
- Test of Lepton Universality, by comparing decays to electrons vs muons



Experimental Scenarios

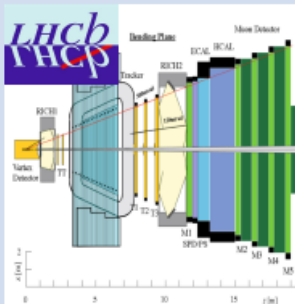
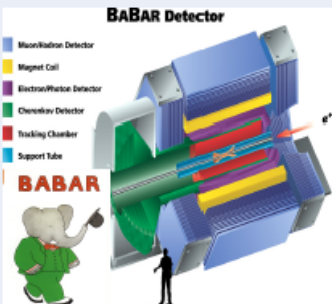
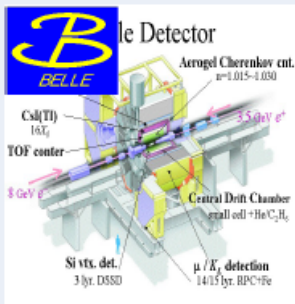
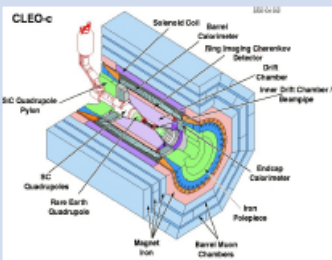
Experiments

BESIII

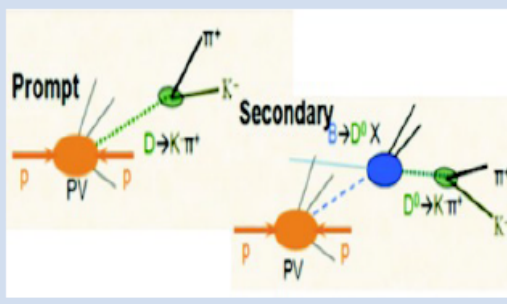
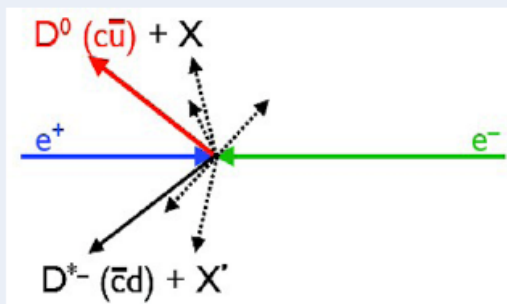
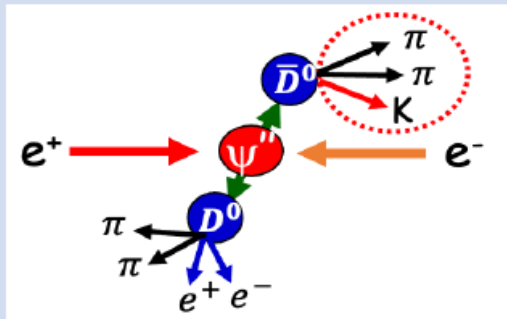


Wire tracker (no Si); TOF + dE/dx for PID; **Si** for μ ; RPC muon

CLEO-c



Decay Chain



Benefit

- Extremely clean environment
- DT method, almost bkg free
- Quantum coherence
- High trigger efficiency
- Easy detection of neutrals and electrons

- Clean environment
- High trigger efficiency
- Easy detection of neutrals
- Boost: time-dependent analysis

- Large production rate
- Large boost: excellent time resolution

Latest Rare Charm Decays Investigations

- Flavor Changing Neutral Current

2019: $D^0 \rightarrow K^-\pi^+e^+e^-$ (BABAR, PRL 122, 081802)

2021: $J/\psi \rightarrow D^-e^+\nu_e$ (BESIII, JHEP06 157)

2021: $D^+_{(S)} \rightarrow h^+l^+l^-$ (LHCb, JHEP06 044)

2021: $D^0 \rightarrow h^+h^-\mu^+\mu^-$ (LHCb, arXiv:2111.03327, submitted to PRL)

2022: $D^0 \rightarrow \pi^0\nu\bar{\nu}$ (BESIII, PRD 105, 071102)

- Lepton Flavor Violation

2020: $D^0 \rightarrow hh'l^+l^-$ (BABAR, PRL 124, 071802)

2020: $D^0 \rightarrow X^0e^\pm\mu^\mp$ (BABAR, PRD 101, 112003)

2021: $D^+_{(S)} \rightarrow he^\pm\mu^\mp$ (LHCb, JHEP06 044)

- Lepton Number Violation

2019: $D \rightarrow K\pi e^+e^+$ (BESIII, PRD 99, 112002)

2020: $D^0 \rightarrow hh'l^+l^+$ (BABAR, PRL 124, 071802)

2021: $D^+_{(S)} \rightarrow hl^+l^+$ (LHCb, JHEP06 044)

- Baryon/Lepton Number Violation

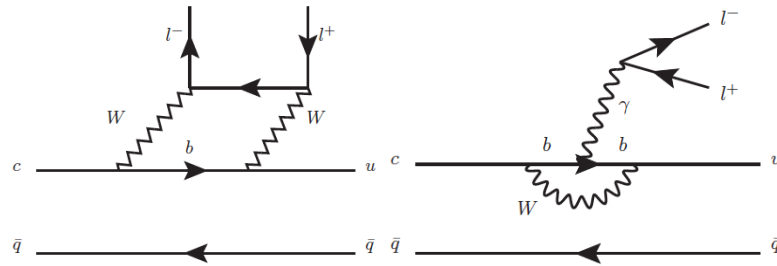
2020: $D^+ \rightarrow \bar{\Lambda}(\bar{\Sigma}^0)e^+$, $D^+ \rightarrow \Lambda(\Sigma^0)e^+$ (BESIII, PRD 101, 031102)

2022: $D^0 \rightarrow pe^- + c.c.$ (BESIII, PRD 105, 032006)

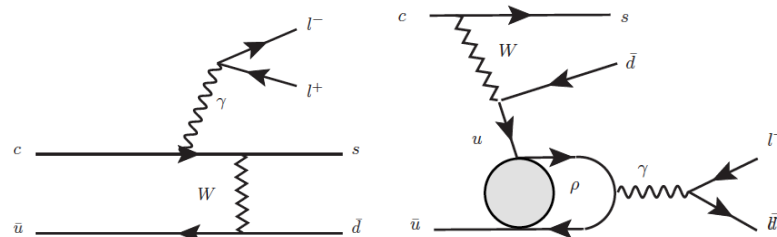
FCNC Processes

- In SM, FCNC is strongly suppressed by *GIM* mechanism and can happen only through loop diagram, leading to a very small BF, 10^{-9} , theoretically
- The suppression in charm decays is much stronger than those in B and K system due to stronger diagram cancellation than the down-type quarks
- However, it can reach 10^{-6} under LD contribution
- Sensitive to New Physics

SD contributions



LD contributions

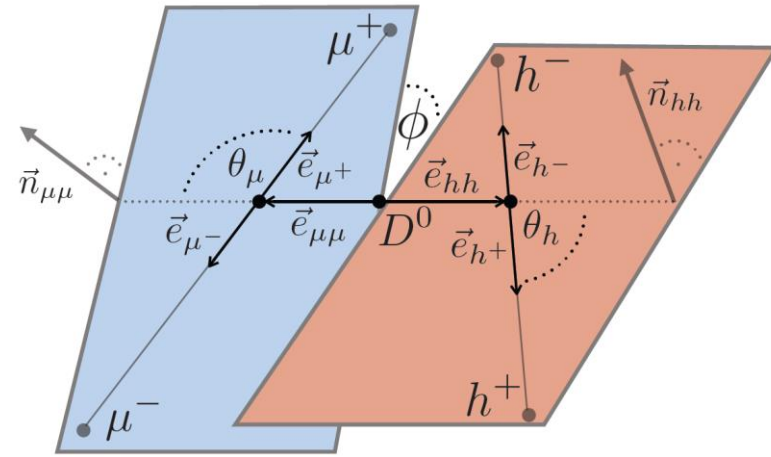


FCNC Processes

- 9 fb⁻¹ at 7, 8, and 13 TeV
- D^{*+} → D⁰π⁺, D⁰ → h⁺h⁻μ⁺μ⁻, h = π, K
- Decays described by:
q²=m²(μ⁺μ⁻), p²=m²(h⁺h⁻), θ_μ, θ_h, φ
- Differential decay rate depends on
9 angular coefficients I₁₋₉



LHCb
arXiv:2111.03327
Submitted to PRL

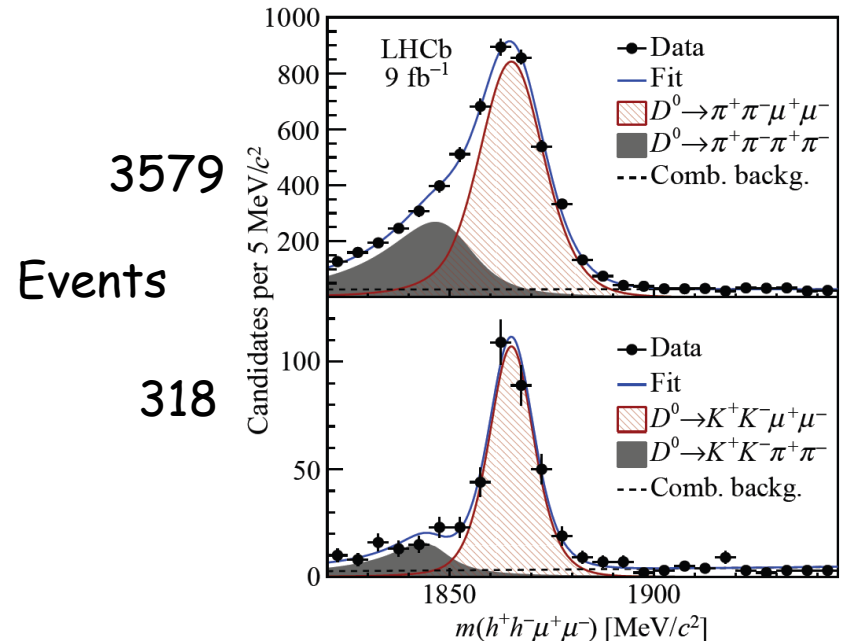


$$\langle I_2 \rangle = \frac{\Gamma(|\cos \theta_\mu| > 0.5) - \Gamma(|\cos \theta_\mu| < 0.5)}{\Gamma(|\cos \theta_\mu| > 0.5) + \Gamma(|\cos \theta_\mu| < 0.5)}$$

CP average $\langle S_i \rangle = \frac{1}{2} [\langle I_i \rangle + (-)\langle \bar{I}_i \rangle]$

Asymmetry $\langle A_i \rangle = \frac{1}{2} [\langle I_i \rangle - (+)\langle \bar{I}_i \rangle]$

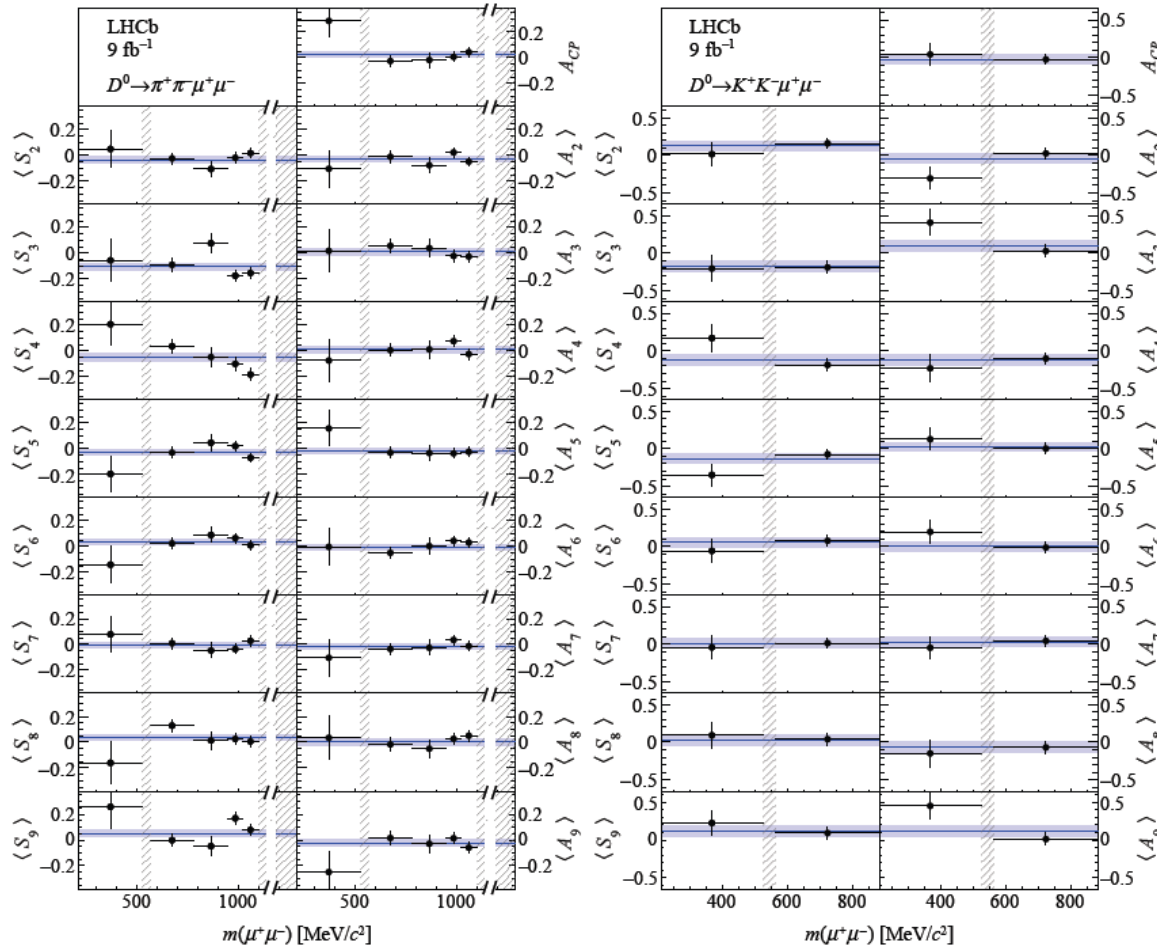
- Signal: Hypatia distribution
- Background: Johnson S_U distribution + exponential



FCNC Processes

LHCb
arXiv:2111.03327
Submitted to PRL

$D^0 \rightarrow h^+ h^- \mu^+ \mu^-$



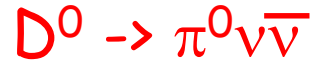
$$\langle S_i \rangle = \frac{1}{2} [\langle I_i \rangle + (-) \langle \bar{I}_i \rangle]$$

$$\langle A_i \rangle = \frac{1}{2} [\langle I_i \rangle - (+) \langle \bar{I}_i \rangle]$$

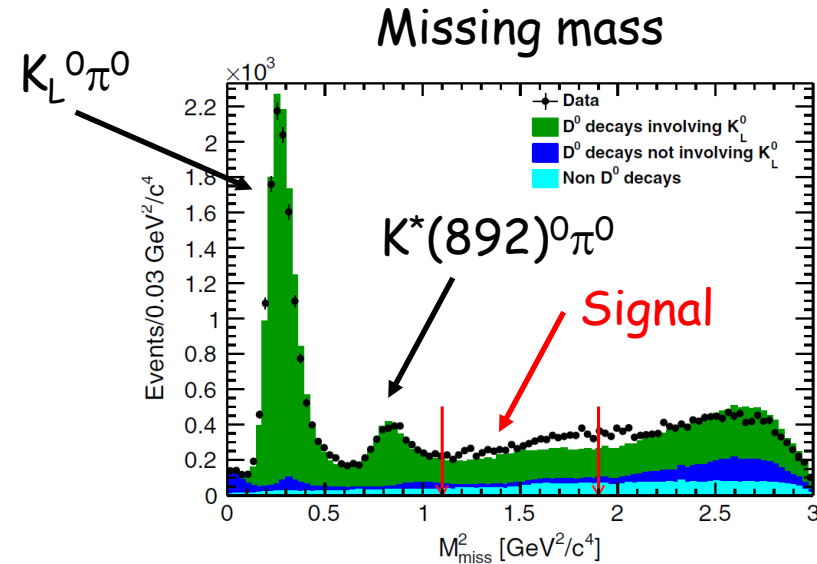
- Null-test observables: $\langle S_{5-7} \rangle$ and $\langle A_{2-9} \rangle$ in agreement with the SM null-hypothesis
- Constrain parameters of physics models
- First full angular analysis

FCNC Processes

BESIII
PRD 105 (2022) L071102



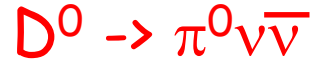
- 2.93 fb⁻¹ @ 3,773 GeV
- Decay chain $e^+e^- \rightarrow D^0 \bar{D}^0$, $D^0 \rightarrow \pi^0 \nu \bar{\nu}$
 $\bar{D}^0 \rightarrow K^+ \pi^-, K^+ \pi^- \pi^0, K^+ \pi^- \pi^- \pi^+$
- First experimental search
- No long distance contributions
- Double-Tag method



- Energy difference: $\Delta E = E_{D^0 \text{bar}} - E_{\text{beam}}$
- Beam constrained mass: $M_{BC} = \sqrt{E_{\text{beam}}^2/c^4 - |\vec{p}_{\bar{D}^0}|^2/c^2}$
- Branching fraction: $B_{sig} = \frac{N_{sig}}{B_{\pi^0 \rightarrow \gamma\gamma} \sum_a N_{tag}^a \epsilon_{tag,sig}^a / \epsilon_{tag}^a}$, a indicate the tag mode
- Background: model obtained with data-driven method

FCNC Processes

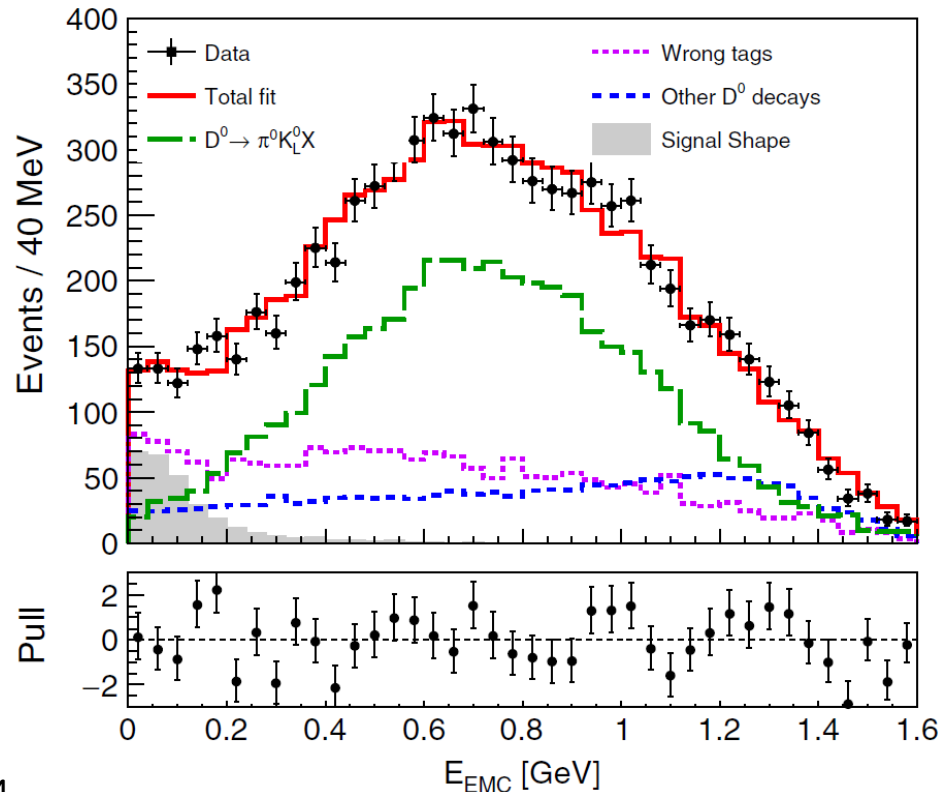
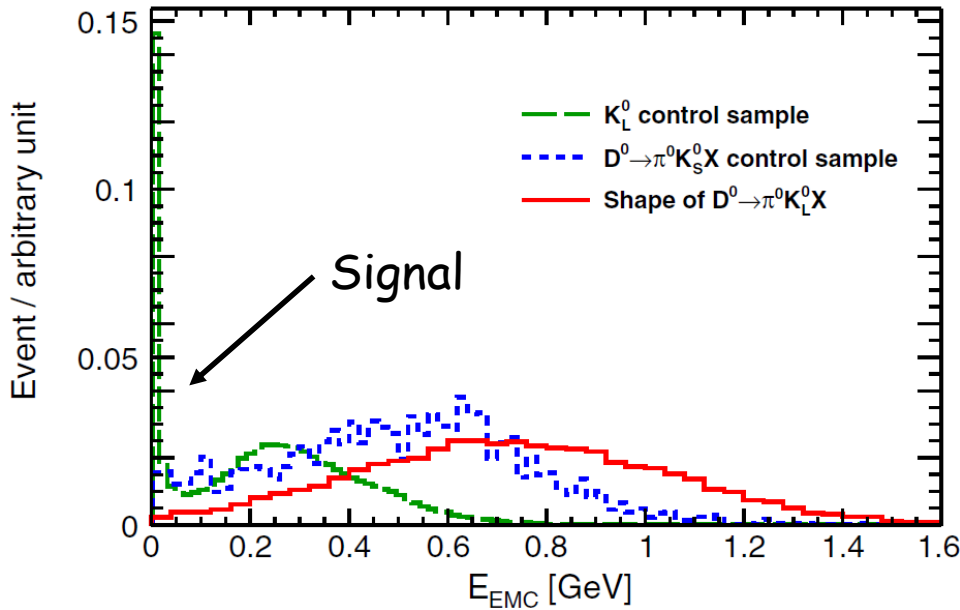
BESIII
PRD 105 (2022) L071102



EMC energy not associated with signal and tag decays

Fit with MC shape

$$N_{\text{sig}} = 14 \pm 30$$



Upper limit at 90% CL: $B_{\text{sig}} = 2.1 \times 10^{-4}$

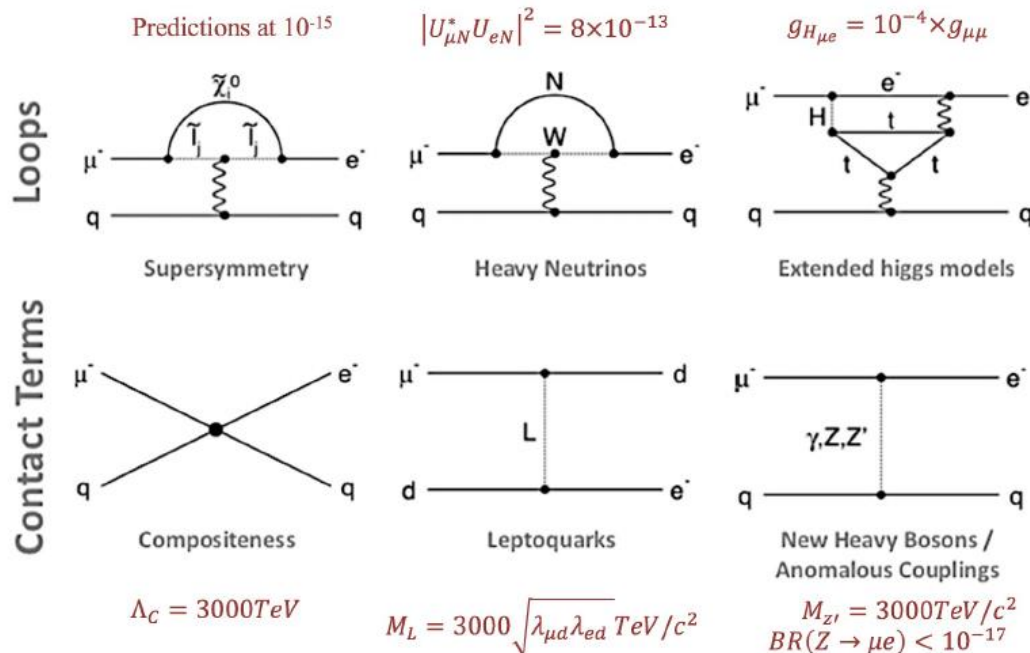
First experimental search for $D^0 \rightarrow \pi^0 \nu \bar{\nu}$

Plan to collect about 20 fb^{-1} at $\psi(3770)$

LFV Processes

- The LFV process is forbidden in SM, however, flavor non-conserving mixing among generations has been observed in neutrino oscillations.
- The smallness of neutrino masses leads to a very large suppression of the predicted branching fractions [1]. So, any significant sign of a LFV signal could indicate physics beyond the SM.

[1] L. Calibbi et al. Riv. Nuovo Cimento 41, 71 (2018)



LFV Processes

- 468 fb⁻¹ @ Y(4S)
- 39 fb⁻¹ "off peak" (40 MeV below Y(4S))



- Decay chain $e^+e^- \rightarrow c\bar{c}$, $D^{*\pm} \rightarrow D^0\pi^\pm$

- 8 decay modes: $D^0 \rightarrow X^0 e^\pm \mu^\mp$
 $X^0 = \pi^0, \eta, K_S^0, \rho, \omega, \phi, K^{*0}(-\rightarrow K^-\pi^+)$

- 3 normalization modes
 $D^0 \rightarrow K^-\pi^+\pi^+\pi^-, K^-K^+\pi^+\pi^-, \pi^-\pi^+\pi^+\pi^-$

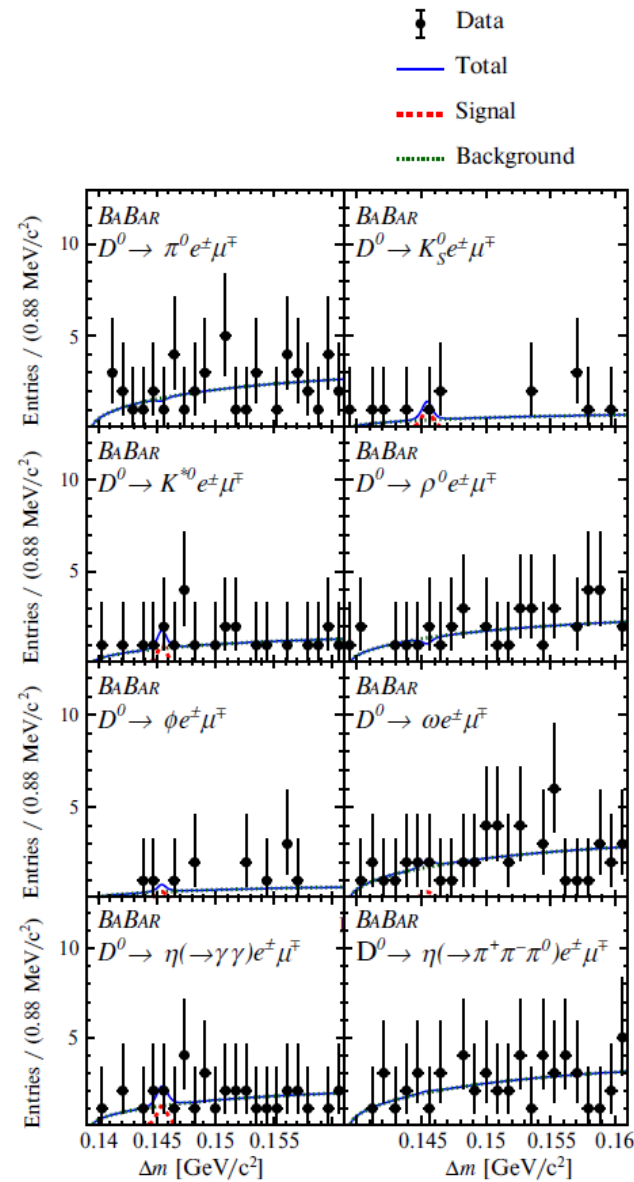
- Full reconstruction of signal modes

- Maximum likelihood fit to $\Delta m = m(D^{*\pm}) - m(D^0)$

- Branching fraction:
$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{sig}}}{N_{\text{norm}}} \frac{\epsilon_{\text{norm}}}{\epsilon_{\text{sig}}} \frac{\mathcal{L}_{\text{norm}}}{\mathcal{L}_{\text{sig}}} \frac{\mathcal{B}_{\text{norm}}}{\mathcal{B}(X^0)}$$

- Signal: Cruijff function,
 ϕ mode: 2 asymmetric-sigma Gaussian
 Background: Argus function

BABAR
PRD 101 (2020) 112003



$$D^0 \rightarrow X^0 e^\pm \mu^\mp$$

- No signal found
- Upper limits calculated at 90% confidence level using Feldman-Cousins method
- 1-2 order of magnitude more stringent constraints

Decay mode	N_{sig} (candidates)	ϵ_{sig} (%)	\mathcal{B} ($\times 10^{-7}$)	\mathcal{B} 90% U.L. ($\times 10^{-7}$)	
				BABAR	Previous
$D^0 \rightarrow \pi^0 e^\pm \mu^\mp$	$-0.3 \pm 2.0 \pm 0.9$	2.15 ± 0.03	$-0.6 \pm 4.8 \pm 2.2$	8.0	860
$D^0 \rightarrow K_S^0 e^\pm \mu^\mp$	$0.7 \pm 1.7 \pm 0.7$	3.01 ± 0.04	$1.9 \pm 4.6 \pm 1.9$	8.7	500
$D^0 \rightarrow \bar{K}^{*0} e^\pm \mu^\mp$	$0.8 \pm 1.8 \pm 0.8$	2.31 ± 0.03	$2.8 \pm 6.1 \pm 2.6$	12.5	830
$D^0 \rightarrow \rho^0 e^\pm \mu^\mp$	$-0.7 \pm 1.7 \pm 0.4$	2.10 ± 0.03	$-1.8 \pm 4.4 \pm 1.0$	5.0	490
$D^0 \rightarrow \phi e^\pm \mu^\mp$	$0.0 \pm 1.4 \pm 0.3$	3.43 ± 0.04	$0.1 \pm 3.8 \pm 0.9$	5.1	340
$D^0 \rightarrow \omega e^\pm \mu^\mp$	$0.4 \pm 2.3 \pm 0.5$	1.46 ± 0.03	$1.8 \pm 9.5 \pm 1.9$	17.1	1200
$D^0 \rightarrow \eta e^\pm \mu^\mp$			$6.1 \pm 9.7 \pm 2.3$	22.5	1000
with $\eta \rightarrow \gamma\gamma$	$1.6 \pm 2.3 \pm 0.5$	2.96 ± 0.04	$7.0 \pm 10.5 \pm 2.4$	24.0	
with $\eta \rightarrow \pi^+ \pi^- \pi^0$	$0.0 \pm 2.8 \pm 0.7$	2.46 ± 0.04	$0.4 \pm 25.8 \pm 6.0$	43.0	

LNV Processes

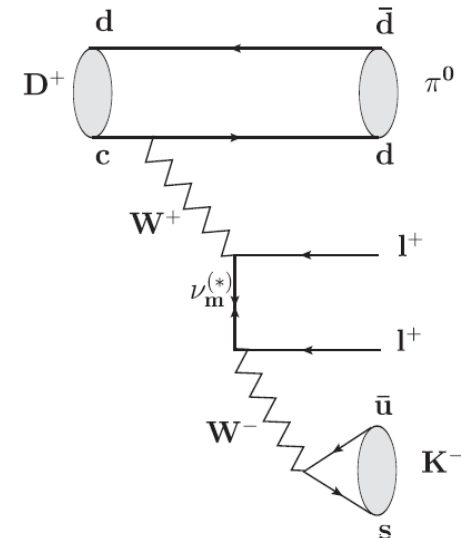
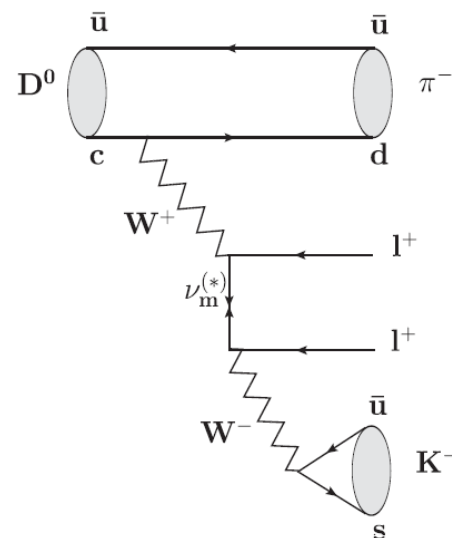
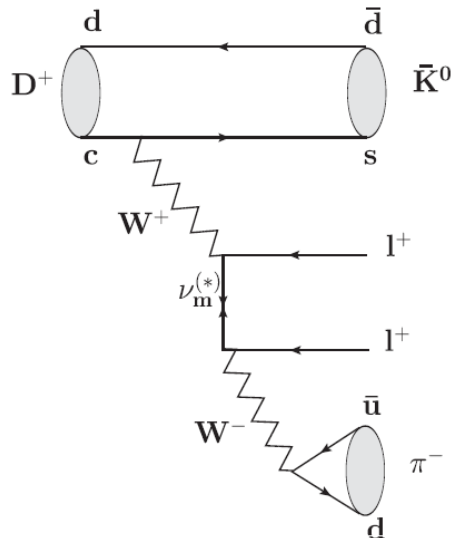
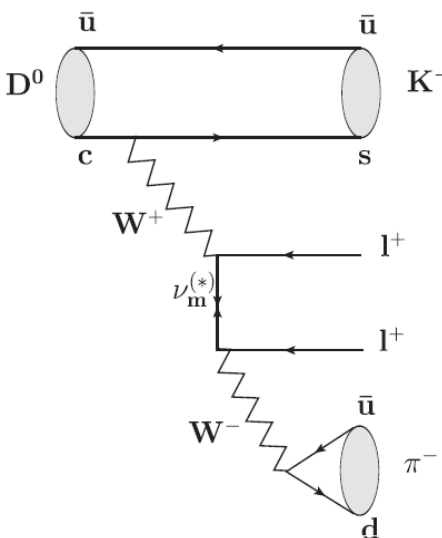
- Lepton number (LN) is conserved in the Standard Model.
- Neutrino oscillation $\rightarrow m_\nu \neq 0 \rightarrow$ New Physics scenario.
- Nature of neutrino: Majorana or Dirac?
- Majorana neutrino can violate LN by two unit
- LNV is introduced in many New Physics models

$$\begin{pmatrix} \nu_\uparrow \\ \nu_\downarrow \\ \bar{\nu}_\uparrow \\ \bar{\nu}_\downarrow \end{pmatrix}$$

or $\begin{pmatrix} \nu_\uparrow \\ \nu_\downarrow \end{pmatrix}$

Dirac

Majorana



(a) $D^0 \rightarrow K^- \pi^- l^+ l^+$ (CF)

(b) $D^+ \rightarrow \bar{K}^0 \pi^- l^+ l^+$ (CF)

(c) $D^0 \rightarrow K^- \pi^- l^+ l^+$ (DCS)

(d) $D^+ \rightarrow K^- \pi^0 l^+ l^+$ (DCS)

LNV Processes

2.93 fb⁻¹ @ 3.773 GeV

Single-Tag analysis

3 channels investigated



$$\Delta E = E_D - E_{\text{beam}} \quad M_{\text{BC}} = \sqrt{E_{\text{beam}}^2 - |\vec{p}_D|^2}$$

Requirements on ΔE to suppress background

Branching fraction:

$$\mathcal{B}_{D \rightarrow K \pi e^+ e^+} = \frac{N_{\text{sig}}}{2 \cdot N_{\text{DD}}^{\text{tot}} \cdot \epsilon \cdot \mathcal{B}}$$

Channels investigated | UL @ 90% CL

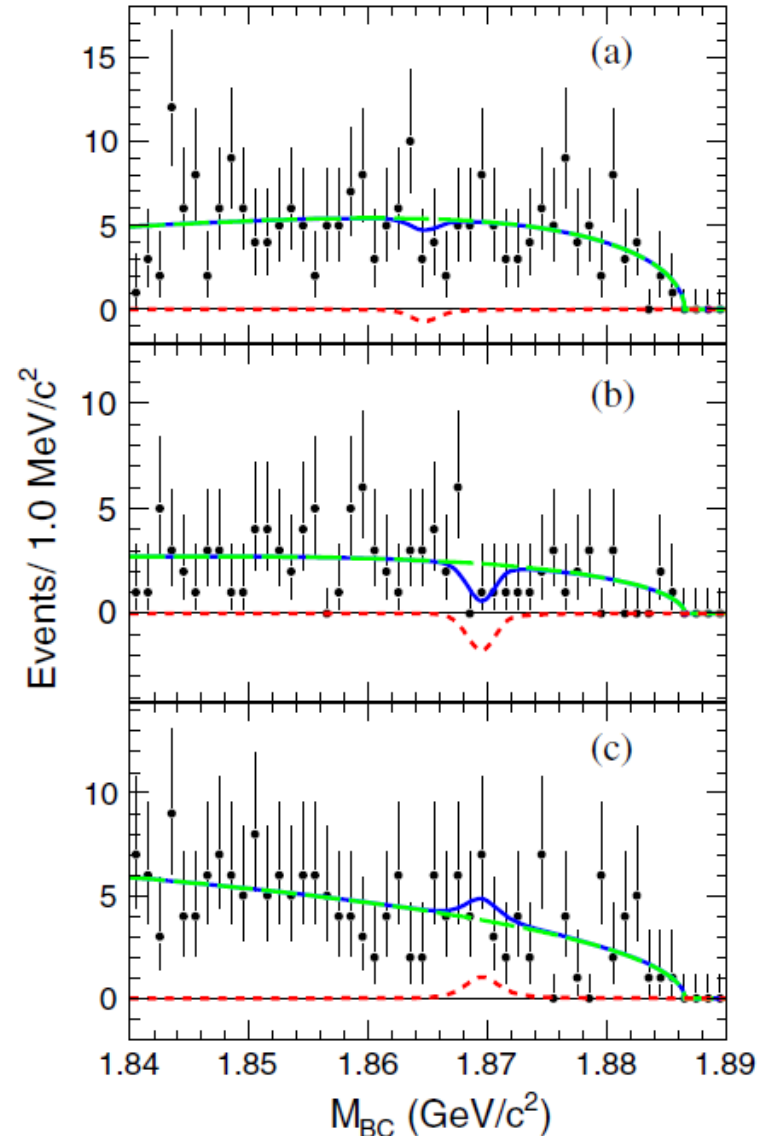
$$D^0 \rightarrow K^- \pi^- e^+ e^+ \quad < 2.8 \times 10^{-6}$$

$$D^+ \rightarrow K_S^0 \pi^- e^+ e^+ \quad < 3.3 \times 10^{-6}$$

$$D^+ \rightarrow K^- \pi^0 e^+ e^+ \quad < 8.5 \times 10^{-6}$$

First searches

BESIII
PRD 99 (2019) 112002

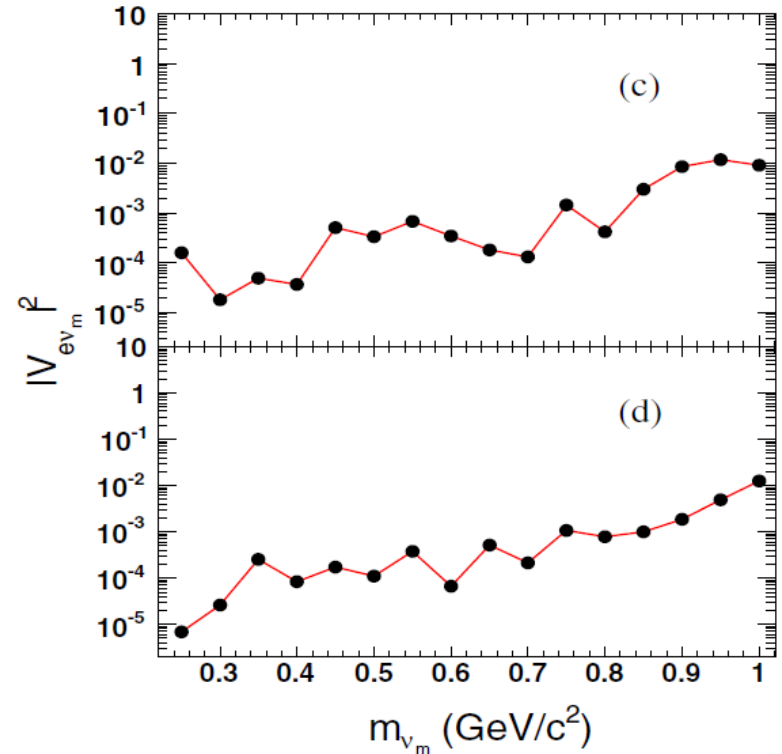
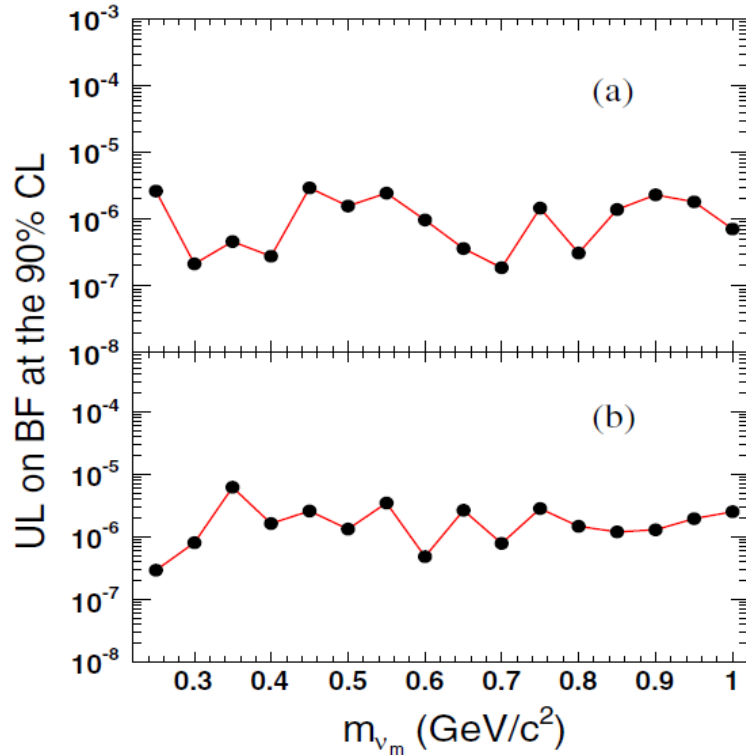


LNV Processes

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PRD 99 (2019) 112002

$D \rightarrow K\pi e^+e^-$

Search for Majorana neutrino



Different m_ν hypothesis tested

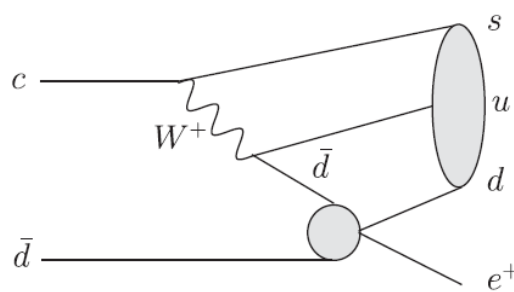
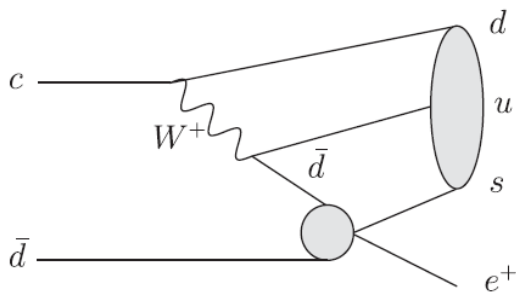
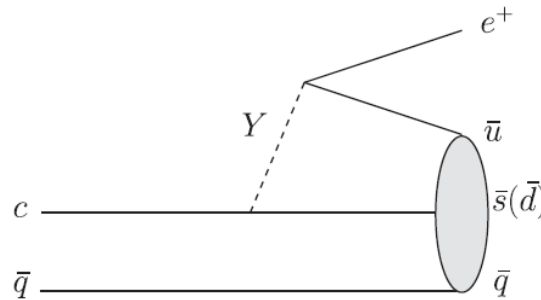
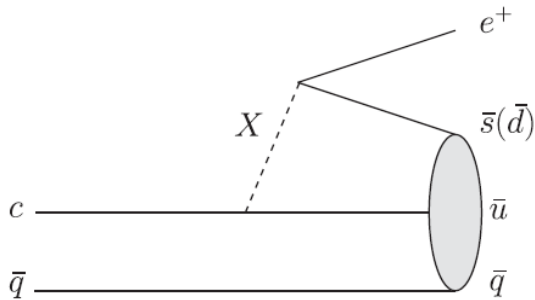
between 0.25 and 1 GeV/c^2

BF related to mixing matrix elements

$$\frac{\Gamma(m_{\nu_m}, V_{e\nu_m}(m_{\nu_m}))}{\Gamma(m_{\nu_m}, V'_{e\nu_m}(m_{\nu_m}))} = \frac{|V_{e\nu_m}(m_{\nu_m})|^4}{|V'_{e\nu_m}(m_{\nu_m})|^4} \quad 17$$

BNV & LNV Processes

- Asymmetry of matter and anti-matter
- Universe evolution
- BNV: even a small amount would have major consequences on the universe and its evolution.
- BNV is allowed in GUTs and SM extensions
- Prediction of $B(D^+ \rightarrow (\bar{\Lambda}^+))$ is no more than 10^{-29} (PRD72, 095001)



SM extension:

under six operators

$$\Delta(B-L) = 0$$

under seven operators

$$\Delta(B-L) = 2$$

BNV-LNV Processes

BESIII
PRD 101 (2020) 031102

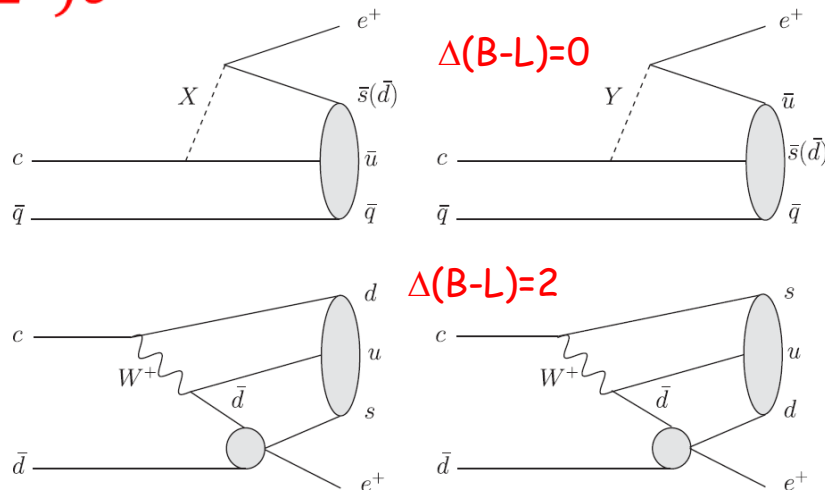


- 2.93 fb⁻¹ @ 3,773 GeV
- Decay chain $e^+e^- \rightarrow D^+D^-$ (8×10^6 events)
 $D^+ \rightarrow \bar{\Lambda}(\bar{\Sigma}^0)e^+$, $D^+ \rightarrow \Lambda(\Sigma^0)e^+$
 $\Lambda \rightarrow p\pi^-$, $\Sigma^0 \rightarrow \gamma\Lambda$

• First measurement

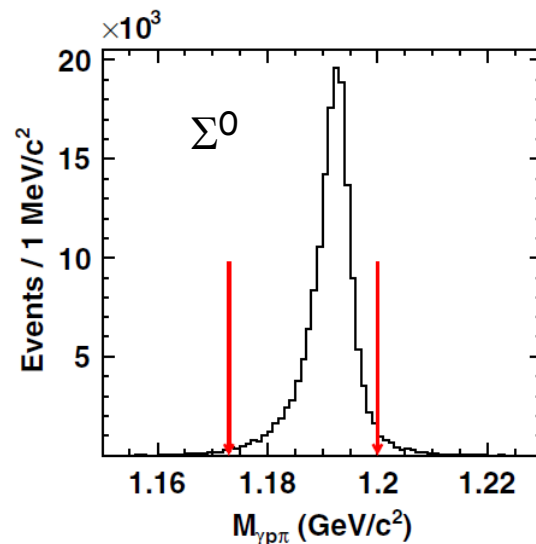
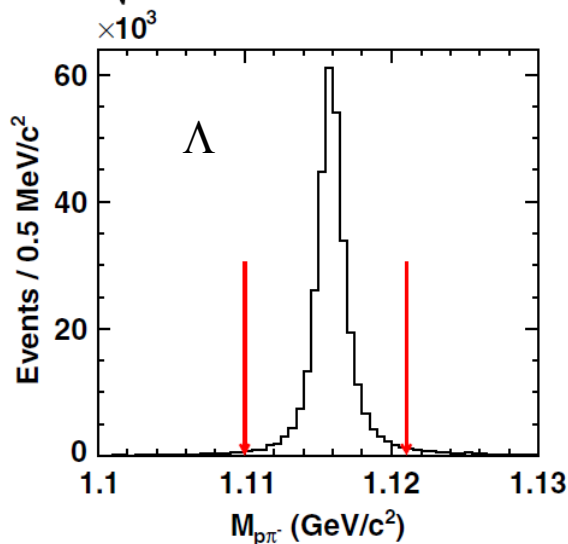
• Energy difference: $\Delta E = E_D - E_{\text{beam}}$

$$\text{Beam constrained mass: } M_{\text{BC}} = \sqrt{E_{\text{beam}}^2 - \vec{p}_D^2}$$



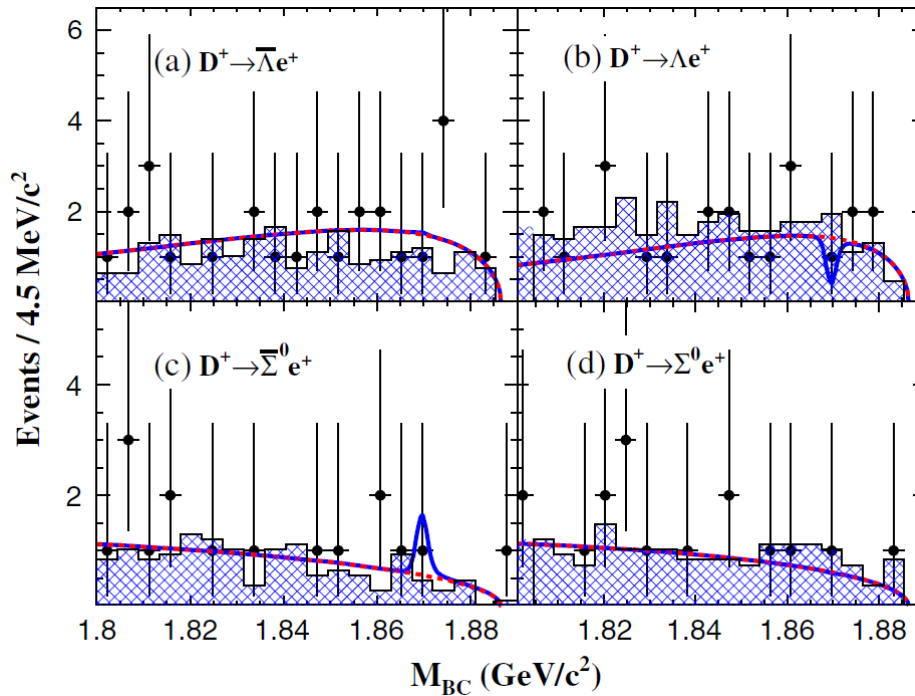
MC simulations

Σ^0 asymmetric selection



BNV-LNV Processes

BESIII
PRD 101 (2020) 031102



Signal: MC shape + Gaussian
Background: ARGUS function
Branching fraction

$$B^{UL} = N_{sig}^{UL} / (2 \cdot N_{D^+D^-}^{tot} \cdot \epsilon \cdot B_{\Lambda, \Sigma^0})$$

First measurement

Mode	N_{sig}^{UL}	ϵ (%)	B^{UL}
Λe^+	5.6	31.11 ± 0.14	1.1×10^{-6}
$\bar{\Lambda} e^+$	3.4	31.18 ± 0.10	6.5×10^{-7}
$\Sigma^0 e^+$	4.5	16.31 ± 0.07	1.7×10^{-6}
$\bar{\Sigma}^0 e^+$	3.5	16.40 ± 0.07	1.3×10^{-6}

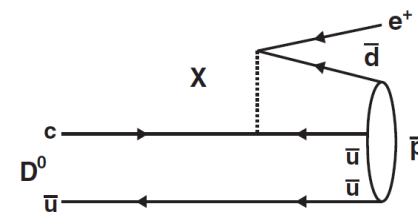
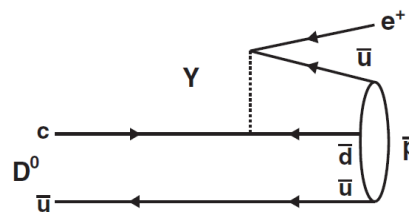
BNV-LNV Processes

BESIII
PRD 105 (2022) 032006

$D^0 \rightarrow pe^-$

• 2.93 fb⁻¹ @ 3,773 GeV

• Decay chain $e^+e^- \rightarrow \bar{D}^0 D^0$, $D^0 \rightarrow pe^- + c.c.$
 $\bar{D}^0 \rightarrow K^+\pi^-, K^+\pi^-\pi^0, K^+\pi^-\pi^+\pi^+$



• X and Y heavy hypothetical gauge bosons

production mechanism

• Double-Tag method

• Full reconstruction of signal modes

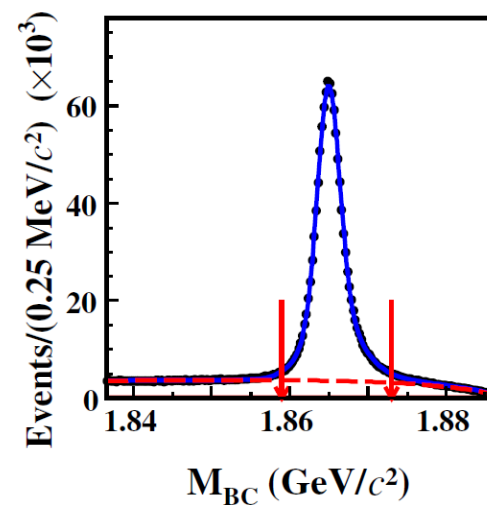
• Energy difference: $\Delta E = E_{D^0\text{bar}} - E_{\text{beam}}$

$$\text{Beam constrained mass: } M_{BC} = \sqrt{E_{\text{beam}}^2/c^4 - |\vec{p}_{D^0}|^2/c^2}$$

• Branching fraction: $B_{sig} = \frac{N_{DT}}{N_{ST}\epsilon_{sig}}$

• Signal: MC shape + double Gaussian
 Background: Argus function

Single-Tag fit



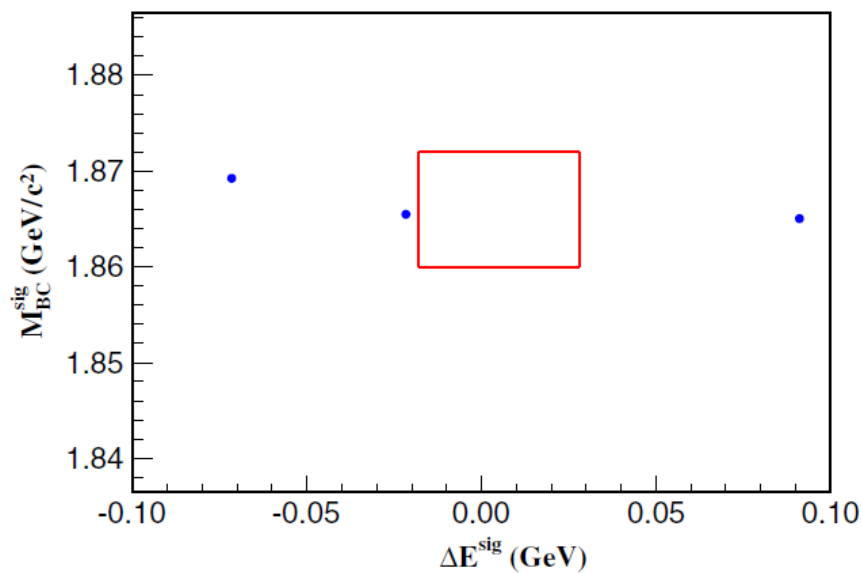
$\bar{D}^0 \rightarrow K^+\pi^-\pi^0$

BNV-LNV Processes

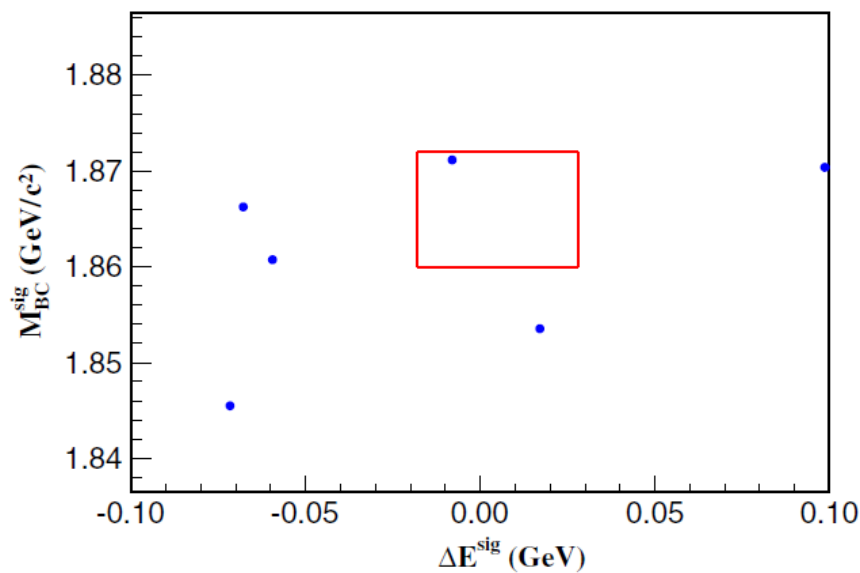
BESIII
PRD 105 (2022) 032006

$D^0 \rightarrow pe^-$

- Asymmetric shapes from MC studies
- No obvious signal observed
- Upper limits $B_{D^0 \rightarrow \bar{p}e^+} < 1.2 \cdot 10^{-6}$ and $B_{D^0 \rightarrow pe^-} < 2.2 \cdot 10^{-6}$
- Most stringent constraints, but far from predictions



$D^0 \rightarrow \bar{p}e^+$



$D^0 \rightarrow pe^-$

FCNC-LFV-LNV Processes

LHCb
JHEP06 (2021) 044

- 1.6 fb⁻¹, 2016 dataset (8 TeV)
- 25 charm decays
- SM allowed decays involve FCNC or weak annihilation
- Forbidden in SM at tree level and CKM suppressed
- Dominated by LD tree level contributions
- Regions dominated by resonances in dilepton mass are vetoed when fitting

$$D^+_{(s)} \rightarrow hll$$

FCNC

$$\begin{aligned} D^+_{(s)} &\rightarrow \pi^+ e^+ e^- \\ D^+_{(s)} &\rightarrow \pi^+ \mu^+ \mu^- \\ D^+_{(s)} &\rightarrow K^+ e^+ e^- \\ D^+_{(s)} &\rightarrow K^+ \mu^+ \mu^- \end{aligned}$$

Resonance dominated

$$\begin{aligned} D^+_{(s)} &\rightarrow \pi^+ \phi(\mu^+ \mu^-) \\ D^+_{(s)} &\rightarrow K^+ \phi(e^+ e^-) \end{aligned}$$

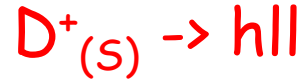
LFV, LFV & LNV

$$\begin{aligned} D^+_{(s)} &\rightarrow \pi^+ \mu^\pm e^\mp \\ D^+_{(s)} &\rightarrow K^+ \mu^\pm e^\mp \end{aligned}$$

$$\begin{aligned} D^+ &\rightarrow K^- \mu^+ e^+ \\ D^+_{(s)} &\rightarrow \pi^- \mu^+ e^+ \\ D^+_{(s)} &\rightarrow \pi^- e^+ e^+ \\ D^+_{(s)} &\rightarrow \pi^- \mu^+ \mu^+ \\ D^+ &\rightarrow K^- e^+ e^+ \\ D^+ &\rightarrow K^- \mu^+ \mu^+ \end{aligned}$$

FCNC-LFV-LNV Processes

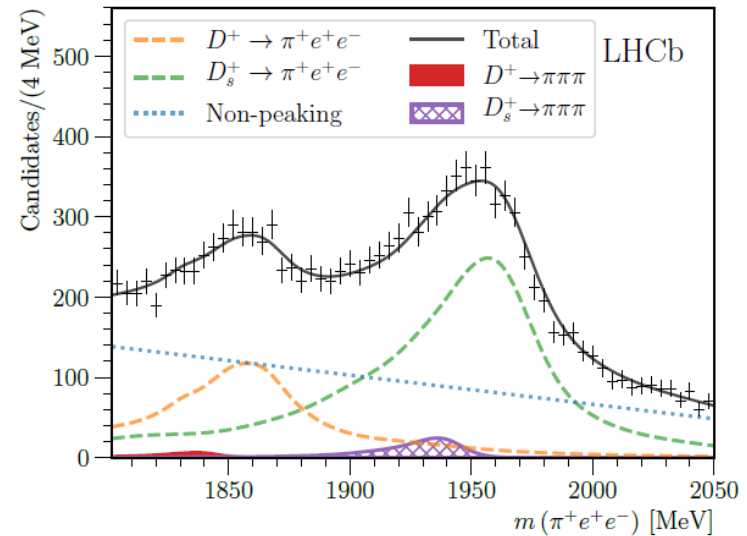
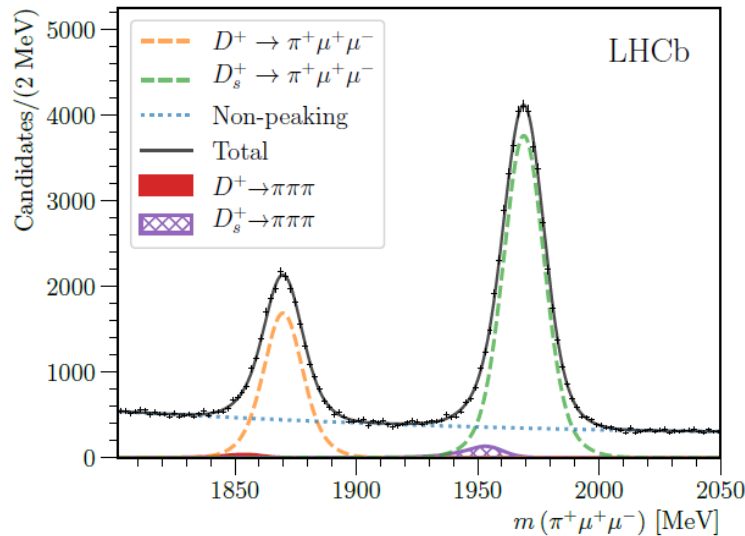
LHCb
JHEP06 (2021) 044



Normalization with $D^+_{(s)} \rightarrow \pi^+ \phi(l^+l^-)$

Signal: double Gaussian

Background: exponential (muons) or third order Chebyshev polynomial (electrons)



Channel	\mathcal{B} [2]	Fitted yield
$D^+ \rightarrow (\phi \rightarrow \mu^- \mu^+) \pi^+$	$(1.63 \pm 0.12) \times 10^{-6}$	$18\,100 \pm 340$
$D^+ \rightarrow (\phi \rightarrow e^- e^+) \pi^+$	$(1.67 \pm 0.07) \times 10^{-6}$	2160 ± 180
$D_s^+ \rightarrow (\phi \rightarrow \mu^- \mu^+) \pi^+$	$(1.33 \pm 0.10) \times 10^{-5}$	$42\,000 \pm 400$
$D_s^+ \rightarrow (\phi \rightarrow e^- e^+) \pi^+$	$(1.37 \pm 0.05) \times 10^{-5}$	5320 ± 180

FCNC-LFV-LNV Processes

LHCb
JHEP06 (2021) 044

Results consistent with background only hypothesis

World's best limits for 23 decays

$D_{(s)}^+ \rightarrow hll$

Decay	Branching fraction upper limit [10^{-9}]				Improvement	
	D^+		D_s^+		D^+	D_s^+
	90 % CL	95 % CL	90 % CL	95 % CL		
$D_{(s)}^+ \rightarrow \pi^+ \mu^+ \mu^-$	67	74	180	210	1.1	2.3
$D_{(s)}^+ \rightarrow \pi^- \mu^+ \mu^+$	14	16	86	96	1.6	1.4
$D_{(s)}^+ \rightarrow K^+ \mu^+ \mu^-$	54	61	140	160	79.0	150.0
$D_{(s)}^+ \rightarrow K^- \mu^+ \mu^+$	-	-	26	30	-	500.0
$D_{(s)}^+ \rightarrow \pi^+ e^+ \mu^-$	210	230	1100	1200	14.0	11.0
$D_{(s)}^+ \rightarrow \pi^+ \mu^+ e^-$	220	220	940	1100	16.0	21.0
$D_{(s)}^+ \rightarrow \pi^- \mu^+ e^+$	130	150	630	710	16.0	13.0
$D_{(s)}^+ \rightarrow K^+ e^+ \mu^-$	75	83	790	880	16.0	18.0
$D_{(s)}^+ \rightarrow K^+ \mu^+ e^-$	100	110	560	640	28.0	17.0
$D_{(s)}^+ \rightarrow K^- \mu^+ e^+$	-	-	260	320	-	23.0
$D_{(s)}^+ \rightarrow \pi^+ e^+ e^-$	1600	1800	5500	6400	0.7	2.3
$D_{(s)}^+ \rightarrow \pi^- e^+ e^+$	530	600	1400	1600	2.1	3.0
$D_{(s)}^+ \rightarrow K^+ e^+ e^-$	850	1000	4900	5500	1.2	0.8
$D_{(s)}^+ \rightarrow K^- e^+ e^+$	-	-	770	840	-	6.7

LNV-LFV Processes

BABAR
PRL 124 (2020) 071802

$D^0 \rightarrow hhll$

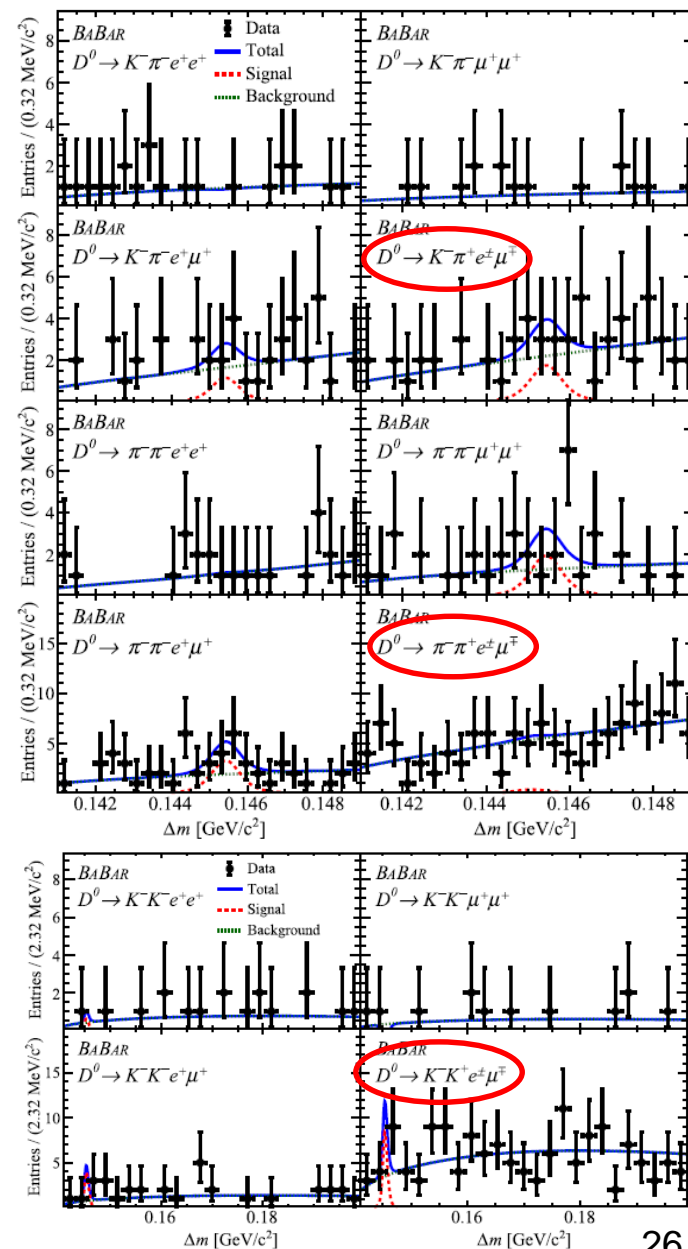
- 468 fb⁻¹ @ Y(4S)
- 39 fb⁻¹ "off peak" (40 MeV below Y(4S))
- Decay chain $e^+e^- \rightarrow c\bar{c}$, $D^{*+} \rightarrow D^0\pi^+$
- 12 decay modes: $D^0 \rightarrow hh'l^+l^-$, $hh'l^+l^-$
 h and $h' = K$ or π

LFV

- 3 normalization modes
 $D^0 \rightarrow K^-\pi^+\pi^+\pi^-$, $K^-K^+\pi^+\pi^-$, $\pi^-\pi^+\pi^+\pi^-$
- Full reconstruction of signal modes
- Maximum likelihood fit to $\Delta m = m(D^{*+}) - m(D^0)$

- Branching fraction:
$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{sig}}}{N_{\text{norm}}} \frac{\epsilon_{\text{norm}}}{\epsilon_{\text{sig}}} \frac{\mathcal{L}_{\text{norm}}}{\mathcal{L}_{\text{sig}}} \mathcal{B}_{\text{norm}}$$

- Signal: Cruijff function
Background: Argus function



LNV-LFV Processes

BABAR
PRL 124 (2020) 071802

$D^0 \rightarrow h h l l$

- No signal found
- Upper limits calculated at 90% confidence level using Feldman-Cousins method
- 1-3 order of magnitude more stringent constraints

Decay mode $D^0 \rightarrow$	N_{sig} (candidates)	ϵ_{sig} (%)	\mathcal{B} ($\times 10^{-7}$)	\mathcal{B} 90% U.L. ($\times 10^{-7}$)	
				BABAR	Previous
$\pi^- \pi^- e^+ e^+$	$0.22 \pm 3.15 \pm 0.54$	4.38 ± 0.05	$0.27 \pm 3.90 \pm 0.67$	9.1	1120
$\pi^- \pi^- \mu^+ \mu^+$	$6.69 \pm 4.88 \pm 0.80$	4.91 ± 0.05	$7.40 \pm 5.40 \pm 0.91$	15.2	290
$\pi^- \pi^- e^+ \mu^+$	$12.42 \pm 5.30 \pm 1.45$	4.38 ± 0.05	$15.41 \pm 6.59 \pm 1.85$	30.6	790
$\pi^- \pi^+ e^\pm \mu^\mp$	$1.37 \pm 6.15 \pm 1.28$	4.79 ± 0.06	$1.55 \pm 6.97 \pm 1.45$	17.1	150
$K^- \pi^- e^+ e^+$	$-0.23 \pm 0.97 \pm 1.28$	3.19 ± 0.05	$-0.38 \pm 1.60 \pm 2.11$	5.0	28 [21]
$K^- \pi^- \mu^+ \mu^+$	$-0.03 \pm 2.10 \pm 0.40$	3.30 ± 0.05	$-0.05 \pm 3.34 \pm 0.64$	5.3	3900
$K^- \pi^- e^+ \mu^+$	$3.87 \pm 3.96 \pm 2.36$	3.48 ± 0.04	$5.84 \pm 5.97 \pm 3.56$	21.0	2180
$K^- \pi^+ e^\pm \mu^\mp$	$2.52 \pm 4.60 \pm 1.35$	3.65 ± 0.05	$3.62 \pm 6.61 \pm 1.95$	19.0	5530
$K^- K^- e^+ e^+$	$0.30 \pm 1.08 \pm 0.41$	3.25 ± 0.04	$0.43 \pm 1.54 \pm 0.58$	3.4	1520
$K^- K^- \mu^+ \mu^+$	$-1.09 \pm 1.29 \pm 0.42$	6.21 ± 0.06	$-0.81 \pm 0.96 \pm 0.32$	1.0	940
$K^- K^- e^+ \mu^+$	$1.93 \pm 1.92 \pm 0.83$	4.63 ± 0.05	$1.93 \pm 1.93 \pm 0.84$	5.8	570
$K^- K^+ e^\pm \mu^\mp$	$4.09 \pm 3.00 \pm 1.59$	4.83 ± 0.05	$3.93 \pm 2.89 \pm 1.45$	10.0	1800

Search for Rare Charm Decays at Belle II

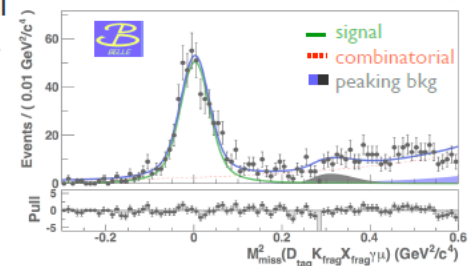
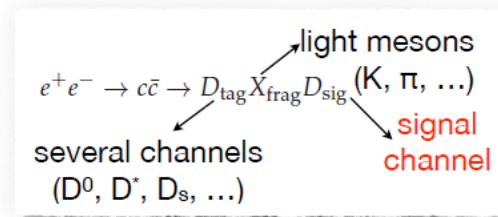
Belle II will search for rare or forbidden charm decays, especially those with *neutrals* or *missing energy* in the final state, for example:

→ $D^0 \rightarrow \gamma\gamma$, $c \rightarrow u$ FCNC unique to Belle II

- current UL $\mathcal{B}(D^0 \rightarrow \gamma\gamma) < 8.5 \times 10^{-7}$ at 90% CL (Belle, PRD 93 051102) is 2 orders of magnitudes higher than SM predictions (PRD 64 074008, PRD 66 014009)
- estimated UL at Belle II $\mathcal{B}(D^0 \rightarrow \gamma\gamma) < 1.5 \times 10^{-7}$ at 90% CL (with 50 ab⁻¹)

→ $D \rightarrow h\nu\bar{\nu}$, $\Lambda_c^+ \rightarrow p\nu\bar{\nu}$, strongly GIM-suppressed in the SM

- powerful reconstruction method: reconstruct the partner charm hadron + fragmentation particles, and then use energy-momentum conservation to determine the invariant mass of the rest (Belle, PRD 95 011102) →
- can be used with *any* type of missing energy (neutrinos, dark matter, axions, other non-SM particles)



BESIII Prospects

White Paper
CPC 44 (2020) 040001

Decay	Upper limit	Experiment	Year	Ref.	BESIII Expected
$D^0 \rightarrow \pi^0 e^+ e^-$	0.4	BESIII	2018	[35]	0.1
$D^0 \rightarrow \eta e^+ e^-$	0.3	BESIII	2018	[35]	0.1
$D^0 \rightarrow \omega e^+ e^-$	0.6	BESIII	2018	[35]	0.2
$D^0 \rightarrow K_S^0 e^+ e^-$	1.2	BESIII	2018	[35]	0.5
$D^0 \rightarrow \rho e^+ e^-$	124.0	E791	2001	[36]	0.5
$D^0 \rightarrow \phi e^+ e^-$	59.0	E791	2001	[36]	0.5
$D^0 \rightarrow \bar{K}^{*0} e^+ e^-$	47.0	E791	2001		0.5
$D^0 \rightarrow \pi^+ \pi^- e^+ e^-$	0.7	BESIII	2018		0.3
$D^0 \rightarrow K^+ K^- e^+ e^-$	1.1	BESIII	2018		0.4
$D^0 \rightarrow K^- \pi^+ e^+ e^-$	4.1	BESIII	2018	[35]	1.6
$D^+ \rightarrow \pi^+ e^+ e^-$	1.1	BaBar	2011	[37]	0.12
$D^+ \rightarrow K^+ e^+ e^-$	1.0	BaBar	2011	[37]	0.46
$D^+ \rightarrow \pi^+ \pi^0 e^+ e^-$	1.4	BESIII	2018	[35]	0.5
$D^+ \rightarrow \pi^+ K_S^0 e^+ e^-$	2.6	BESIII	2018	[35]	1.0
$D^+ \rightarrow K_S^0 K^+ e^+ e^-$	1.1	BESIII	2018	[35]	0.4
$D^+ \rightarrow K^+ \pi^0 e^+ e^-$	1.5	BESIII	2018	[35]	0.6
$D_s^+ \rightarrow \pi^+ e^+ e^-$	13.0	BaBar	2011		70.0
$D_s^+ \rightarrow K^+ e^+ e^-$	3.7	BaBar	2011		1.7

20 fb⁻¹
@ 3.773 GeV

6 fb⁻¹@ 4.18 GeV

Summary

- Rare decays are a great tool for **New Physics** studies
- **Rare charm decays**
 - up-type quark dynamics
 - complementary to strange and beauty results
- Limits are still above SM predictions
- New Physics **effects have not been found yet**
- New results expected from BESIII, BelleII, LHCb, and *Super Tau-Charm Factories*