

Anomalies in neutral-current B-decays

The 2022 Conference on Flavor Physics and CP Violation

Dedicated in memory of Sheldon Stone

The University of Mississippi

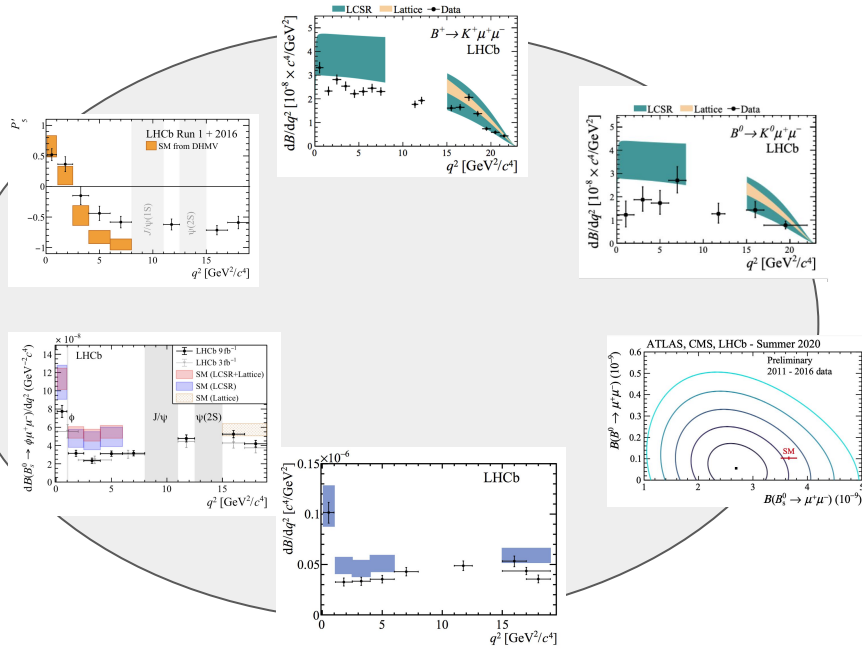
Nico Serra - University of Zurich

On behalf of the LHCb Collaboration

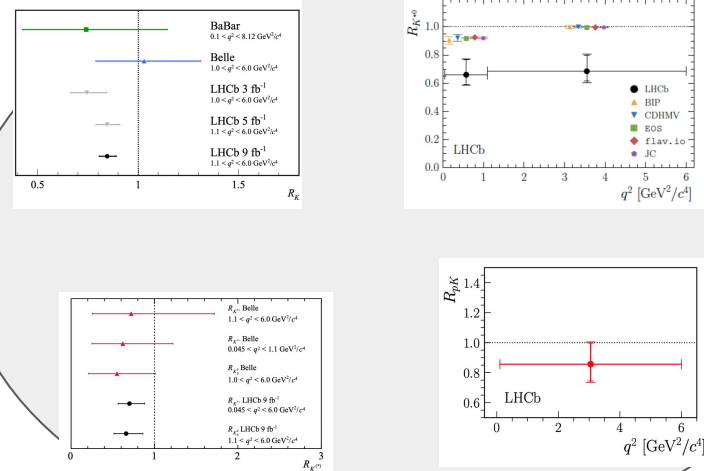


Overview

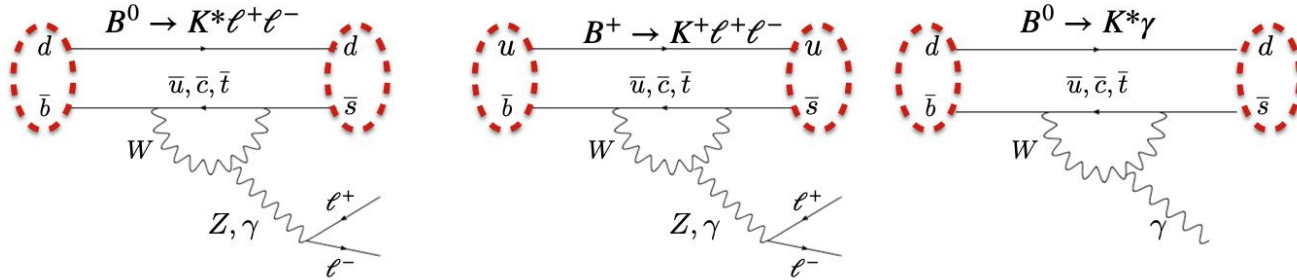
$b \rightarrow s \mu \mu$



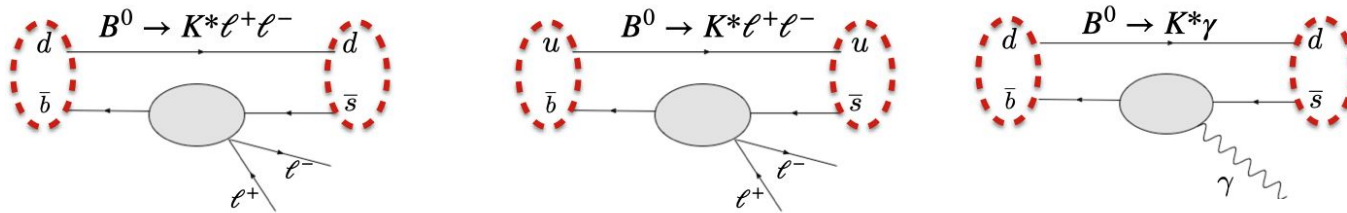
$b \rightarrow s \mu \mu / b \rightarrow s e e$



Effective Hamiltonian



Use an effective operator approach, similar to Fermi theory of weak interaction



$$\mathcal{A}(i \rightarrow f) = \langle f | \mathcal{H}_{\text{eff}} | i \rangle$$

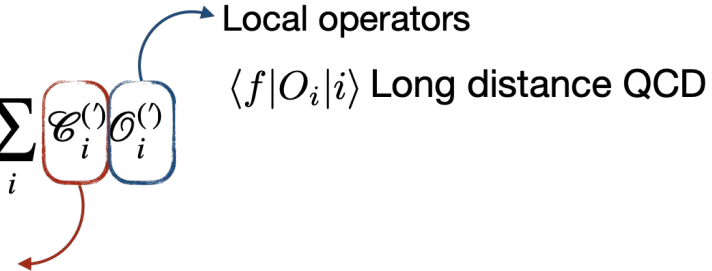
Introduction

Effective Hamiltonian

$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i \mathcal{C}_i^{(\prime)} \mathcal{O}_i^{(\prime)}$$

Wilson Coefficients
Effective coupling

Local operators
 $\langle f | \mathcal{O}_i | i \rangle$ Long distance QCD



Effective Hamiltonian

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Wilson Coefficients
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Local operators
 $\langle f | O_i | i \rangle$ Long distance QCD

New Physics can contribute to different WCs depending on its Lorentz structure

Introduction

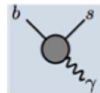
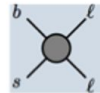
Effective Hamiltonian

$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i \mathcal{C}_i^{(\prime)} \mathcal{O}_i^{(\prime)}$$

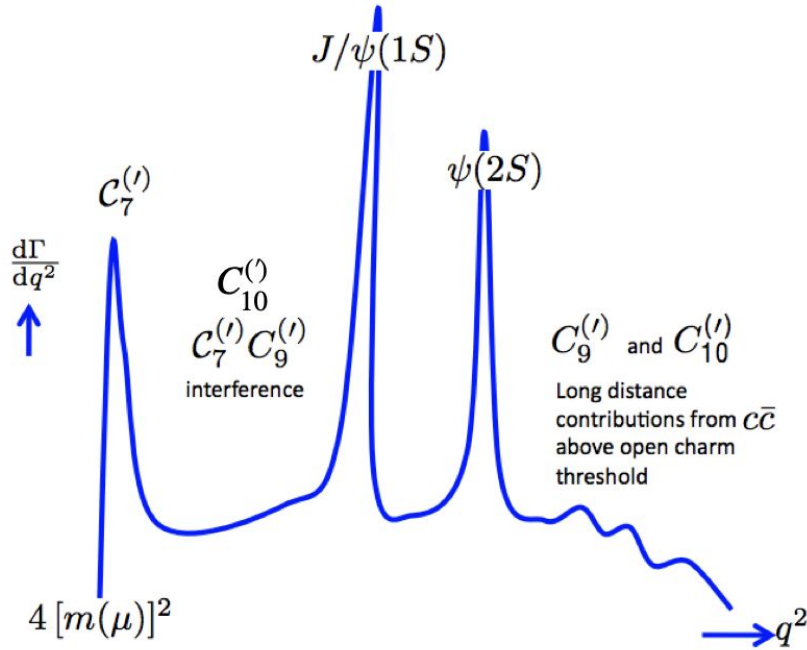
Local operators
 $\langle f | \mathcal{O}_i | i \rangle$ Long distance QCD

Wilson Coefficients
Effective coupling

New Physics can contribute to different WCs depending on its Lorentz structure

Operator \mathcal{O}_i	$B \rightarrow K^{*0} \gamma$	$B \rightarrow K^{*0} \mu^+ \mu^-$	$B \rightarrow \mu^+ \mu^-$
 $\mathcal{O}_7 \sim m_b (\bar{s}_L \sigma_{\mu\nu} b_R) F_{\mu\nu}$	✓	✓	
$\mathcal{O}_9 \sim (\bar{s} b)_{V-A} (\bar{\ell} \ell)_V$		✓	
 $\mathcal{O}_{10} \sim (\bar{s} b)_{V-A} (\bar{\ell} \ell)_A$		✓	✓
$\mathcal{O}_{S,P} \sim (\bar{s} b)_{S+P} (\bar{\ell} \ell)_{S,P}$			✓

Angular analysis of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$



$$\mathcal{A}(i \rightarrow f) = \langle f | \mathcal{H}_{eff} | i \rangle$$

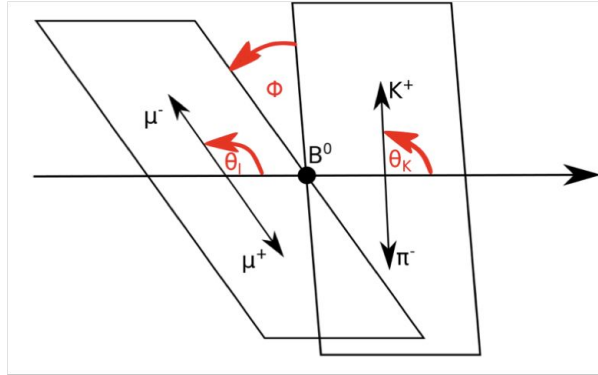
- Six complex amplitudes
- Amplitudes labelled according to the K^* polarization and the L/R chirality of the di-muon

$$A_0^{L,R} \propto [C_{9\mp 10}^+ A_{12} + C_7^+ T_{23}]$$

$$A_{\parallel}^{L,R} \propto [C_{9\mp 10}^- A_1 + C_7^- T_2]$$

$$A_{\perp}^{L,R} \propto [C_{9\mp 10}^- V + C_7^- T_1]$$

Angular analysis of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$



- Differential decay rate described by 3 angles (θ_l, θ_K, Φ) and the di-muon invariant mass squared (q^2)
- Angular observables bilinear combinations of the 6 complex amplitudes
- P_5' is the best known due to the measured discrepancy

$$\frac{1}{\Gamma} \frac{d^3(\Gamma + \bar{\Gamma})}{d \cos \theta_\ell d \cos \theta_K d \phi} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \right. \\ \left. \sqrt{F_L(1 - F_L)} P_5' \sin 2\theta_K \sin \theta_\ell \cos \phi + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + \right. \\ \left. S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

Angular analysis of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$

Several observables proposed references

At large recoil (low- q^2)

$$R_1 = \frac{T_1}{V} \sim 1$$

$$R_2 = \frac{T_2}{A_1} \sim 1$$

$$R_3 = \frac{T_{23}}{A_{12}} \sim \frac{q^2}{m_B^2}$$

P-basis (P_1, \dots, P_8) FF appears in the numerator and in the denominator

$$P'_5 \propto \frac{\mathcal{R}(A_0 A_\perp)}{\sqrt{|A_0|^2 \times |A_\perp|^2}} \quad \text{J. Matias et al. JHEP 04 (2012) 104}$$

Using full form-factors with correlations similar results are obtained with the (S_i) basis

[Altmannshofer et al. JHEP 01 \(2009\) 019](#)

$$S_i = \frac{I_i + \bar{I}_i}{d\Gamma/dq^2 + d\bar{\Gamma}/dq^2}$$

Other observables have been suggested

[Becirevic et al., Nucl.Phys.B 854 \(2012\) 321-339](#)

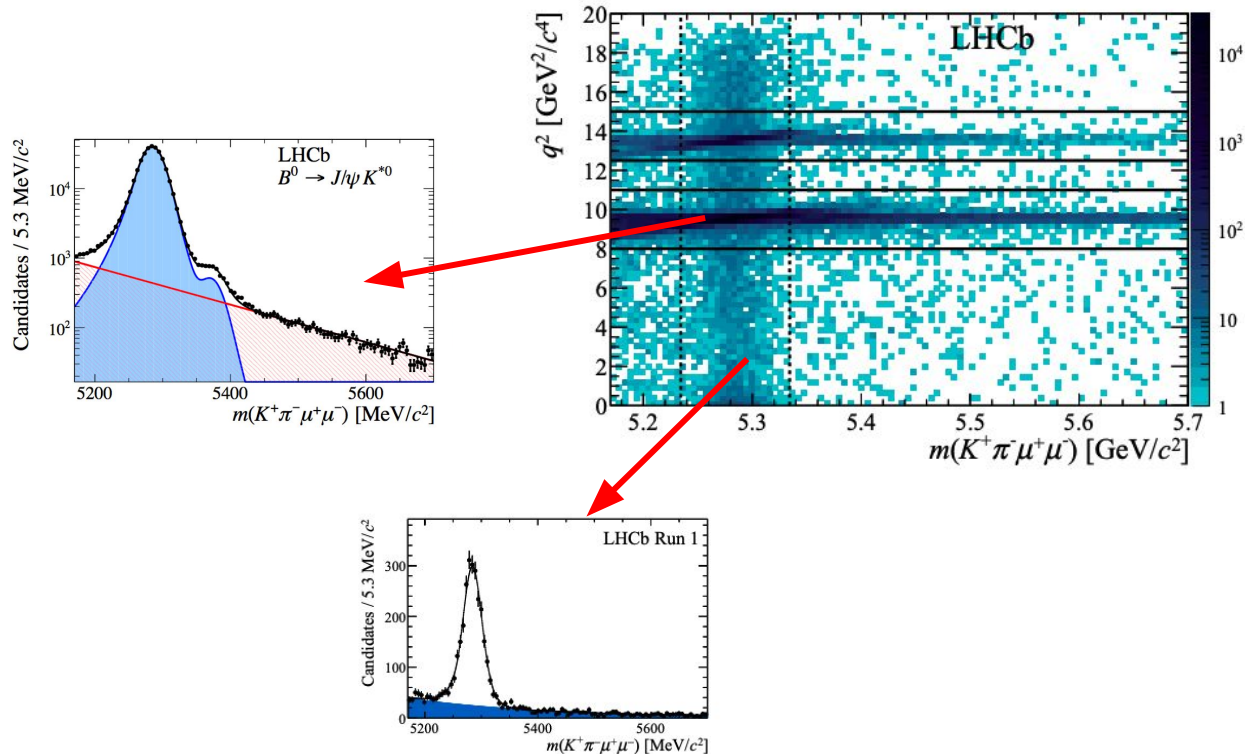
[Bobeth et al., JHEP 07 \(2010\) 098](#)

[Lunghi, Soni, JHEP 11 \(2010\) 121](#)

and references therein

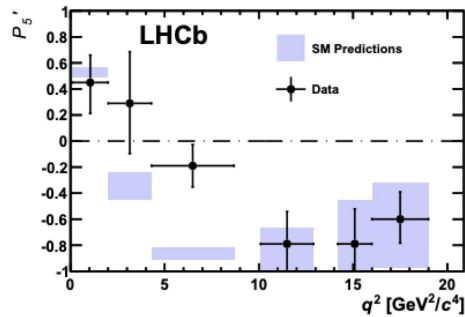
Angular analysis of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$

[LHCb Coll. Phys.Rev.Lett. 125 \(2020\) 1, 011802](#)

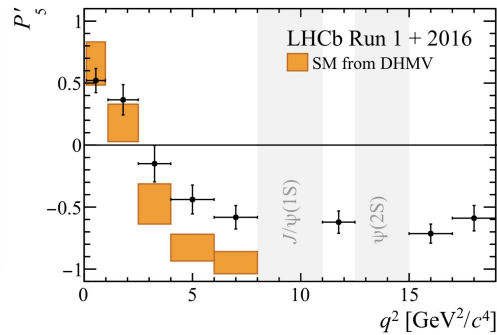


Angular analysis of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$

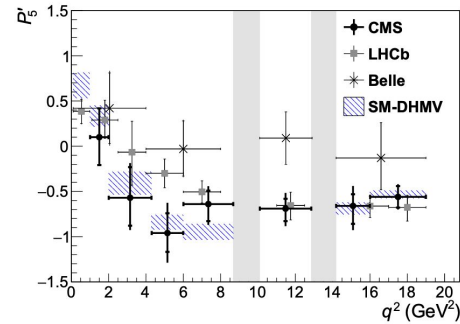
- Deviations from SM predictions observed by LHCb in P_5' (and other angular observables) in the decay $B \rightarrow K^*\mu\mu$ (2013, 1fb^{-1})
- Confirmed by followed up analyses of $B \rightarrow K^*\mu\mu$ (2015, 3fb^{-1} and 2019, 5fb^{-1})



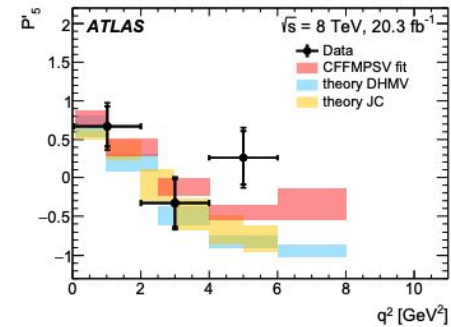
[Phys.Rev.Lett. 111 \(2013\) 191801](#)



[Phys.Rev.Lett. 125 \(2020\) 1, 011802](#)



[Phys.Lett.B 781 \(2018\) 517-541](#)

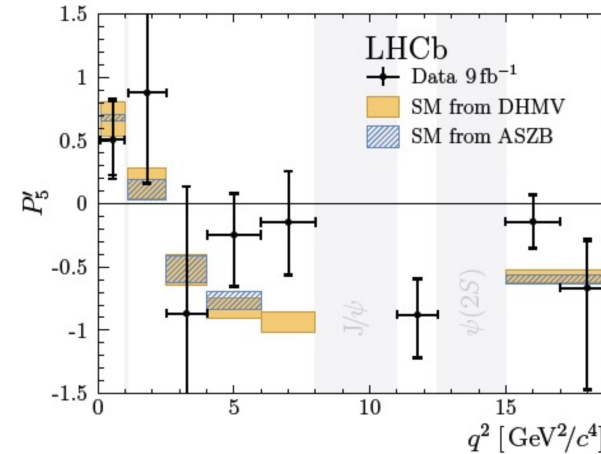
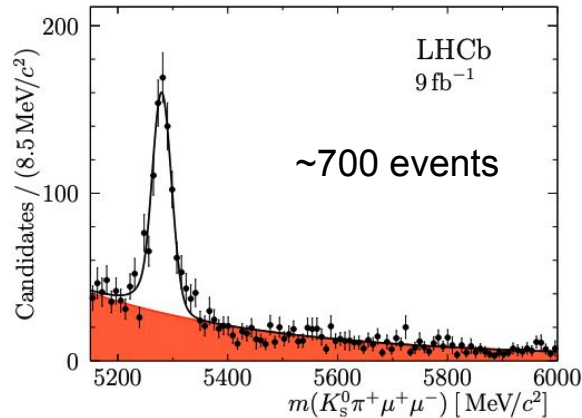


[JHEP 10 \(2018\) 047](#)

Angular analysis of $B^+ \rightarrow K^{*+} \mu \mu$

[LHCb Coll, Phys.Rev.Lett. 126 \(2021\) 16, 161802](#)

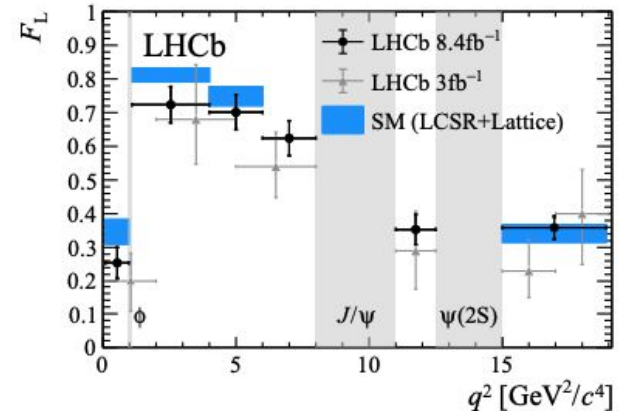
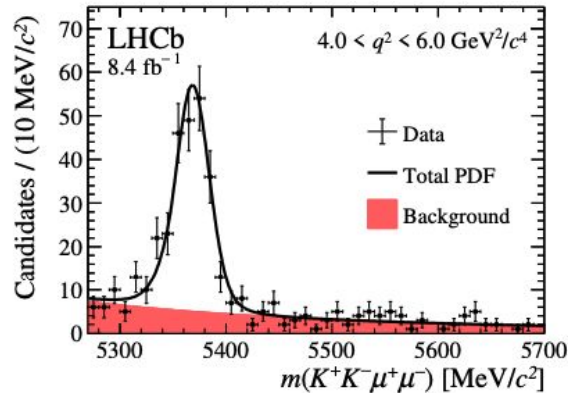
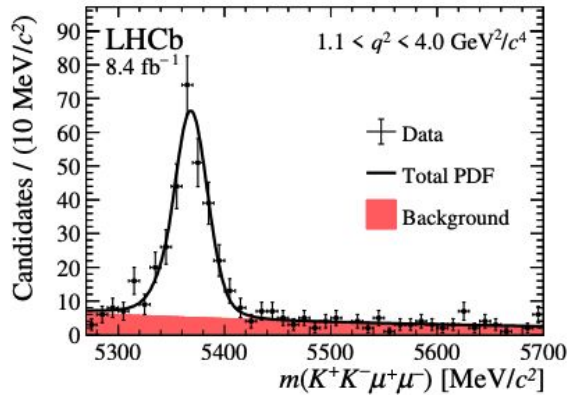
- Angular analysis of $B^+ \rightarrow K^{*+} \mu \mu$ in very good agreement with the tension observed in $B \rightarrow K^* \mu \mu$
- Different systematics and background wrt $B \rightarrow K^* \mu \mu$



Angular analysis of $B_s \rightarrow \Phi \mu \mu$

[LHCb Coll. JHEP 09 \(2015\) 179](#)

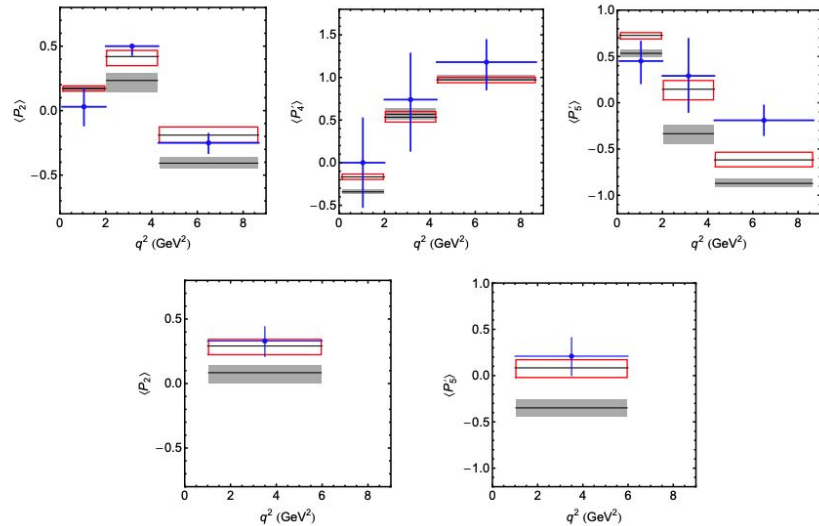
- Angular analyses of the decay $B_s \rightarrow \Phi \mu \mu$ also shows discrepancies wrt SM predictions
- No access to P_5' or A_{FB} since $B_s \rightarrow \Phi \mu \mu$ is not self-tagging



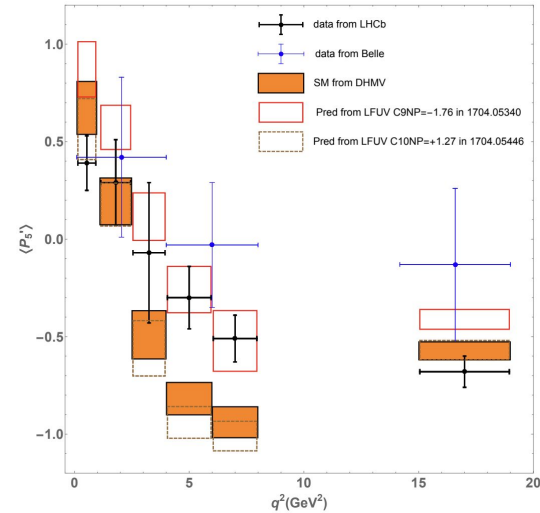
Theory explanations of the $B \rightarrow K^* \mu \mu$ anomaly

- Discrepancies in the angular distribution of $B \rightarrow K^* \mu \mu$ best explained by shift in C_9

[Decotes-Genon, Matias, Virto Phys.Rev.D 88 \(2013\) 074002](#)



[Capdevilla et al., JHEP 01 \(2018\) 093](#)



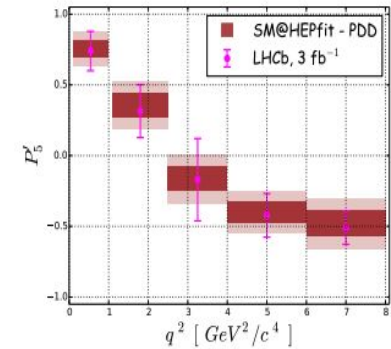
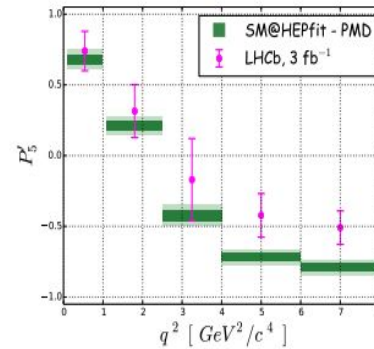
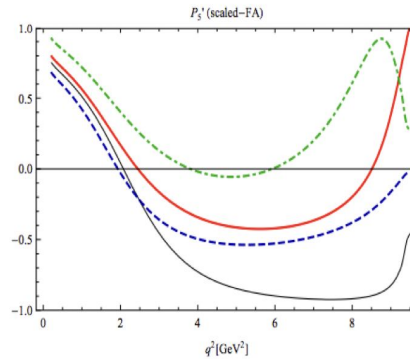
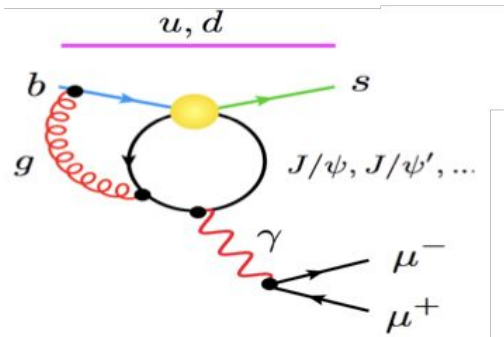
See also [Altmannshofer, Straub Eur.Phys.J.C 73 \(2013\) 2646](#), [Beaujean et al., Eur.Phys.J.C 74 \(2014\) 2897](#), [Hurth et al., JHEP 04 \(2014\) 097](#)

Theory explanations of the $B \rightarrow K^* \mu \mu$ anomaly

- This can be interpreted either as NP or as larger-than-expected charm loop

[Lyon, Zwicky arXiv:1406.0566](#)

[Ciuchini et al., JHEP 06 \(2016\) 116](#)

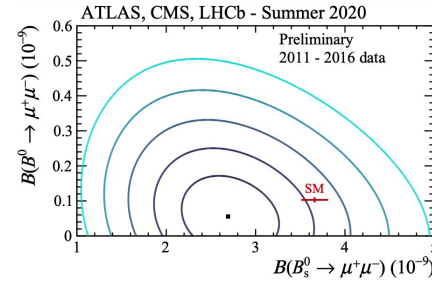
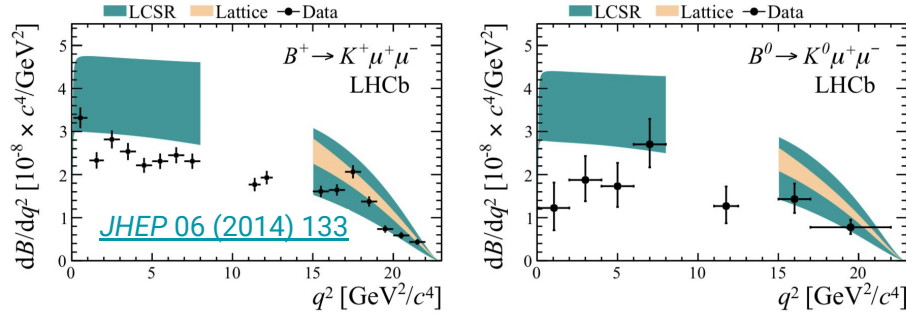


Branching ratio measurements of $b \rightarrow s \mu \mu$

- LHCb observes low values of branching ratios for $b \rightarrow s \mu \mu$ transitions
- Can be explained by shift in C_9 or $C_{9/10}$ simultaneously

[LHCb Coll. Phys. Rev. Lett. 128, 041801](#)

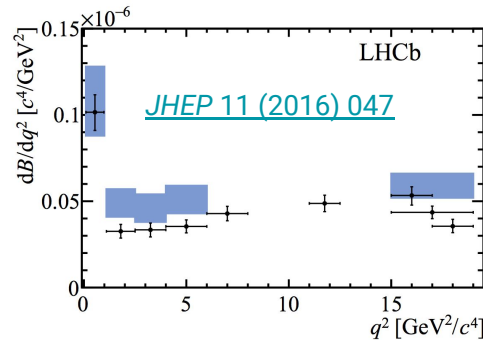
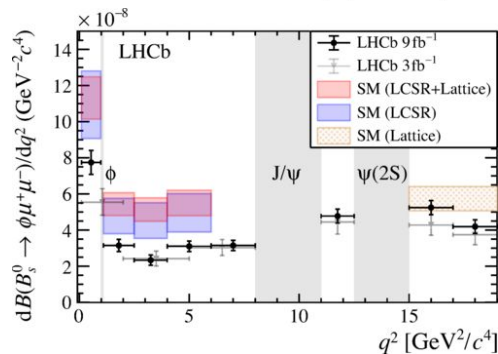
[LHCb Coll., Phys.Rev.D 105 \(2022\) 1, 012010](#)



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-10}$$

[CMS-PAS-BPH-20-003](#)
[LHCb-CONF-2020-002](#)
[ATLAS-CONF-2020-049](#)

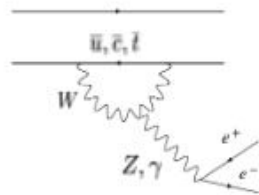
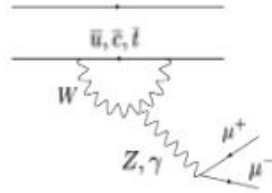


- Waiting for $B_s \rightarrow \mu \mu$ updates since C_{10} is theoretically clean
- Possibility to extract C_{10} also from $B \rightarrow K^* \mu \mu$ angular distributions

LFU tests in rare decays

- Test of LFU are sensitive to those models that have a hierarchical coupling with lepton families
- LFU R-ratios have small theory uncertainty (<1%) [Bordone et al., Eur.Phys.J.C 76 \(2016\) 8, 440](#)
[Isidori, Zwicky JHEP 12 \(2020\) 104](#)

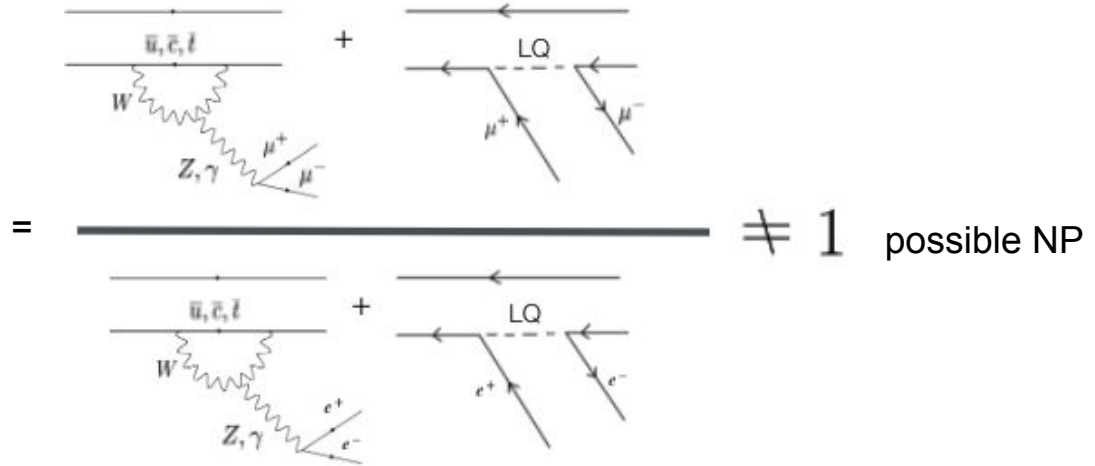
$$R_X = \frac{\int_{q_{\min}}^{q_{\max}} \frac{d\Gamma(H_b \rightarrow X_s \mu \mu)}{dq^2}}{\int_{q_{\min}}^{q_{\max}} \frac{d\Gamma(H_b \rightarrow X_s e e)}{dq^2}} = \frac{\text{Diagram 1}}{\text{Diagram 2}} = 1 \quad \text{SM}$$



LFU tests in rare decays

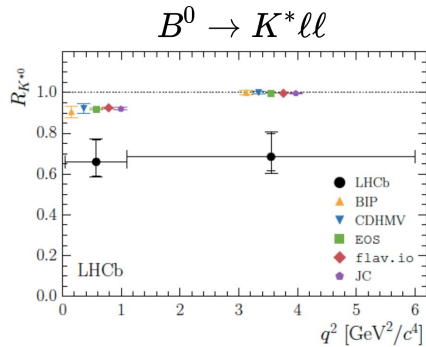
- Test of LFU are sensitive to those models that have a hierarchical coupling with lepton families
- LFU R-ratios have small theory uncertainty (<1%) [Bordone et al., Eur.Phys.J.C 76 \(2016\) 8, 440](#)
[Isidori, Zwicky JHEP 12 \(2020\) 104](#)

$$R_X = \frac{\int_{q_{\min}}^{q_{\max}} \frac{d\Gamma(H_b \rightarrow X_s \mu \mu)}{dq^2}}{\int_{q_{\min}}^{q_{\max}} \frac{d\Gamma(H_b \rightarrow X_s e e)}{dq^2}}$$

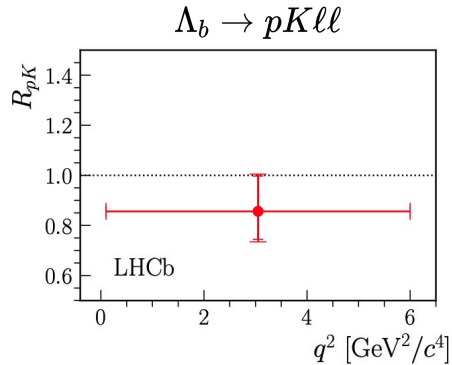


LFU tests in rare decays

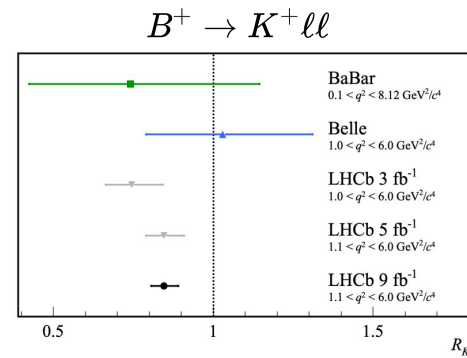
- Since 2014 LHCb measured deviations from LFU in $b \rightarrow sll$ transitions
- Still statistically limited but all measurements of $b \rightarrow s\mu\mu / b \rightarrow see$ ratios are below 1.0 (SM prediction)



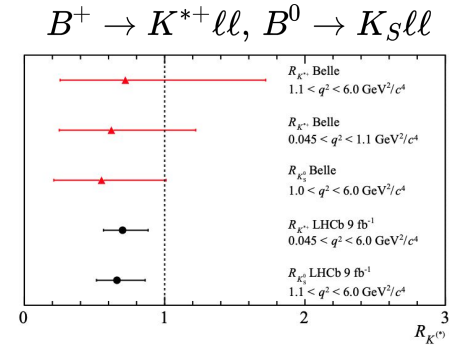
[Phys.Rev.Lett. 125 \(2020\) 1, 011802](#)



[JHEP 05 \(2020\) 040](#)



[Nature Phys. 18 \(2022\) 3, 277-282](#)



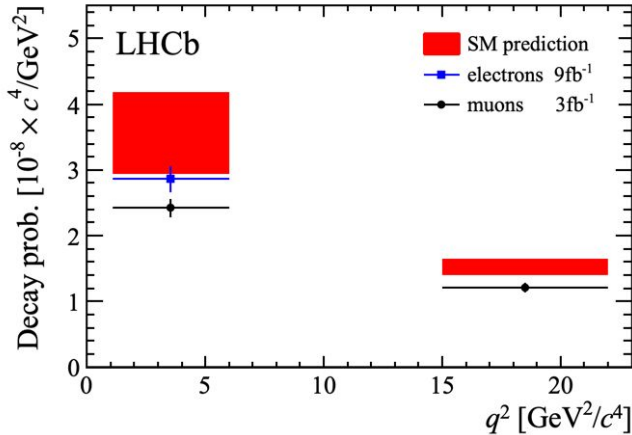
[Phys.Rev.Lett. 128 \(2022\) 19, 191802](#)

[See talk by Silvia Ferreres Solé \(parallel session on Tuesday morning\)](#)

$b \rightarrow sll$ anomalies

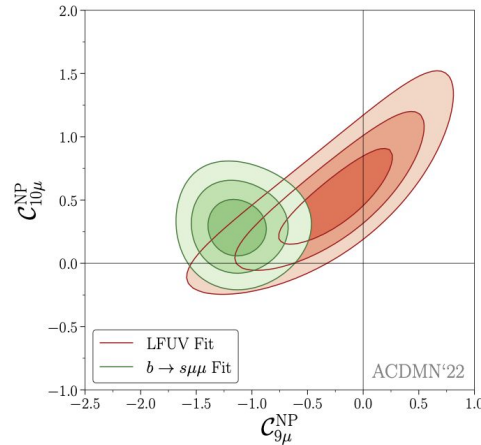
Are $b \rightarrow s\mu\mu$ and LFUV anomalies connected?

[Nature Phys. 18 \(2022\) 3, 277-282](#)



Courtesy of Quim Matias

[Eur.Phys.J.C 82 \(2022\) 4, 326](#)



In agreement with other fitting groups
([Flavour Anomaly Workshop 21](#)):

[Altmannshofer, Stangl Eur.Phys.J.C 81 \(2021\) 10, 952](#)

[Ciuchini et al., Phys.Rev.D 103 \(2021\) 1, 015030](#)

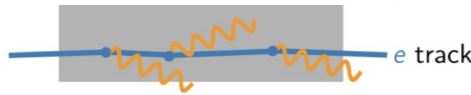
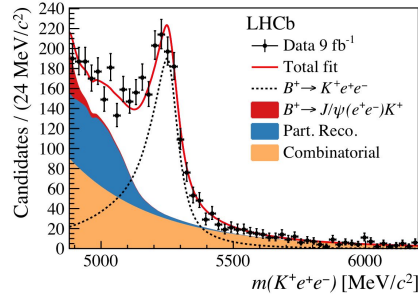
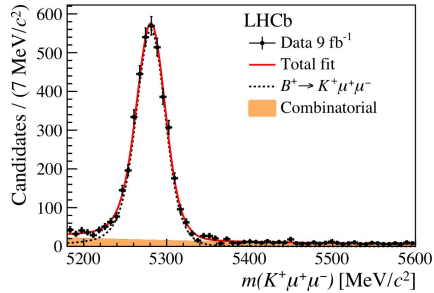
[Hurth et al., Phys.Lett.B 824 \(2022\) 136838](#)

- LFU measurements seem to point to deficit of muons with respect to electrons
- This is numerically consistent with the anomalies measured in $b \rightarrow s\mu\mu$ transitions
- Electrons are found to be consistent with SM

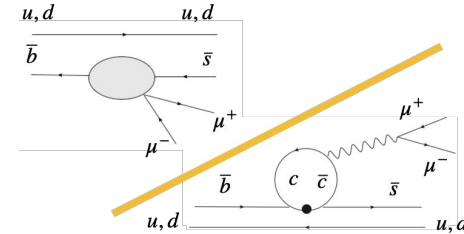
Theory VS experiments

Muon vs electrons

[Nature Phys. 18 \(2022\) 3, 277-282](#)

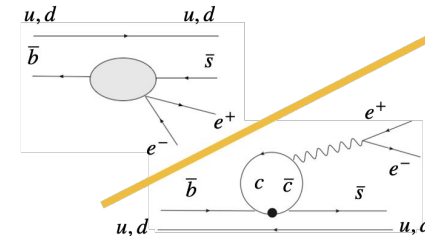


- Electron mode less efficient
- Much worse mass resolution
- More difficult charmonia vetos
- More difficult background
- More difficult calibration (alleviated by double ratio)



EPJC 76 (2016) 8, 440

$$= 1.00 \pm 0.01$$

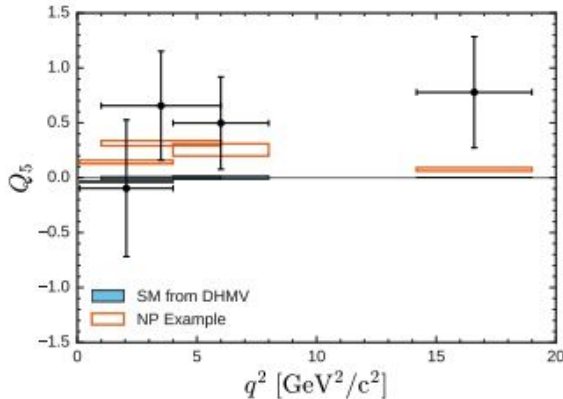


Measuring more LFU R-ratios

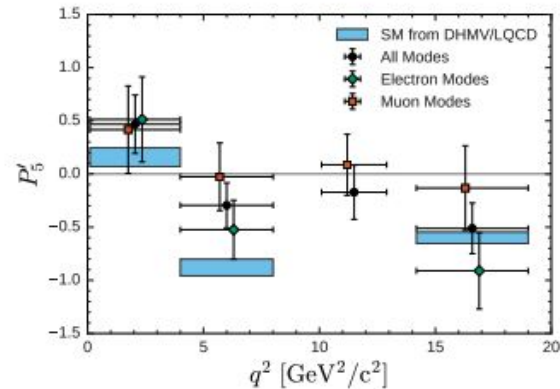
Important to perform more LFU measurements with different systematics

- R_K, R_{K^*} at high- q^2 (experimentally challenging)
- $R_{K\pi} = \text{Br}(B \rightarrow K\pi ee) / \text{Br}(B \rightarrow K\pi \mu\mu)$, $R_{K\pi\pi} = \text{Br}(B \rightarrow K\pi\pi ee) / \text{Br}(B \rightarrow K\pi\pi \mu\mu)$
(see [Isidori et al., Phys.Lett.B 830 \(2022\) 137151](#) and [Hiller et al., JHEP 02 \(2015\) 055](#))
- LFU test of angular observables in $B \rightarrow K^*ll$
(see [Matias et al., JHEP 10 \(2016\) 075](#))

$$Q_5 = P'_5(B^0 \rightarrow K^* \mu\mu) - P'_5(B^0 \rightarrow K^* ee)$$

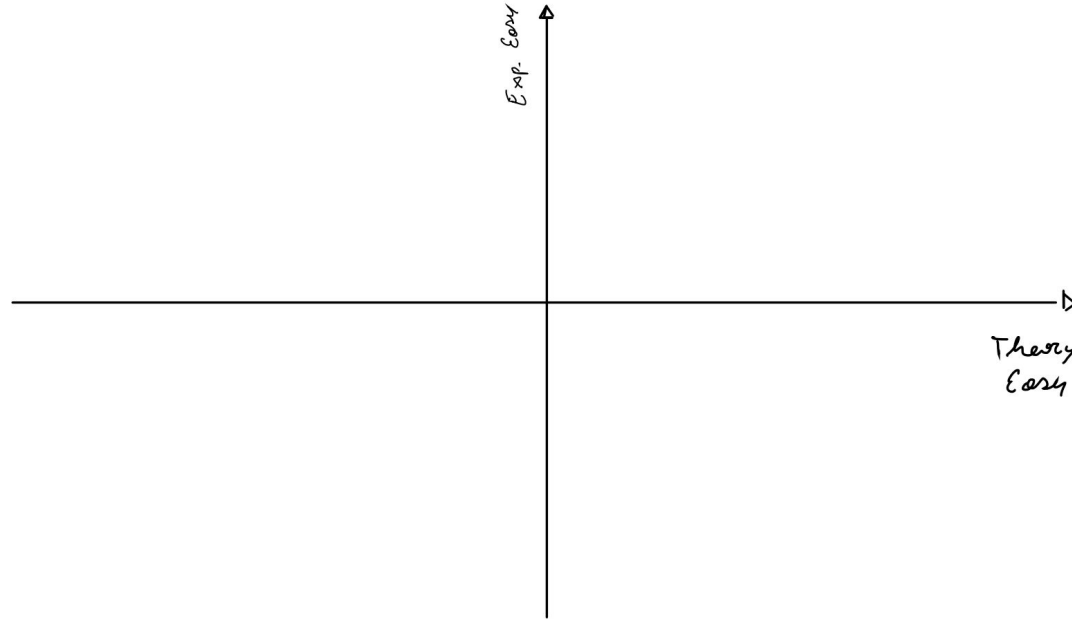


[Belle Coll., Phys.Rev.Lett. 118 \(2017\) 11. 111801](#)



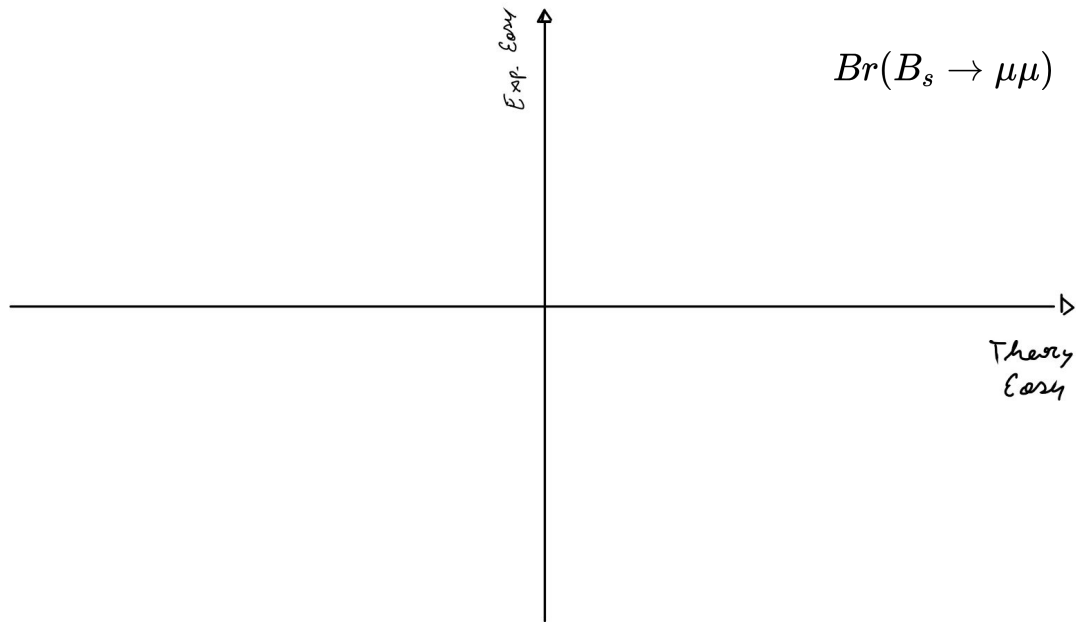
Theory VS experiments

Theory VS Experimentally easy



Theory VS experiments

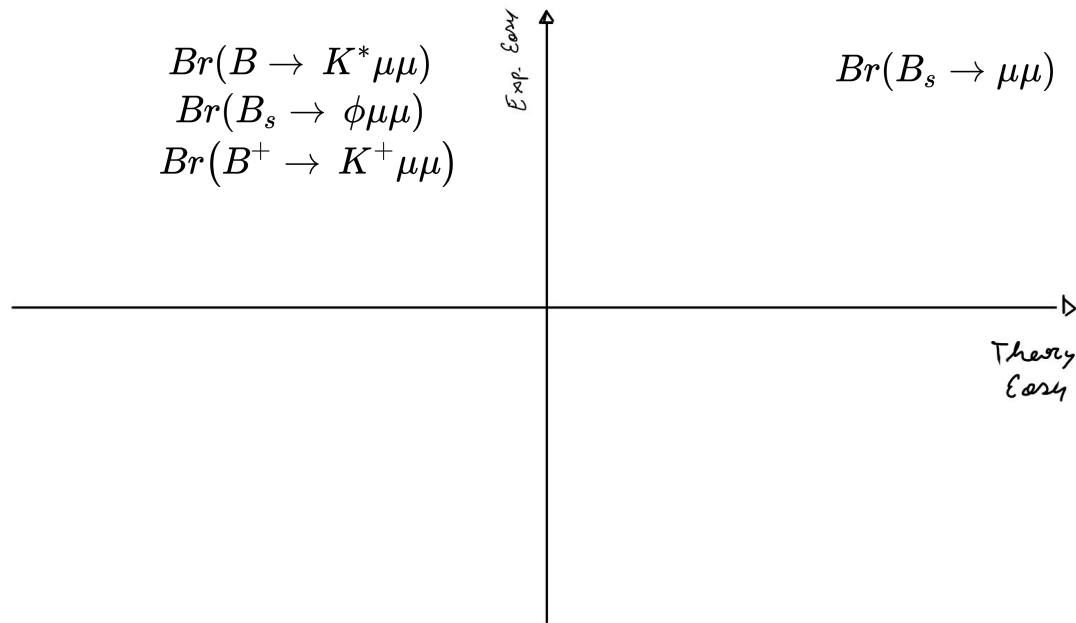
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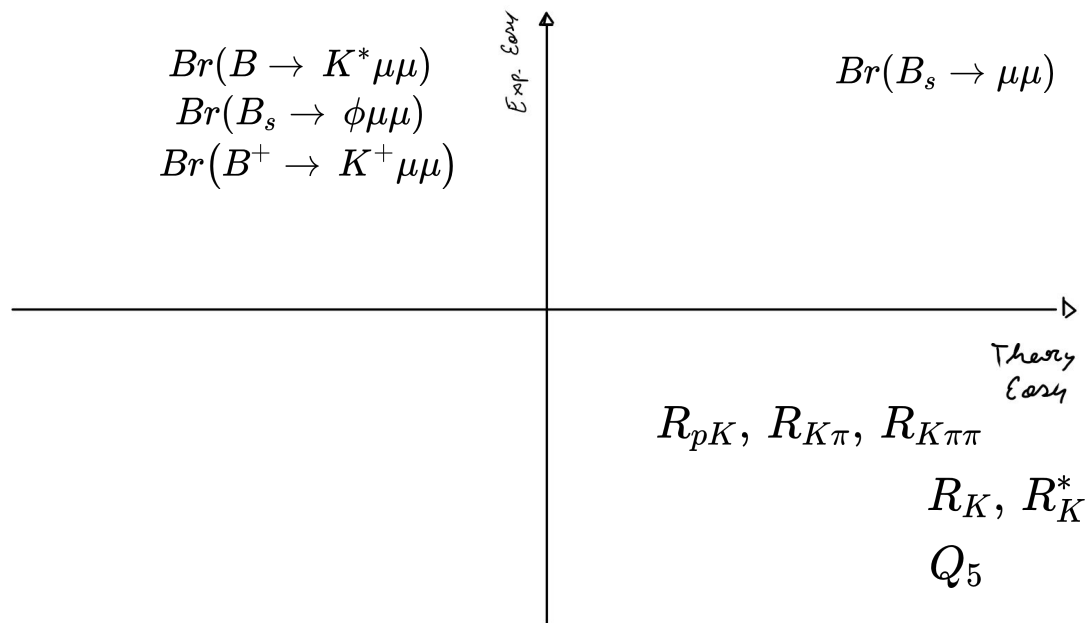
Theory VS experiments



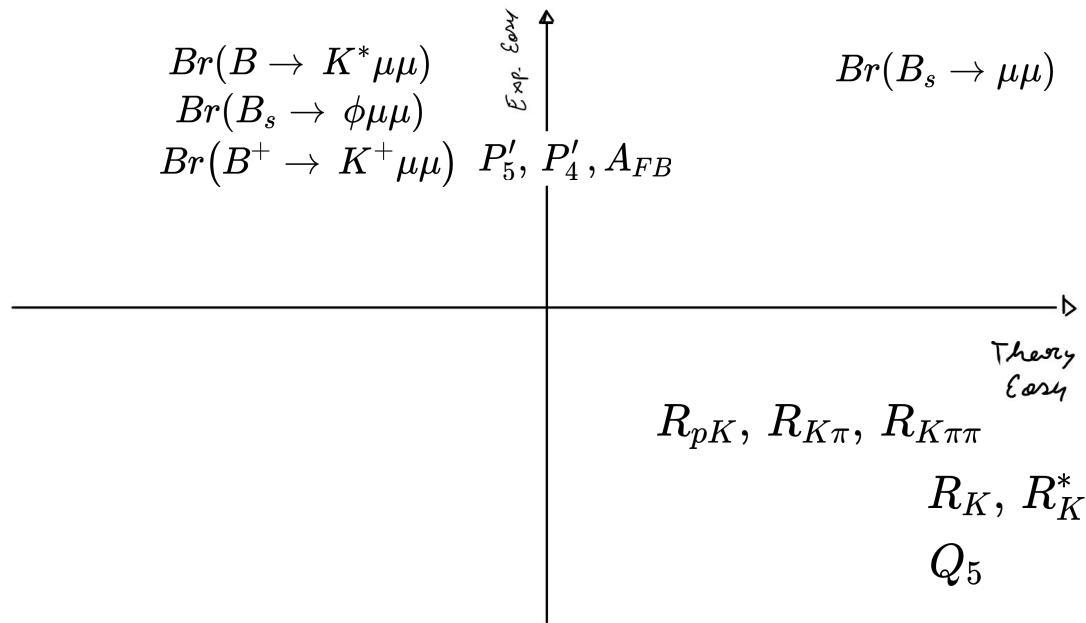
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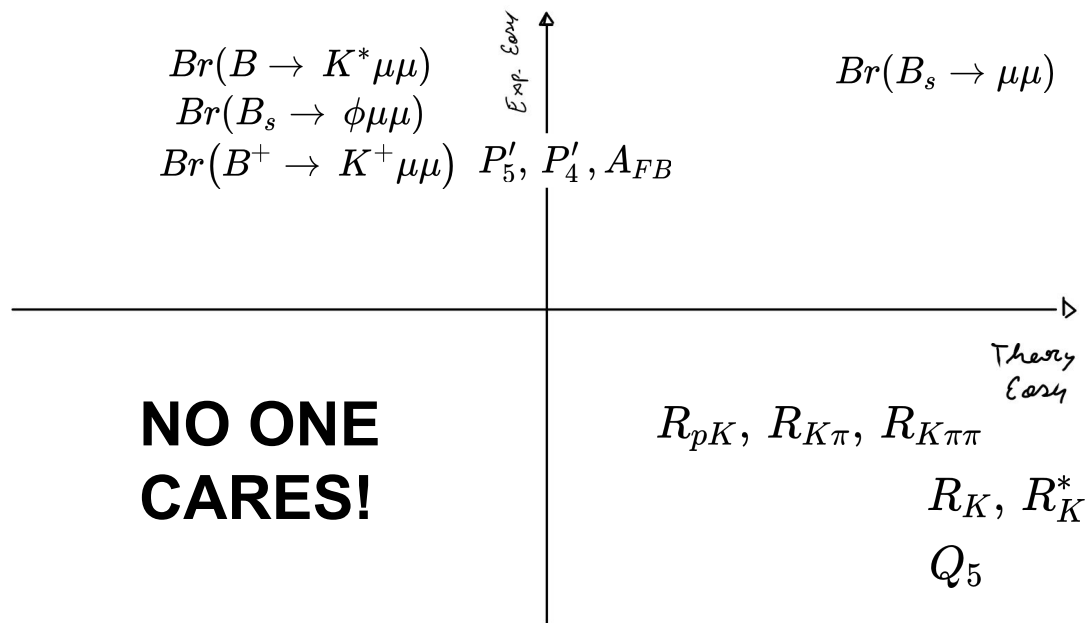
Theory VS Experimentally easy



Theory VS Experimentally easy

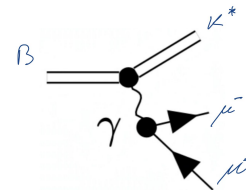
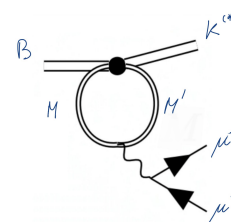
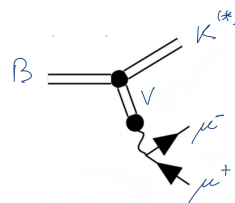
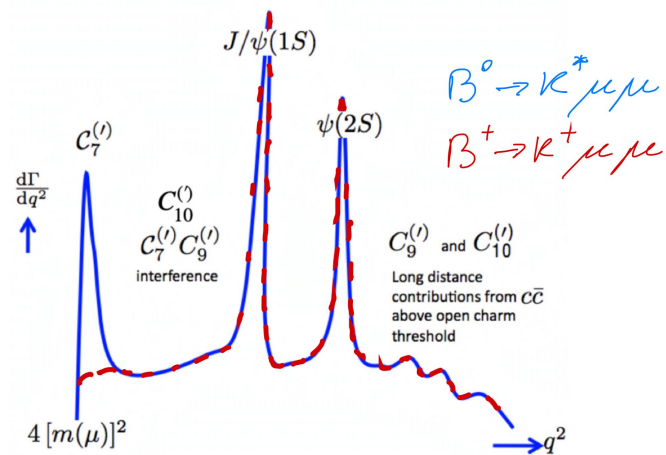


Theory VS Experimentally easy



Measuring the charm loop in Experiment

General idea



- Q^2 spectrum has theory uncertainties from form-factors and hadronic long-distance contributions
- Form-factors well described by lattice QCD ([ailey et al., Phys.Rev.D 93 \(2016\) 2, 025026](#)) and LC sum rules ([Gubernari et al., JHEP 01 \(2019\) 150](#))
- Far from resonances, estimation using perturbative bounds ([Beneke et al., Nucl.Phys.B 612 \(2001\) 25-58](#), [Khodjamirian et al., JHEP 09 \(2010\) 089](#))
- Reliable description of the whole spectrum needs a hybrid data-driven theory approach

Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu \mu$

$$\frac{d\Gamma}{dq^2} = \frac{\alpha_{\text{em}}^2 G_F^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} \kappa(q^2) \beta(q^2) \left\{ \frac{2}{3} \kappa^2(q^2) \beta^2(q^2) |C_{10}^\mu f_+(q^2)|^2 + \frac{m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} |C_{10}^\mu f_0(q^2)|^2 \right. \\ \left. + \kappa^2(q^2) \left[1 - \frac{1}{3} \beta^2(q^2) \right] \left| C_9^\mu f_+(q^2) + 2C_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}$$

Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu \mu$

phase space

lepton mass

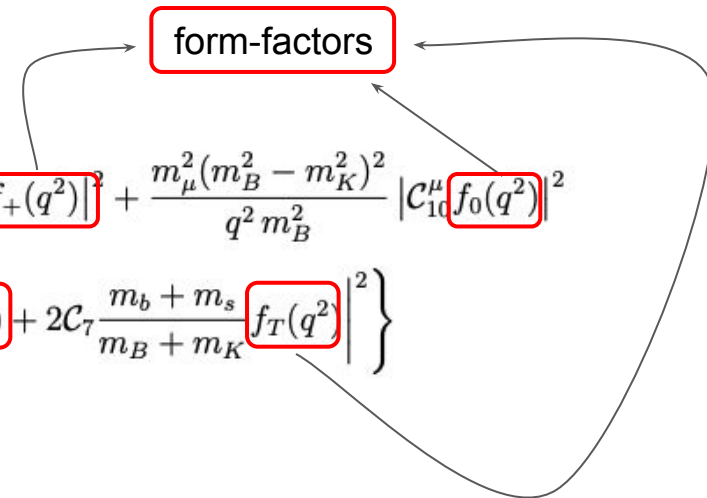
$$\frac{d\Gamma}{dq^2} = \frac{\alpha_{\text{em}}^2 G_F^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} \kappa(q^2) \beta(q^2) \left\{ \frac{2}{3} \kappa^2(q^2) \beta^2(q^2) |C_{10}^\mu f_+(q^2)|^2 + \frac{m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} |C_{10}^\mu f_0(q^2)|^2 \right. \\ \left. + \kappa^2(q^2) \left[1 - \frac{1}{3} \beta^2(q^2) \right] \left| C_9^\mu f_+(q^2) + 2C_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}$$

Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu \mu$

$$\frac{d\Gamma}{dq^2} = \frac{\alpha_{\text{em}}^2 G_F^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} \kappa(q^2) \beta(q^2) \left\{ \frac{2}{3} \kappa^2(q^2) \beta^2(q^2) |C_{10}^\mu f_+(q^2)|^2 + \frac{m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} |C_{10}^\mu f_0(q^2)|^2 \right. \\ \left. + \kappa^2(q^2) \left[1 - \frac{1}{3} \beta^2(q^2) \right] \left| C_9^\mu f_+(q^2) + 2C_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}$$

form-factors



Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu \mu$

Wilson Coefficients

$$\frac{d\Gamma}{dq^2} = \frac{\alpha_{\text{em}}^2 G_F^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} \kappa(q^2) \beta(q^2) \left\{ \frac{2}{3} \kappa^2(q^2) \beta^2(q^2) \left| \mathcal{C}_{10}^\mu f_+(q^2) \right|^2 + \frac{m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} \left| \mathcal{C}_{10}^\mu f_0(q^2) \right|^2 \right. \\ \left. + \kappa^2(q^2) \left[1 - \frac{1}{3} \beta^2(q^2) \right] \left| \mathcal{C}_9^\mu f_+(q^2) + 2 \mathcal{C}_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}$$

Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu \mu$

$$\frac{d\Gamma}{dq^2} = \frac{\alpha_{\text{em}}^2 G_F^2 |V_{tb} V_{ts}^*|^2}{128 \pi^5} \kappa(q^2) \beta(q^2) \left\{ \frac{2}{3} \kappa^2(q^2) \beta^2(q^2) |C_{10}^\mu f_+(q^2)|^2 + \frac{m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} |C_{10}^\mu f_0(q^2)|^2 \right. \\ \left. + \kappa^2(q^2) \left[1 - \frac{1}{3} \beta^2(q^2) \right] \left| C_9^\mu f_+(q^2) + 2C_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}$$

Long distance hadronic contribution (including resonances) goes here: $C_9^\mu \rightarrow C_9^{\mu, \text{eff}}(q^2) = C_9^\mu + Y(q^2)$

The structure of C_9

Cornella et al., Eur.Phys.J.C 80 (2020) 12, 1095

$$C_9^{\mu,\text{eff}}(q^2) = C_9^\mu + Y_{c\bar{c}}^{(0)} + \Delta Y_{c\bar{c}}^{1P}(q^2) + \Delta Y_{c\bar{c}}^{2P}(q^2) + Y_{\text{light}}^{1P}(q^2) + Y_{\tau\bar{\tau}}(q^2)$$

Measuring the charm loop in Experiment

The structure of C_9

Cornella et al., Eur.Phys.J.C 80 (2020) 12, 1095

$$Y_{c\bar{c}}^{(0)} \approx -0.10 \pm 0.05$$

*Khodjamirian, Mannel,
Wang JHEP 02 (2013) 010*

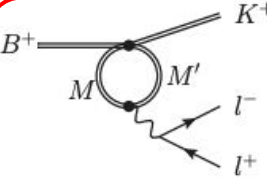
$$C_9^{\mu,\text{eff}}(q^2) = C_9^\mu + Y_{c\bar{c}}^{(0)} + \Delta Y_{c\bar{c}}^{1P}(q^2) + \Delta Y_{c\bar{c}}^{2P}(q^2) + Y_{\text{light}}^{1P}(q^2) + Y_{\tau\bar{\tau}}(q^2)$$

Short distance (in the $C_9^{\text{SM}} \sim 4.23$)

Measuring the charm loop in Experiment

The structure of C_9

Cornella et al., Eur.Phys.J.C 80 (2020) 12, 1095

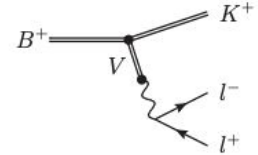


A Feynman diagram showing a B^+ meson (quark line) and a K^+ meson (quark line) meeting at a vertex. A charm quark loop is formed by a charm quark line and a charm antiquark line. A photon is emitted from the charm quark line and splits into a lepton pair (l^- and l^+). The vertices are labeled M and M' .

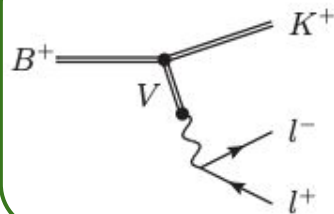
$$\Delta Y_{c\bar{c}}^{2P}(q^2) = \sum_j \eta_j e^{i\delta_j} A_j^{2P}(q^2), \quad A_j^{2P}(q^2) = \frac{q^2}{\pi} \int_{s_j^i}^{\infty} \frac{ds}{s} \frac{\hat{\rho}_j(s)}{(s-q^2)}$$

$$\hat{\rho}_{DD}(s) = \left(1 - \frac{4m_D^2}{s}\right)^{3/2}, \quad \hat{\rho}_{D^*D^*}(s) = \left(1 - \frac{4m_{D^*}^2}{s}\right)^{3/2}, \quad \hat{\rho}_{DD^*}(s) = \left(1 - \frac{4m_D^2}{s}\right)^{1/2}$$

$$Y_{\text{light}}^{1P}(q^2) = \sum_{j=\rho,\omega,\phi} \eta_j e^{i\delta_j} A_j^{\text{res}}(q^2)$$



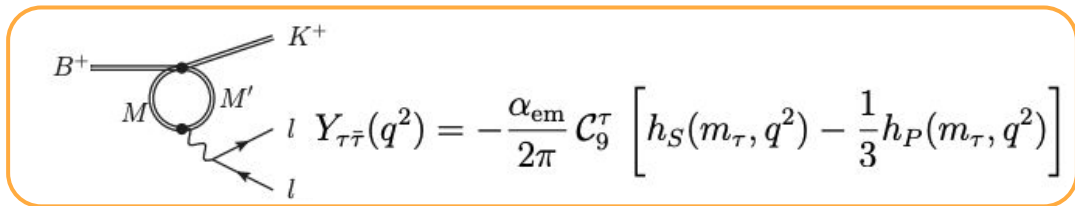
$$C_9^{\mu,\text{eff}}(q^2) = C_9^\mu + Y_{c\bar{c}}^{(0)} + \Delta Y_{c\bar{c}}^{1P}(q^2) + \Delta Y_{c\bar{c}}^{2P}(q^2) + Y_{\text{light}}^{1P}(q^2) + Y_{\tau\bar{\tau}}(q^2)$$



$$\Delta Y_{c\bar{c}}^{1P}(q^2) = \sum_{j=\Psi(1S), \dots, \Psi(4415)} \eta_j e^{i\delta_j} \frac{q^2}{m_j^2} A_j^{\text{res}}(q^2), \quad A_j^{\text{res}}(s) = \frac{m_j \Gamma_j}{(m_j^2 - s) - im_j \Gamma_j}$$

The structure of C_9

[Cornella et al., Eur.Phys.J.C 80 \(2020\) 12, 1095](#)



$$C_9^{\mu, \text{eff}}(q^2) = C_9^\mu + Y_{c\bar{c}}^{(0)} + \Delta Y_{c\bar{c}}^{1\text{P}}(q^2) + \Delta Y_{c\bar{c}}^{2\text{P}}(q^2) + Y_{\text{light}}^{1\text{P}}(q^2) + Y_{\tau\bar{\tau}}(q^2)$$

[Crivellin et al., Phys.Rev.Lett. 122 \(2019\) 1, 011805](#):

Connection between RD/RD* and $b \rightarrow s\mu\mu$

[Alguero et al., Phys.Rev.D 99 \(2019\) 7, 075017](#)

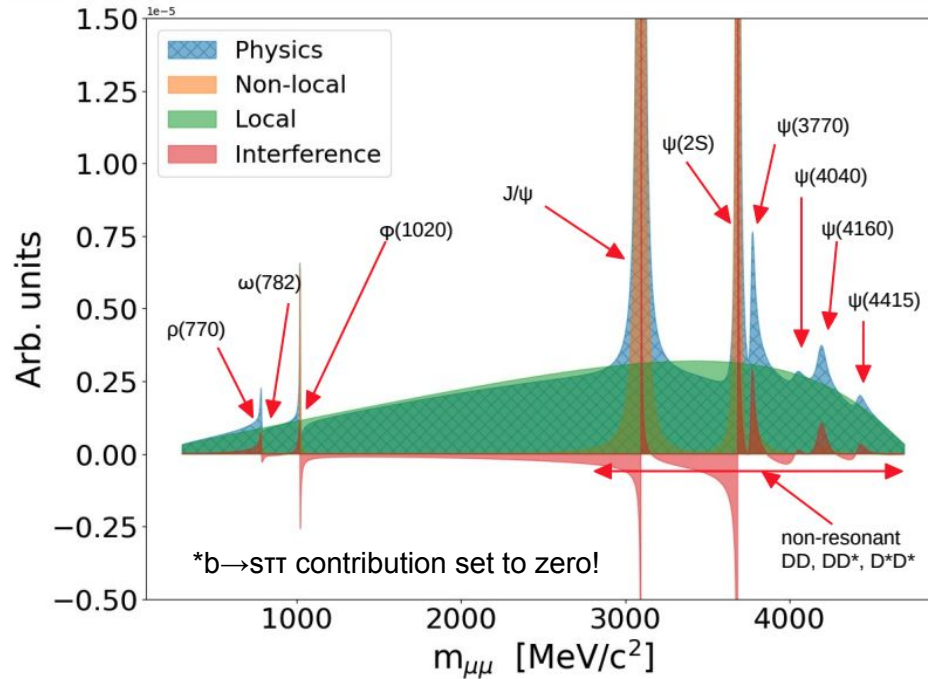
Lepton Universal NP contribution to C_9

[Cornella et al., Eur.Phys.J.C 80 \(2020\) 12, 1095](#):

Dependence on q^2

$B^+ \rightarrow K^+ \mu\mu$

Courtesy of Lakshan Ram Madhan Mohan



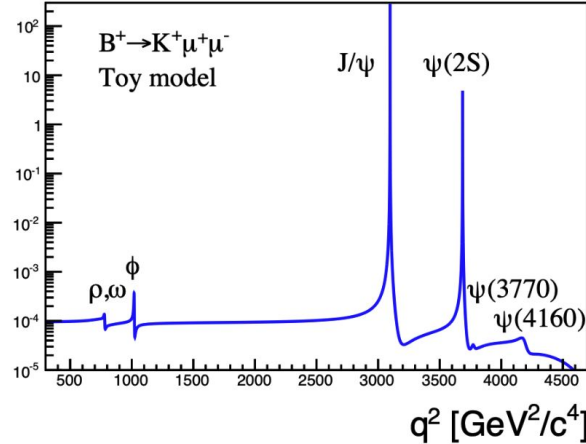
Measuring the charm loop in Experiment

$B^+ \rightarrow K^+ \mu^+ \mu^-$

[LHCb Coll., Eur.Phys.J.C 77 \(2017\) 3, 161](#)

Courtesy of Patrick Owen

Decay	% of $B^+ \rightarrow K^+ \mu^+ \mu^-$
Penguin	0.6 %
$B^+ \rightarrow \rho K^+$	0.0003 %
$B^+ \rightarrow \omega K^+$	0.0006 %
$B^+ \rightarrow \phi K^+$	0.003 %
$B^+ \rightarrow J/\psi K^+$	92 %
$B^+ \rightarrow \psi(2S) K^+$	7.3 %
$B^+ \rightarrow \psi(3770) K^+$	0.007 %
$B^+ \rightarrow \psi(4040) K^+$	~ 0 %
$B^+ \rightarrow \psi(4160) K^+$	0.005 %
$B^+ \rightarrow \psi(4415) K^+$	~ 0 %



$$\mathcal{C}_9^{\mu, \text{eff}}(q^2) = \mathcal{C}_9^\mu + \Delta Y_{cc}^{1P}(q^2) + Y_{\text{light}}^{1P}(q^2)$$

$$\mathcal{C}_9^{\text{eff}} = \mathcal{C}_9 + \sum_j \eta_j e^{i\delta_j} A_j^{\text{res}}(q^2)$$

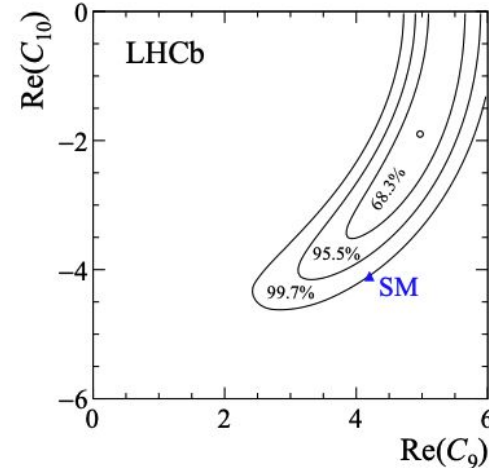
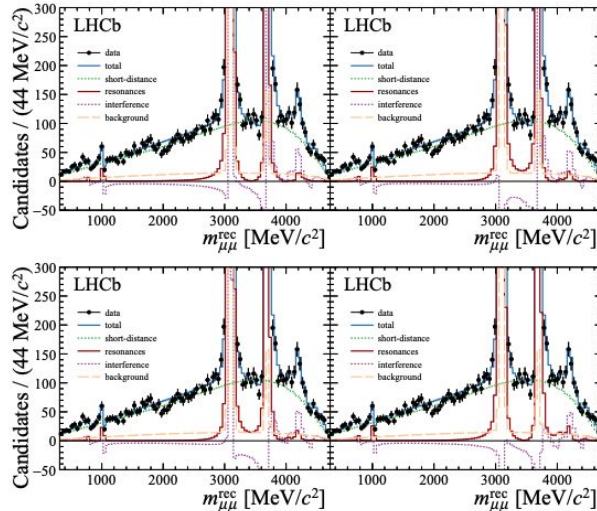
$$A_j^{\text{res}}(q^2) = \frac{m_{0j} \Gamma_{0j}}{(m_{0j}^2 - q^2) - im_{0j} \Gamma_j(q^2)}$$

- Resonances added as relativistic BW
- Branching ratios of $B^+ \rightarrow VK^+$ constrained from the PDG (assuming factorization)
- Form-factors constrained from lattice QCD ([Bailey et al., Phys.Rev.D 93 \(2016\) 2, 025026](#))
- Contribution of $D^{(*)}D^{(*)}$ ignored

Measuring the charm loop in Experiment

$$B^+ \rightarrow K^+ \mu \mu$$

[LHCb Coll., Eur.Phys.J.C 77 \(2017\) 3, 161](#)



- Results show minimal interference between rare mode and J/Ψ and $\Psi(2S)$
- Allow to fit for C_9 and C_{10} leading to tension with respect to prediction (model dependent)
- Improved uncertainty of the form-factors
- Extension to $B \rightarrow K^* \mu \mu$ discussed in [Egede et al., Eur.Phys.J.C 78 \(2018\) 6, 453](#)

Measuring the charm loop in Experiment

Extension to $B \rightarrow K^* \mu \mu$

$$\mathcal{A}_\lambda^{L,R} = N_\lambda \left\{ \boxed{(C_9 \mp C_{10})} \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[\boxed{C_7} \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

✦ Wilson coefficients

✦ Form factors

✦ Non-local hadronic matrix elements

Interesting theory development
[Van Dyk et al., IPPP workshop 'Beyond the flavour anomalies'](#)

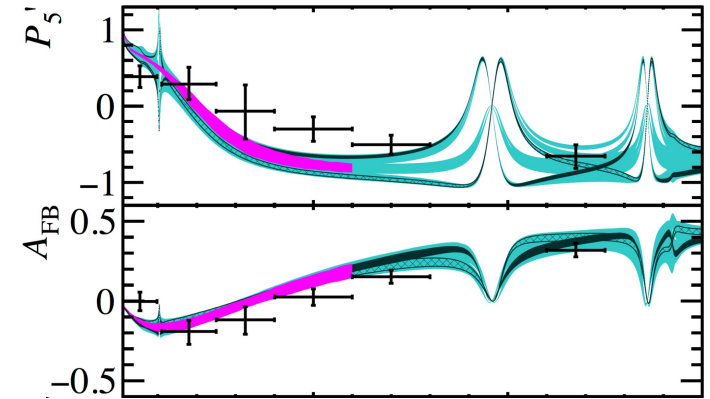
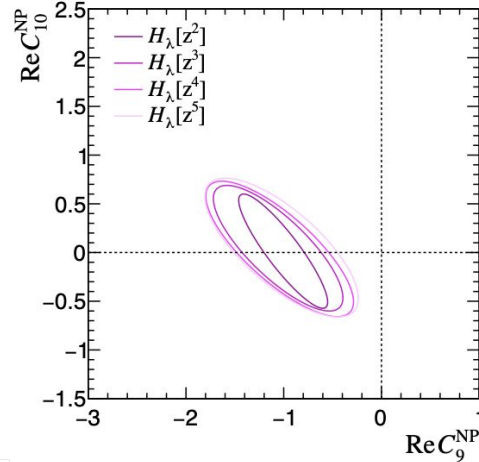
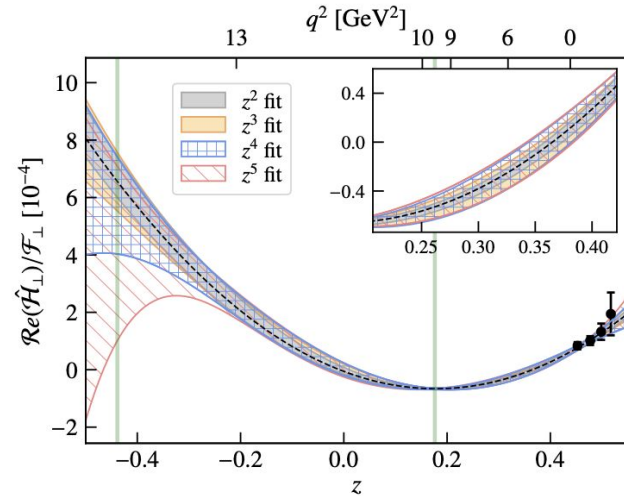
- Combining the approaches of [Egede et al., Eur.Phys.J.C 78 \(2018\) 6, 453](#) and [Cornella et al., Eur.Phys.J.C 80 \(2020\) 12, 1095](#) to include all known contributions to C_9
- Approach of [Chrzaszcz et al., JHEP 10 \(2019\) 236](#) and [Bobeth et al., Eur.Phys.J.C 78 \(2018\) 6, 451](#) consists of expanding $H(q^2)$ as polynomial in $z(q^2)$ fitting simultaneously with pseudo-observables coming from J/Ψ and $\Psi(2S)$ and theory points at negative q^2
- Both approaches have their own merits and both are pursued at LHCb

Measuring the charm loop in Experiment

Extension to $B \rightarrow K^* \mu\mu$

[Chrzaszcz et al., JHEP 10 \(2019\) 236](#)

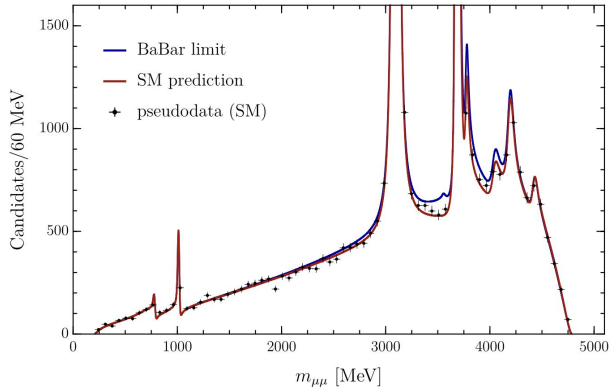
[Egede et al., Eur.Phys.J.C 78 \(2018\) 6, 453](#)



- Sensitivity studies with pseudo-experiment
- To be understood the tradeoff between model dependence and uncertainty

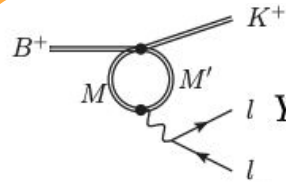
Hunting $b \rightarrow s\tau\tau$ in the dimuon spectrum of $b \rightarrow s\mu\mu$

[Cornella et al., Eur.Phys.J.C 80 \(2020\) 12, 1095](#)



$$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \tau^-) \approx \begin{cases} 8.7 \times 10^{-9} \times |\mathcal{C}_9^\tau|^2 & \mathcal{C}_9^\tau = \mathcal{C}_{10}^\tau \\ 2.7 \times 10^{-9} \times |\mathcal{C}_9^\tau|^2 & \mathcal{C}_{10}^\tau = 0 \end{cases}$$

- Constraint on \mathcal{C}_9^τ competitive with direct searches
- Allows to explore possible correlations between $b \rightarrow s\mu\mu$ and $b \rightarrow c\tau\nu$ anomalies ([Crivellin et al., Phys.Rev.Lett. 122 \(2019\) 1, 011805](#), [Alguero et al., Phys.Rev.D 99 \(2019\) 7, 075017](#))



$$Y_{\tau\bar{\tau}}(q^2) = -\frac{\alpha_{\text{em}}}{2\pi} \mathcal{C}_9^\tau \left[h_S(m_\tau, q^2) - \frac{1}{3} h_P(m_\tau, q^2) \right]$$

$$h_P(m, q^2) = \frac{2}{3} + \left(1 - \frac{4m^2}{q^2}\right) h_S(m, q^2), \quad h_S(m, q^2) = 2 - G\left(1 - \frac{4m^2}{q^2}\right)$$

$$G(y) = \sqrt{|y|} \left\{ \Theta(y) \left[\ln\left(\frac{1+\sqrt{y}}{1-\sqrt{y}}\right) - i\pi \right] + 2 \Theta(-y) \arctan\left(\frac{1}{\sqrt{-y}}\right) \right\}$$

Measurements of $b \rightarrow s\tau\tau$

- Important to search $b \rightarrow s\tau\tau$ directly and indirectly
- Possible correlations with $b \rightarrow c\tau\nu$
- Important to understand charm-loop

$$Br(B_s \rightarrow \tau\tau) < 6.8 \cdot 10^{-3} \text{ @95\%CL}$$

$$Br(B^0 \rightarrow \tau\tau) < 2.1 \cdot 10^{-3} \text{ @95\%CL}$$

$$Br(B^+ \rightarrow K^+ \tau\tau) < 2.25 \cdot 10^{-3} \text{ @90\%CL}$$

$$Br(B^0 \rightarrow K^* \tau\tau) < 2.0 \cdot 10^{-3} \text{ @90\%CL}$$

[LHCb Coll., Phys. Rev. Lett. 118, 251802](#)

[BaBar Coll., Phys.Rev.Lett. 118 \(2017\) 3, 031802](#)

[Belle Coll., 2110.03871 \[hep-ex\]](#)

[See talk by Niladri Sahoo \(parallel session on Wednesday afternoon\)](#)

[Belle II Physics Book](#)

Observables	Belle 0.71 ab^{-1} (0.12 ab^{-1})	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
$Br(B^+ \rightarrow K^+ \tau^+ \tau^-) \cdot 10^5$	< 32	< 6.5	< 2.0
$Br(B^0 \rightarrow \tau^+ \tau^-) \cdot 10^5$	< 140	< 30	< 9.6
$Br(B_s^0 \rightarrow \tau^+ \tau^-) \cdot 10^4$	< 70	< 8.1	—
$Br(B^+ \rightarrow K^+ \tau^\pm e^\mp) \cdot 10^6$	—	—	< 2.1
$Br(B^+ \rightarrow K^+ \tau^\pm \mu^\mp) \cdot 10^6$	—	—	< 3.3
$Br(B^0 \rightarrow \tau^\pm e^\mp) \cdot 10^6$	—	—	< 1.6
$Br(B^0 \rightarrow \tau^\pm \mu^\mp) \cdot 10^6$	—	—	< 1.3

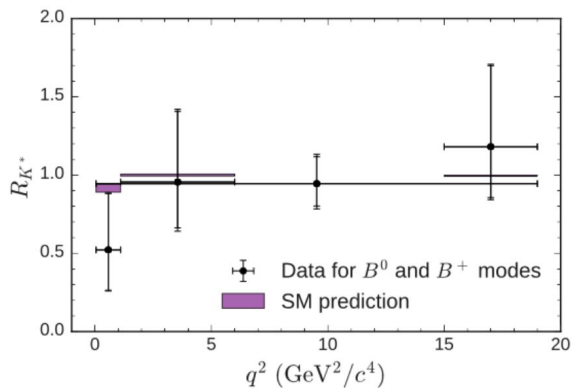
[BelleII Physics for Snowmass 2021](#)

ab ⁻¹	$\mathcal{B}(B^0 \rightarrow K^{*0} \tau\tau)$ (had tag)	
	"Baseline" scenario	"Improved" scenario
1	< 3.2×10^{-3}	< 1.2×10^{-3}
5	< 2.0×10^{-3}	< 6.8×10^{-4}
10	< 1.8×10^{-3}	< 6.5×10^{-4}
50	< 1.6×10^{-3}	< 5.3×10^{-4}

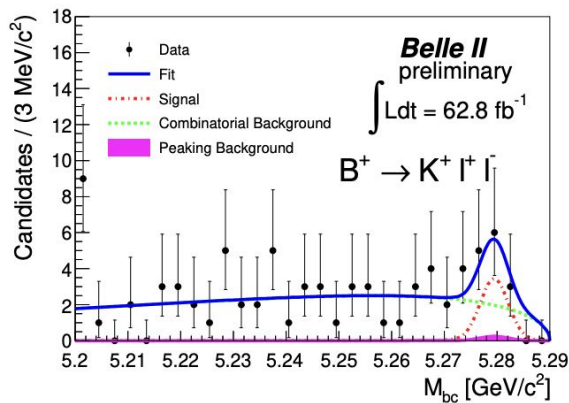


Anomalies @ Belle II

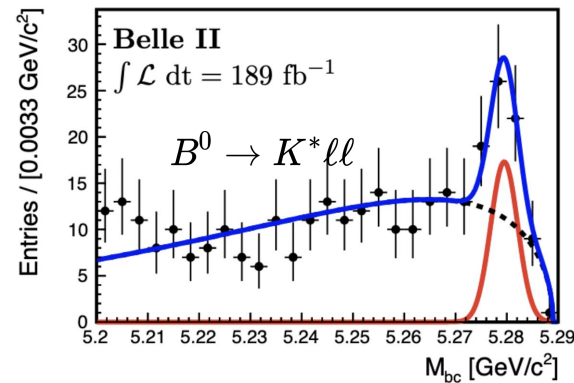
[Belle Coll., Phys.Rev.Lett. 126 \(2021\) 16, 161801](#)



[Belle2-NOTE-PL-2021-005](#)



[E Manoni Moriond EW 2022](#)

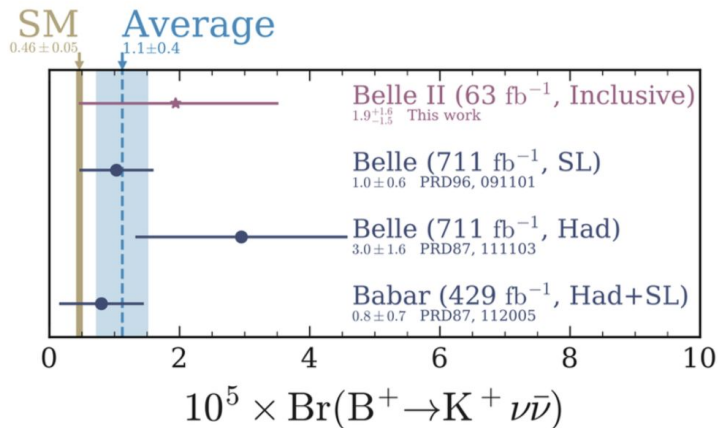


- Belle II results will coming (already preliminary results with 63fb^{-1} and 190fb^{-1})
- Belle II expected uncertainty on LFU R-ratio about 2% with 50/ab ([Belle II Physics Book](#))
- Already with few ab^{-1} Belle II will provide independent cross-check on the anomalies
- Belle II almost symmetric electron/muon reconstruction performances
- Belle II could provide absolute BR measurements for electrons and muons



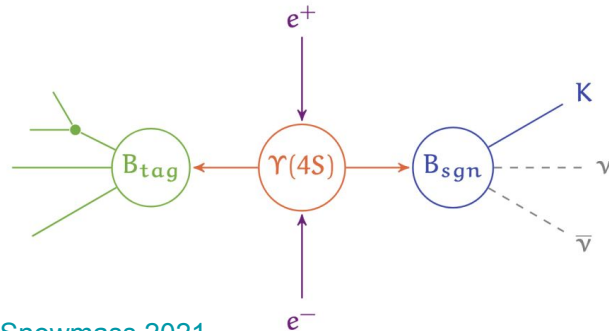
Future Prospects

Anomalies @ Belle II



$$B(B^+ \rightarrow K^+ \nu \bar{\nu}) < 4.1 \times 10^{-5} \text{ @90\% CL}$$

[Belle II Coll., Phys. Rev. Lett. **127**, 181802](#)



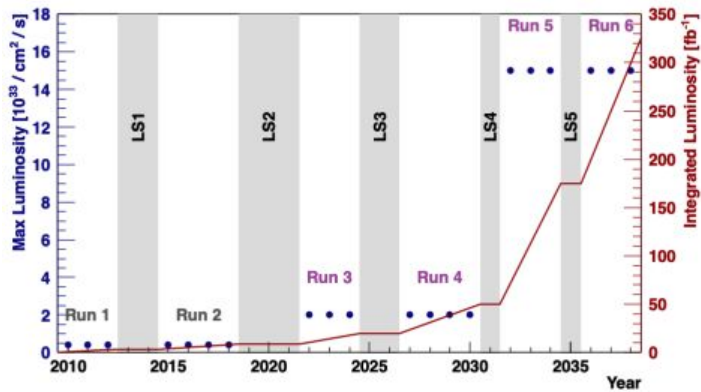
[BelleII Physics for Snowmass 2021](#)

Decay	1 ab ⁻¹	5 ab ⁻¹	10 ab ⁻¹	50 ab ⁻¹
$B^+ \rightarrow K^+ \nu \bar{\nu}$	0.55 (0.37)	0.28 (0.19)	0.21 (0.14)	0.11 (0.08)
$B^0 \rightarrow K_S^0 \nu \bar{\nu}$	2.06 (1.37)	1.31 (0.87)	1.05 (0.70)	0.59 (0.40)
$B^+ \rightarrow K^{*+} \nu \bar{\nu}$	2.04 (1.45)	1.06 (0.75)	0.83 (0.59)	0.53 (0.38)
$B^0 \rightarrow K^{*0} \nu \bar{\nu}$	1.08 (0.72)	0.60 (0.40)	0.49 (0.33)	0.34 (0.23)

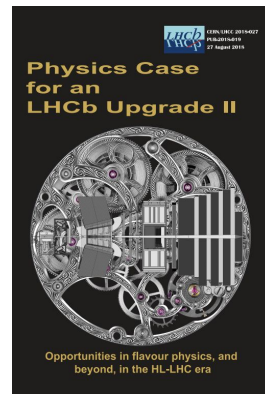
- $B \rightarrow K \nu \bar{\nu}$ includes all neutrino species
- Complementary probe to $b \rightarrow s \tau \tau \rightarrow$ Possible correlation with semileptonic anomaly

LHCb Upgrades

- LHCb Upgrade starts this year, almost an independent experiment



[EoI LHCb Upgrade II](#)

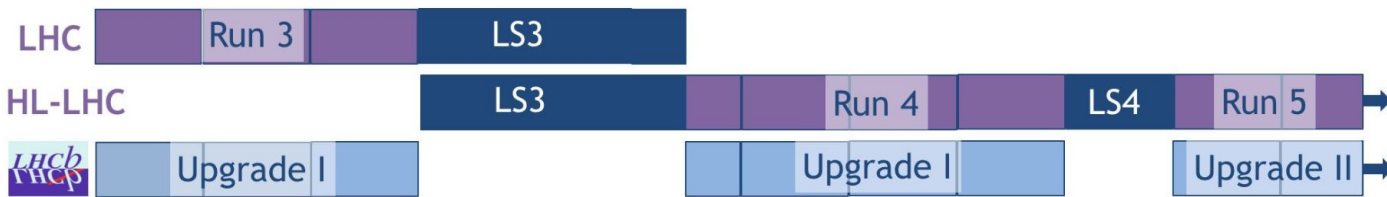


[arXiv:1808.08865](#)



[Framework TDR](#)

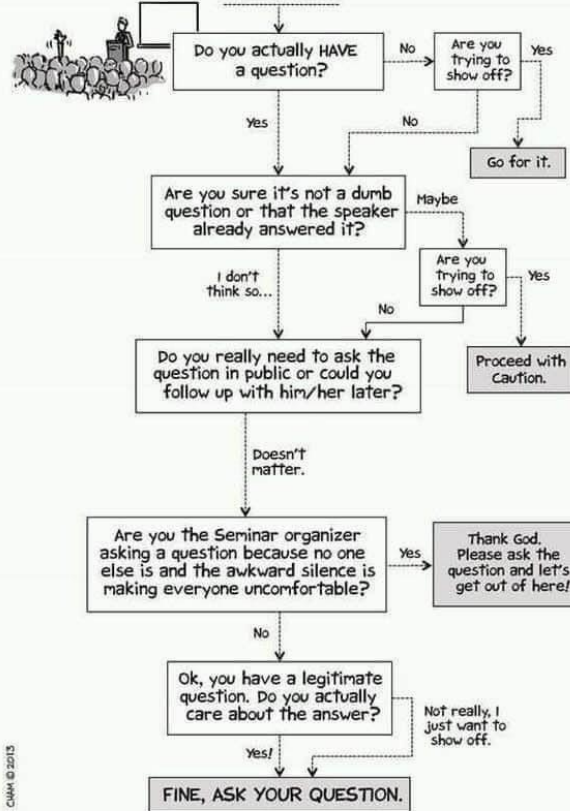
2022 2023 2024 2025 2026 2027 2028 2029 2030 2031 ...



Conclusions

- Interesting anomalies in rare decays
- $b \rightarrow s \mu \mu$ anomaly limited by theory uncertainty (charm loop)
- Several ideas to improve our understanding of long distance hadronic contribution \rightarrow Needed cooperation between experimentalists and theorists
- Intriguing discrepancies in LFU observables (experimentally challenging) \rightarrow more measurements needed
- LHCb Upgrades and Belle II will clarify these anomalies

Should you ask a Question during at a FPCP22 talk?



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Backup slides

i	I_i	f_i
1s	$\frac{3}{4} \left[\mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^L ^2 + \mathcal{A}_{\parallel}^R ^2 + \mathcal{A}_{\perp}^R ^2 \right]$	$\sin^2 \theta_K$
1c	$ \mathcal{A}_0^L ^2 + \mathcal{A}_0^R ^2$	$\cos^2 \theta_K$
2s	$\frac{1}{4} \left[\mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^L ^2 + \mathcal{A}_{\parallel}^R ^2 + \mathcal{A}_{\perp}^R ^2 \right]$	$\sin^2 \theta_K \cos 2\theta_l$
2c	$- \mathcal{A}_0^L ^2 - \mathcal{A}_0^R ^2$	$\cos^2 \theta_K \cos 2\theta_l$
3	$\frac{1}{2} \left[\mathcal{A}_{\perp}^L ^2 - \mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^R ^2 - \mathcal{A}_{\parallel}^R ^2 \right]$	$\sin^2 \theta_K \sin^2 \theta_l \cos 2\phi$
4	$\sqrt{\frac{1}{2}} \operatorname{Re}(\mathcal{A}_0^L \mathcal{A}_{\parallel}^{L*} + \mathcal{A}_0^R \mathcal{A}_{\parallel}^{R*})$	$\sin 2\theta_K \sin 2\theta_l \cos \phi$
5	$\sqrt{2} \operatorname{Re}(\mathcal{A}_0^L \mathcal{A}_{\perp}^{L*} - \mathcal{A}_0^R \mathcal{A}_{\perp}^{R*})$	$\sin 2\theta_K \sin \theta_l \cos \phi$
6s	$2 \operatorname{Re}(\mathcal{A}_{\parallel}^L \mathcal{A}_{\perp}^{L*} - \mathcal{A}_{\parallel}^R \mathcal{A}_{\perp}^{R*})$	$\sin^2 \theta_K \cos \theta_l$
7	$\sqrt{2} \operatorname{Im}(\mathcal{A}_0^L \mathcal{A}_{\parallel}^{L*} - \mathcal{A}_0^R \mathcal{A}_{\parallel}^{R*})$	$\sin 2\theta_K \sin \theta_l \sin \phi$
8	$\sqrt{\frac{1}{2}} \operatorname{Im}(\mathcal{A}_0^L \mathcal{A}_{\perp}^{L*} + \mathcal{A}_0^R \mathcal{A}_{\perp}^{R*})$	$\sin 2\theta_K \sin 2\theta_l \sin \phi$
9	$\operatorname{Im}(\mathcal{A}_{\parallel}^{L*} \mathcal{A}_{\perp}^L + \mathcal{A}_{\parallel}^{R*} \mathcal{A}_{\perp}^R)$	$\sin^2 \theta_K \sin^2 \theta_l \sin 2\phi$

Backup slides

- The decay is described by six complex amplitudes $A_{0,\parallel,\perp}^{L,R}$
- Correspond to different transversity state of the K^*
- and different (left- and right-handed) chiralities of the dimuon system

$$F_L = \frac{A_0^2}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} = 1 - F_T$$

$$S_3 = \frac{1}{2} \frac{A_{\perp}^{L2} - A_{\parallel}^{L2}}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} + L \rightarrow R$$

$$S_4 = \frac{1}{\sqrt{2}} \frac{\Re(A_0^{L*} A_{\parallel}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} + L \rightarrow R$$

$$S_5 = \sqrt{2} \frac{\Re(A_0^{L*} A_{\perp}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} - L \rightarrow R$$

$$A_{FB} = \frac{8}{3} \frac{\Re(A_{\perp}^{L*} A_{\parallel}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} - L \rightarrow R$$

$$S_7 = \sqrt{2} \frac{\Im(A_0^{L*} A_{\parallel}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} + L \rightarrow R$$

$$S_8 = \frac{1}{\sqrt{2}} \frac{\Im(A_0^{L*} A_{\perp}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} + L \rightarrow R$$

$$S_9 = \frac{\Im(A_{\perp}^{L*} A_{\parallel}^L)}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} - L \rightarrow R$$

- $\Gamma = |A_{\parallel}|^2 + |A_0|^2 + |A_{\perp}|^2$

- Let's see how the amplitudes depend on Wilson coefficients and form factors

Backup slides

$$A_{\perp}^{L,R} \propto [(C_9^{eff} + C_9^{eff'}) \mp (C_{10}^{eff} + C_{10}^{eff'}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} (C_7^{eff} + C_7^{eff'}) T_1(q^2)]$$

$$A_{\parallel}^{L,R} \propto [(C_9^{eff} - C_9^{eff'}) \mp (C_{10}^{eff} - C_{10}^{eff'}) \frac{A_1(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} (C_7^{eff} - C_7^{eff'}) T_2(q^2)]$$

$$A_0^{L,R} \propto [(C_9^{eff} - C_9^{eff'}) \mp (C_{10}^{eff} - C_{10}^{eff'})] \times [(m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*} A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}})] + \\ 2m_b (C_7^{eff} + C_7^{eff'}) [(m_B^2 + 3m_{K^*}^2 - q^2) T_2(q^2) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(q^2)]$$

Backup slides

$$R_1 = \frac{T_1}{V} \sim 1$$

$$R_2 = \frac{T_2}{A_1} \sim 1$$

$$R_3 = \frac{T_{23}}{A_{12}} \sim \frac{q^2}{m_B^2}$$

$$A_{\perp}^{L,R} = \sqrt{2}Nm_B(1 - \hat{s}) \left[(\mathcal{C}_9^{\text{eff}} + \mathcal{C}_9^{\text{eff}'}) \mp (\mathcal{C}_{10} + \mathcal{C}'_{10}) + \frac{2\hat{m}_b}{\hat{s}}(\mathcal{C}_7^{\text{eff}} + \mathcal{C}_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*})$$

$$A_{\parallel}^{L,R} = -\sqrt{2}Nm_B(1 - \hat{s}) \left[(\mathcal{C}_9^{\text{eff}} - \mathcal{C}_9^{\text{eff}'}) \mp (\mathcal{C}_{10} - \mathcal{C}'_{10}) + \frac{2\hat{m}_b}{\hat{s}}(\mathcal{C}_7^{\text{eff}} - \mathcal{C}_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*})$$

$$A_0^{L,R} = -\frac{Nm_B(1 - \hat{s})^2}{2\hat{m}_{K^*}\sqrt{\hat{s}}} \left[(\mathcal{C}_9^{\text{eff}} - \mathcal{C}_9^{\text{eff}'}) \mp (\mathcal{C}_{10} - \mathcal{C}'_{10}) + 2\hat{m}_b(\mathcal{C}_7^{\text{eff}} - \mathcal{C}_7^{\text{eff}'}) \right] \xi_{\parallel}(E_{K^*})$$

P-basis (P_1, \dots, P_8) FF appears in the numerator and in the denominator

$$P'_5 \propto \frac{\mathcal{R}(A_0 A_{\perp})}{\sqrt{|A_0|^2 \times |A_{\perp}|^2}}$$

Backup slides

$$P_1 = A_T^{(2)} = \frac{2S_3}{(1-F_L)} = \frac{A_\perp^{L2} - A_\parallel^{L2}}{A_\parallel^2 + A_\perp^2} + L \rightarrow R$$

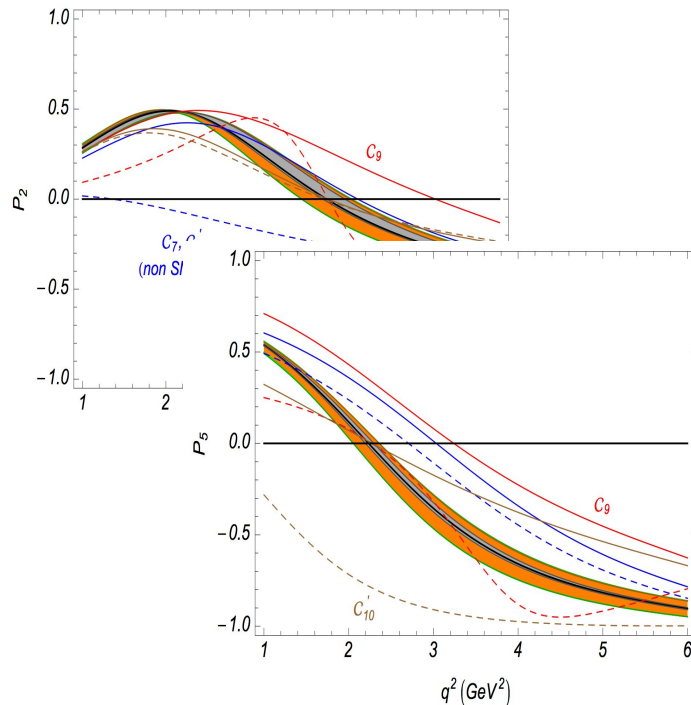
$$P_2 = 2A_T^{Re} = \frac{2A_{FB}}{3(1-F_L)} \propto \frac{\Re(A_\perp^{L*} A_\parallel^L)}{A_\parallel^2 + A_\perp^2} - L \rightarrow R$$

$$P_3 = \frac{S_9}{(1-F_L)} = \frac{\Im(A_\perp^{L*} A_\parallel^L)}{A_\parallel^2 + A_\perp^2} - L \rightarrow R$$

$$P_4' = \frac{S_4}{\sqrt{F_L(1-F_L)}} \propto \frac{\Re(A_0^{L*} A_\parallel^L)}{\sqrt{|A_0|^2 |A_\parallel|^2}} + L \rightarrow R$$

$$P_5' = \frac{S_5}{\sqrt{F_L(1-F_L)}} \propto \frac{\Re(A_0^{L*} A_\perp^L)}{\sqrt{|A_\perp|^2 |A_0|^2}} - L \rightarrow R$$

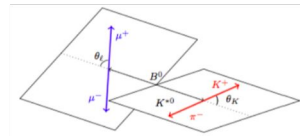
$$P_6' = \frac{S_7}{\sqrt{F_L(1-F_L)}} \propto \frac{\Im(A_0^{L*} A_\parallel^L)}{\sqrt{|A_\parallel|^2 |A_0|^2}} + L \rightarrow R$$



Backup slides

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- * Extended unbinned amplitude fit: $\frac{1}{\Gamma} \frac{d^4\Gamma}{dq^2 d\Omega}$



- * Parametrization introduced by Bobeth et al. [arxiv:1707.07305]

$$\mathcal{A}_\lambda^{L,R} = N_\lambda \left\{ \left[C_9 \mp C_{10} \right] \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) \right] - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right\}$$

- ♦ Wilson coefficients
- ♦ Form factors
- ♦ Non-local hadronic matrix elements ("charm loop")

mapping: $q^2 \rightarrow z(q^2)$

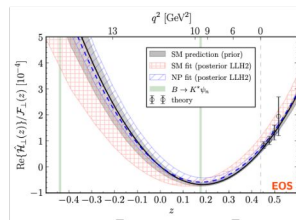
$$\mathcal{H}_\lambda(z) = \frac{1 - z z_{J/\psi}^*}{z - z_{J/\psi}} \frac{1 - z z_{\psi(2S)}^*}{z - z_{\psi(2S)}} \hat{\mathcal{H}}_\lambda(z)$$

extract the poles

polynomial expansion

$$\hat{\mathcal{H}}_\lambda(z) = \left[\sum_k \alpha_k^{(\lambda)} z^k \right] \mathcal{F}_\lambda(z)$$

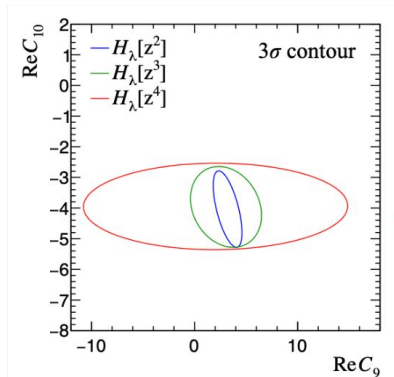
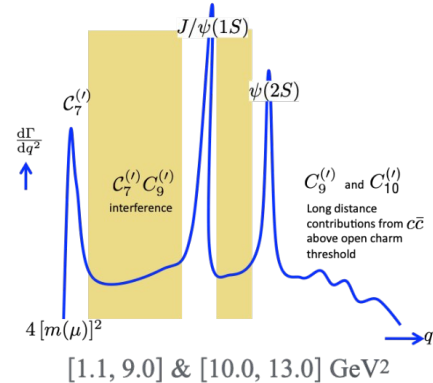
- * analytic within $|z| = 1$
- * truncation at order z^k
 - which order of z describes well nature is a-priori unknown



Backup slides

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- ◆ signal yield fitted to \mathcal{BR}
- ◆ full set of parameters floating:
 - ◆ CKM, FF \rightarrow multi-Gauss. constraints
 - ◆ $H \rightarrow$ **free floating**
- ◆ sensitivity based in signal-only toys
 - ◆ no experimental effects (e.g. background, s-wave, acceptance, efficiency)



Scanning the order of the z -expansion:

- ◆ C_9 : Strong dependence on the cut-off ✗
- ◆ C_{10} : unaffected! ✓

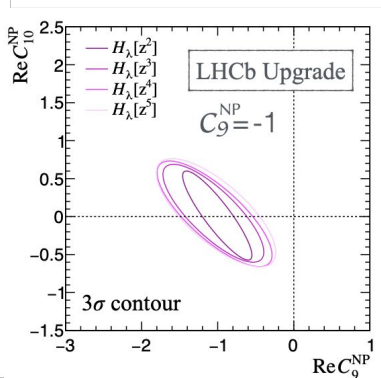
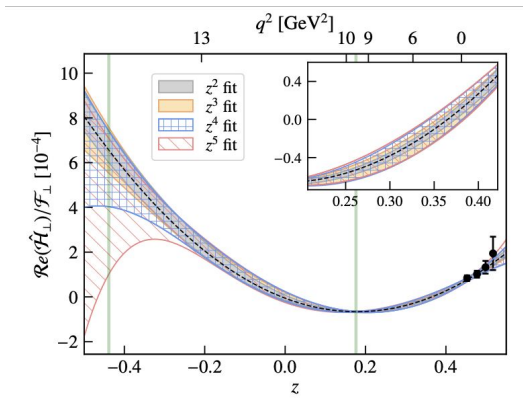
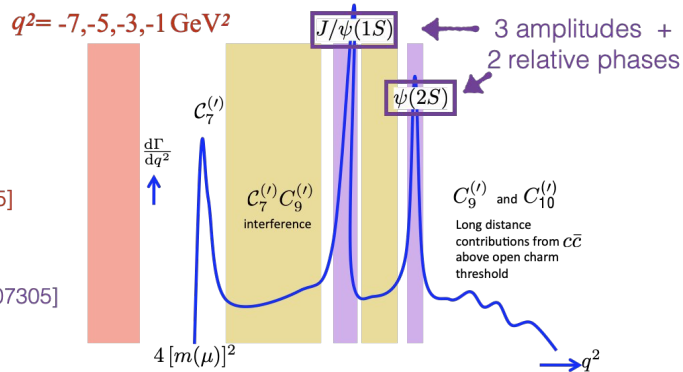
* Direct fits to with different approaches have been proposed in JHEP 11 (2017) 176 and EPJ C78 (2018) n.6 453

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Combined fit to:

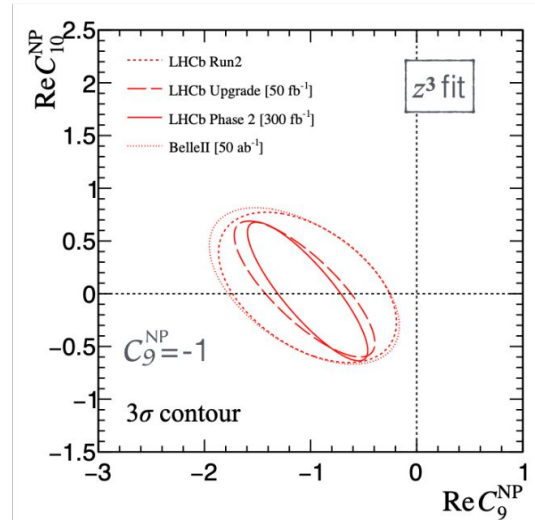
- ◆ semi-muonic $B \rightarrow K^* \mu \mu$ decays
- ◆ theory points at negative q^2
 - ◆ reliable theory predictions [arxiv:1707.07305]
- ◆ hadronic $B \rightarrow K^* \{J/\psi, \psi(2S)\}$ decays
 - ◆ sets of 5 pseudo-observables [arxiv:1707.07305]



- ◆ Uncertainty only slightly increases after z^3 fits
- ◆ We can access in a quantitative way this model-dependency

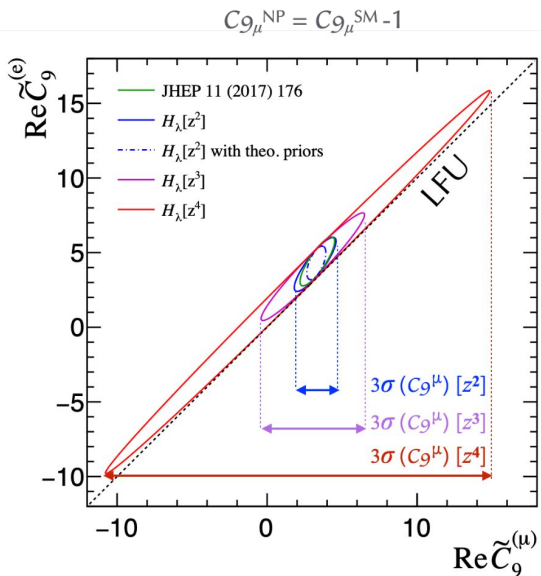
- ◆ Measurement of C_{10} independent on the lack of knowledge on the charm-loop
- ◆ Precision saturates due to the form factors uncertainty after LHCb Run II
 - ◆ we have been very conservative doubling the FF uncertainty of JHEP 08, 098 (2016)
- ◆ Possible 3σ observation after LHCb Run II (depending on the NP scenario...)

Sensitivity for different statistical scenarios



Backup slides

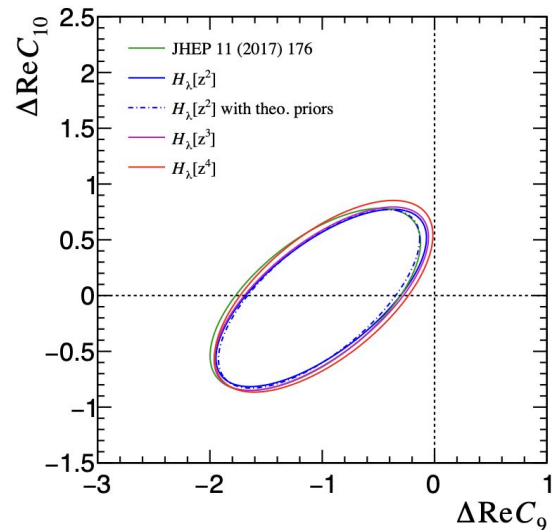
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- * $C_{9\mu}^{(\ell)}$ strongly model-dependent
- * Model-independent determination of the **difference** between electron and muon WCs

$$\Delta C_i = C_i^{(\mu)} - C_i^{(e)}$$

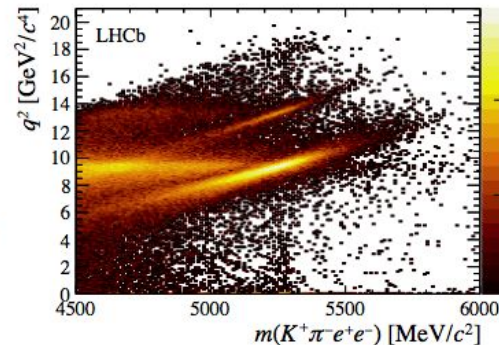
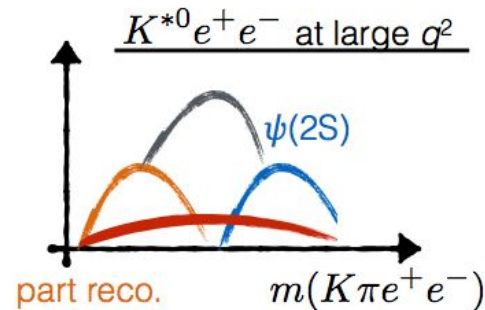
- * Insensitive to the parametrization of the charm loop
- * Significance wrt LFU hypothesis is unbiased



Determination of ΔC_9 and ΔC_{10} is model-independent

Backup slides

- Very little rate for $q^2 < 1.0 \text{ GeV}^2$ (no photon pole)
- Working to add high q^2 bin – difficulty same for R_K and R_{K^*}
 - Rare decays with higher K^* resonances can leak into signal region from below
 - $\psi(2S)K^*$ decays can leak into signal region on the upper side
 - Signal sandwiched between these and hence difficult to fit reliably



Backup slides

- Non-exclusive R-ratios affected by larger theory uncertainty, but can still be rigorously combined
- Neglecting lepton masses ($q^2 \gg m_l^2$) (very good approximation) no interference between left and right handed lepton currents

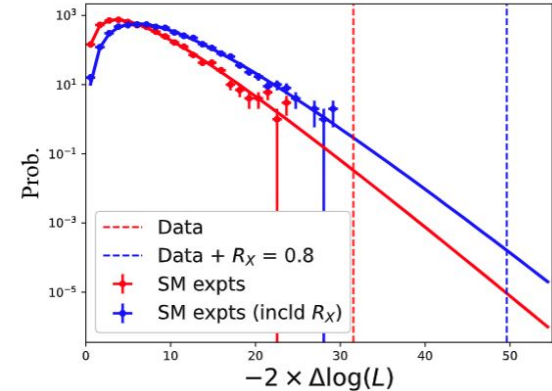
$$\mathcal{A}(B \rightarrow X_s \ell^+ \ell^-) \propto (\mathcal{M}_{X,L}^\ell)^\alpha (J_L^\ell)_\alpha + (\mathcal{M}_{X,R}^\ell)^\alpha (J_R^\ell)_\alpha$$

$$\left\langle X_s \left| \sum_i C_i O_i \right| B \right\rangle \rightarrow \bar{\ell}_L \gamma^\alpha \ell_L$$

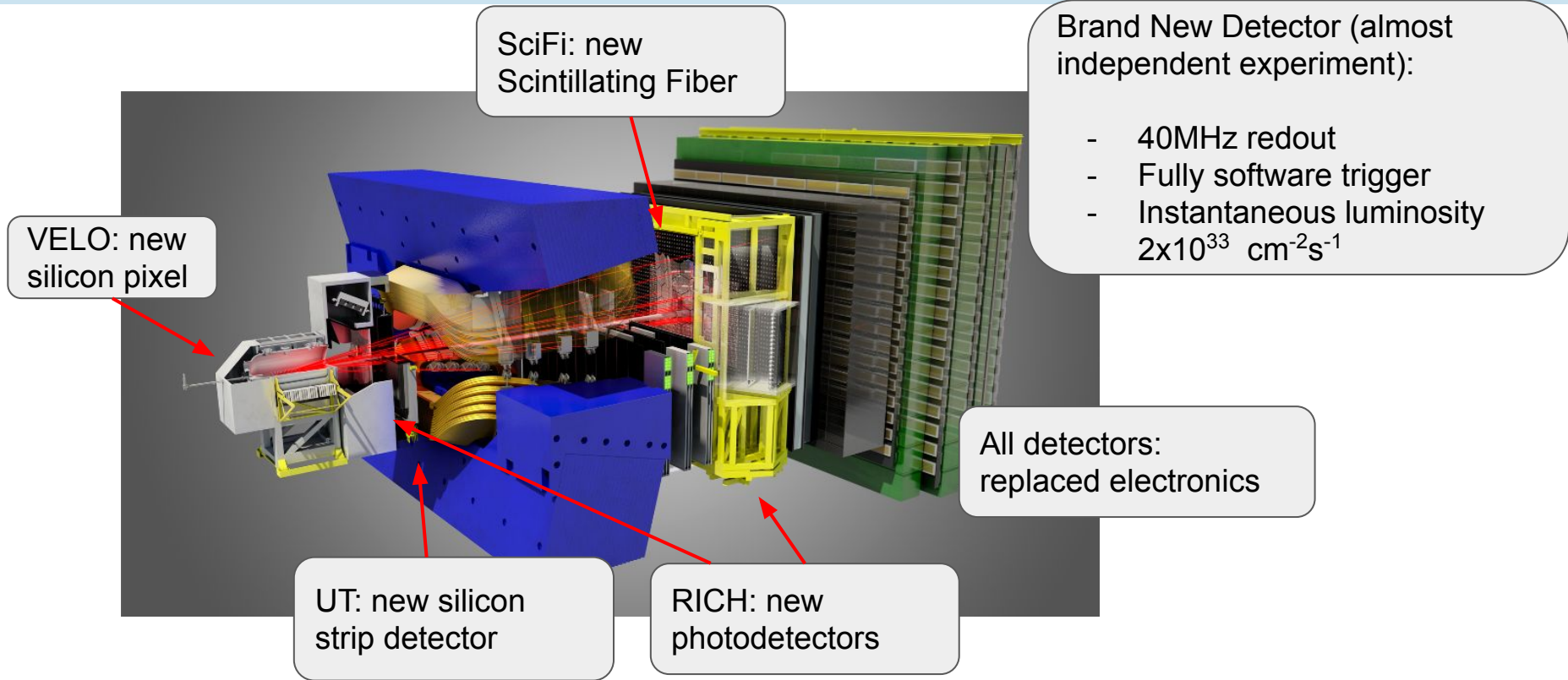
$$R_X = \frac{\left\{ (C_L^\mu)^2 + (C_L^{\prime\mu})^2 + \langle \eta_X^0 \rangle C_L^\mu C_L^{\prime\mu} + C_7 \cdot (\langle \eta_X^{77} \rangle C_7 + \langle \eta_X^{79} \rangle C_L^\mu + \langle \eta_X^{79} \rangle C_L^{\prime\mu}) \right\} + (L \rightarrow R)}{\left\{ (C_L^e)^2 + (C_L^{\prime e})^2 + \langle \eta_X^0 \rangle C_L^e C_L^{\prime e} + C_7 \cdot (\langle \eta_X^{77} \rangle C_7 + \langle \eta_X^{79} \rangle C_L^e + \langle \eta_X^{79} \rangle C_L^{\prime e}) \right\} + (L \rightarrow R)}$$

After integrating on anything apart for q^2

$$\frac{d\Gamma_X^\ell}{dq^2} = \frac{d\Gamma_{X,L}^\ell}{dq^2} + \frac{d\Gamma_{X,R}^\ell}{dq^2} \quad \frac{d\Gamma_{X,R}^\ell}{dq^2} = \frac{d\Gamma_{X,L}^\ell}{dq^2} \Big|_{\{C_L^\ell \rightarrow C_R^\ell, C_L^{\prime\ell} \rightarrow C_R^{\prime\ell}\}}$$



Backup slides



Backup slides

