

Measurement of branching fraction and search for  
 $CP$  violation in  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  decays at Belle

FPCP 2022



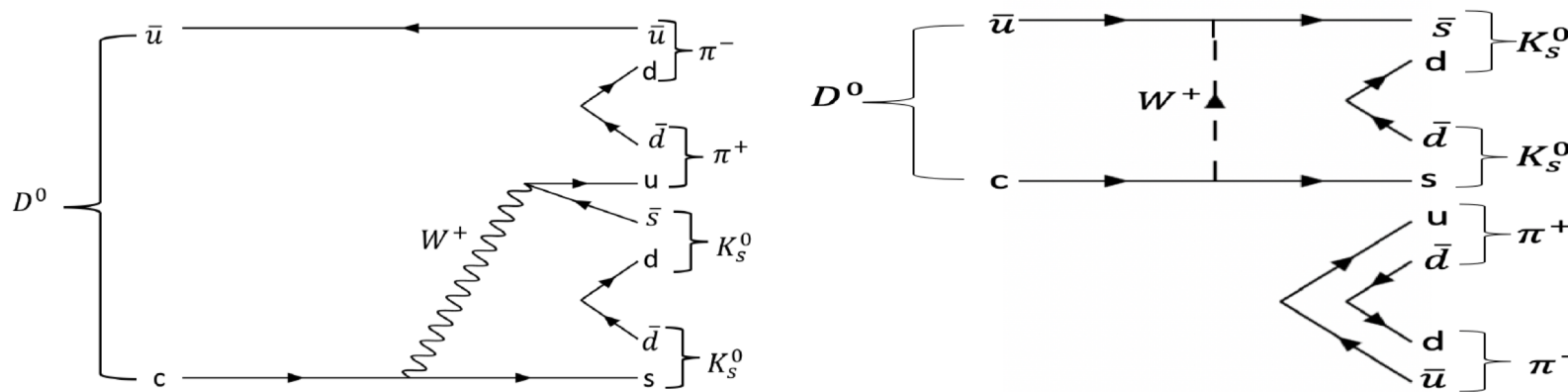
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# Motivation:

- In Standard Model framework, charm meson decays are expected to have very small  $CP$  violation,  $\mathcal{O}(10^{-3})$  or smaller [1]
- $CP$  violation measurement significantly deviating from SM expectation will probe new physics.
- Singly Cabibbo suppressed (SCS) charm decays are expected to be uniquely sensitive to new physics effects. [1]
- First experimental observation of  $CP$  violation in SCS charm mesons was made by LHCb. [2]
- In this analysis, we have searched for  $CP$  violation in the **SCS charm meson decay**  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$
- We also performed branching fraction measurement for this decay mode. (previously measured by BESIII)



[1] (yuval grossman, et al. Phys.Rev.D 75 (2007), 036008)  
 [2] LHCb Collaboration Phys.Rev.Lett. 122 (2019) 21, 211803

# CP violating observable $a_{CP}^T$ :

- We measure the CP violation using T-odd triple product (TP) asymmetries.

- We define scalar triple product  $C_T$  as:

- $$C_T = \vec{p}_{K_s^0} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-})$$
 ( $K_s^0$  with higher momentum is used)

- For  $D^0$  decays, T-odd triple product asymmetry  $A_T$  is defined as :

- $$A_T = \frac{N_1 (C_T > 0) - N_2 (C_T < 0)}{N_1 (C_T > 0) + N_2 (C_T < 0)}$$

- For  $\bar{D}^0$  decays, CP conjugate observables:  $A_T \xrightarrow{CP} \bar{A}_T$ ,  $C_T \xrightarrow{C} \bar{C}_T \xrightarrow{P} -\bar{C}_T$

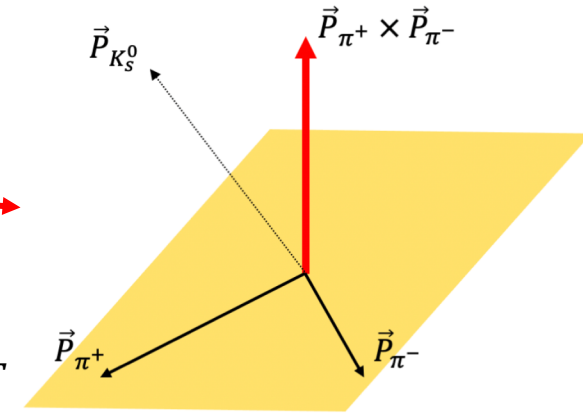
- $$\bar{A}_T = \frac{N_3 (-\bar{C}_T > 0) - N_4 (-\bar{C}_T < 0)}{N_3 (-\bar{C}_T > 0) + N_4 (-\bar{C}_T < 0)}$$

- The difference  $a_{CP}^T = \frac{1}{2} (A_T - \bar{A}_T)$  is a CP violating observable.

- The observable  $a_{CP}^T$  is independent of effects from strong phases.

- By construction,  $a_{CP}^T$  is mostly unaffected by production and detection related asymmetries.

- I. I. Y. Bigi. Charm physics: Like Botticelli in the Sistine Chapel.
- Michael Gronau et.al PRD,495 84(9), Nov 2011.



- Michael Gronau et.al PRD,495 84(9), Nov 2011.

# $CP$ violation measurement using $A_{CP}$ :

- We also measure the  $CP$  violating observable  $A_{CP}$  defined as:

$$A_{CP}^{\text{det}} = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow \bar{f})}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow \bar{f})}$$

- It is the difference in number of  $D^0$  and  $\bar{D}^0$  decays to the  $CP$  conjugate final states  $f$  and  $\bar{f}$ .
- Measurement of both  $A_{CP}$  and  $a_{CP}^T$  are complementary to each other:
  - The observable  $A_{CP} \propto \sin(\phi) \sin(\delta)$ , where  $(\phi)$  is weak and  $(\delta)$  is strong phase difference between the contributing amplitudes.
    - [A. Datta et.al, Int.J.Mod.Phys.A 19 \(2004\), 2505-2544](#)
  - The observable  $a_{CP}^T \propto \sin(\phi) \cos(\delta)$
  - To observe a non zero  $A_{CP}$  strong phase difference  $(\delta)$  must be non zero, whereas the  $a_{CP}^T$  is largest when the strong phase difference  $(\delta)$  is zero.

# Branching fraction (BF) measurement:

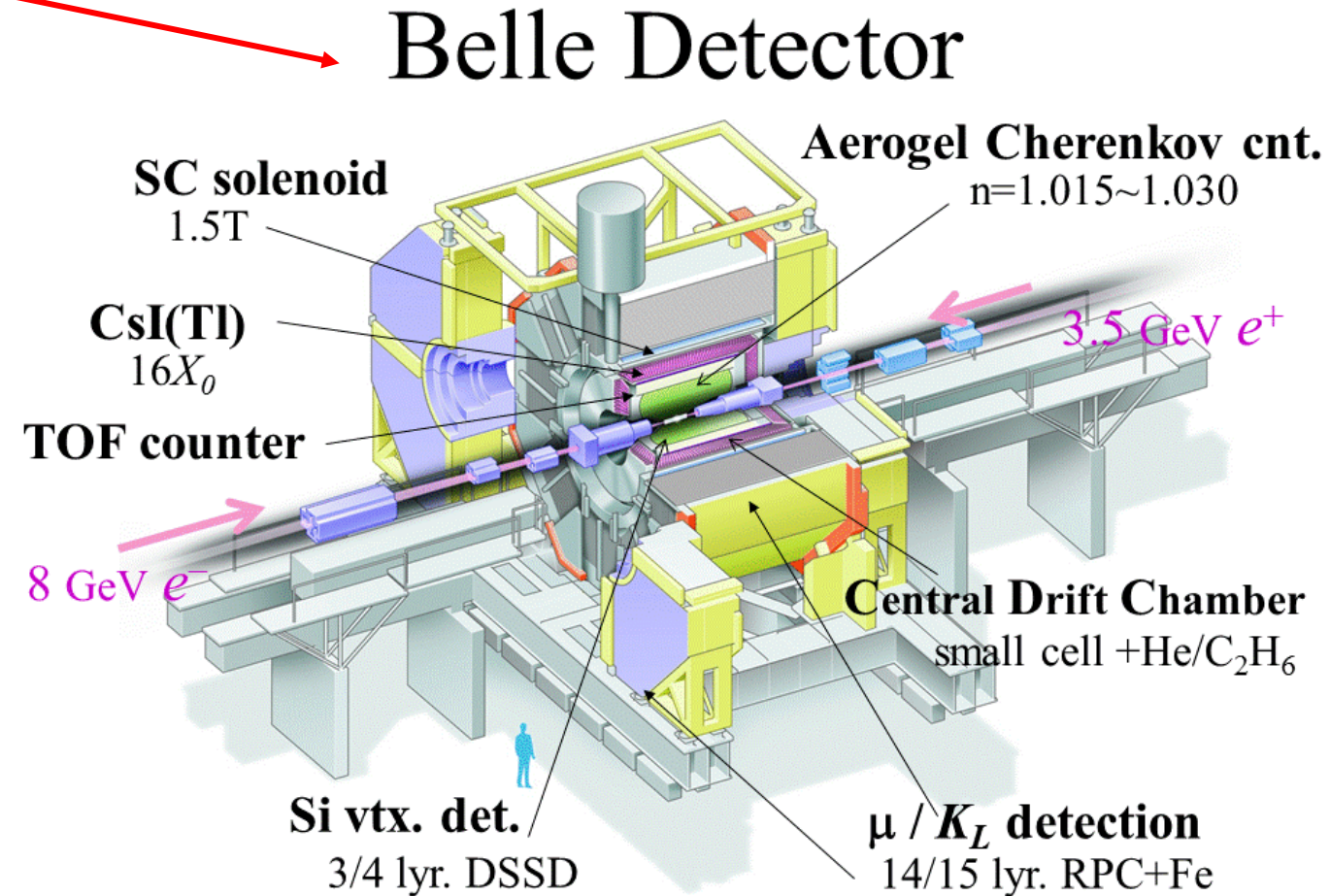
- With our data sample of  $921 \text{ fb}^{-1}$ , we can perform world's most precise measurement of  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  branching fraction.
- We will measure the branching fraction relative to normalization channel  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ .
- The Branching fraction is calculated using :

$$\mathcal{B}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = \left( \frac{N_{K_S^0 K_S^0 \pi^+ \pi^-}}{N_{K_S^0 \pi^+ \pi^-}} \right) \left( \frac{\varepsilon_{K_S^0 \pi^+ \pi^-}}{\varepsilon_{K_S^0 K_S^0 \pi^+ \pi^-}} \right) \times \frac{\mathcal{B}(D^0 \rightarrow K_S^0 \pi^+ \pi^-)}{\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)}$$

Total  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$       Total  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$       Reconstruction efficiency for  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$       Reconstruction efficiency for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$       World average value      World average value

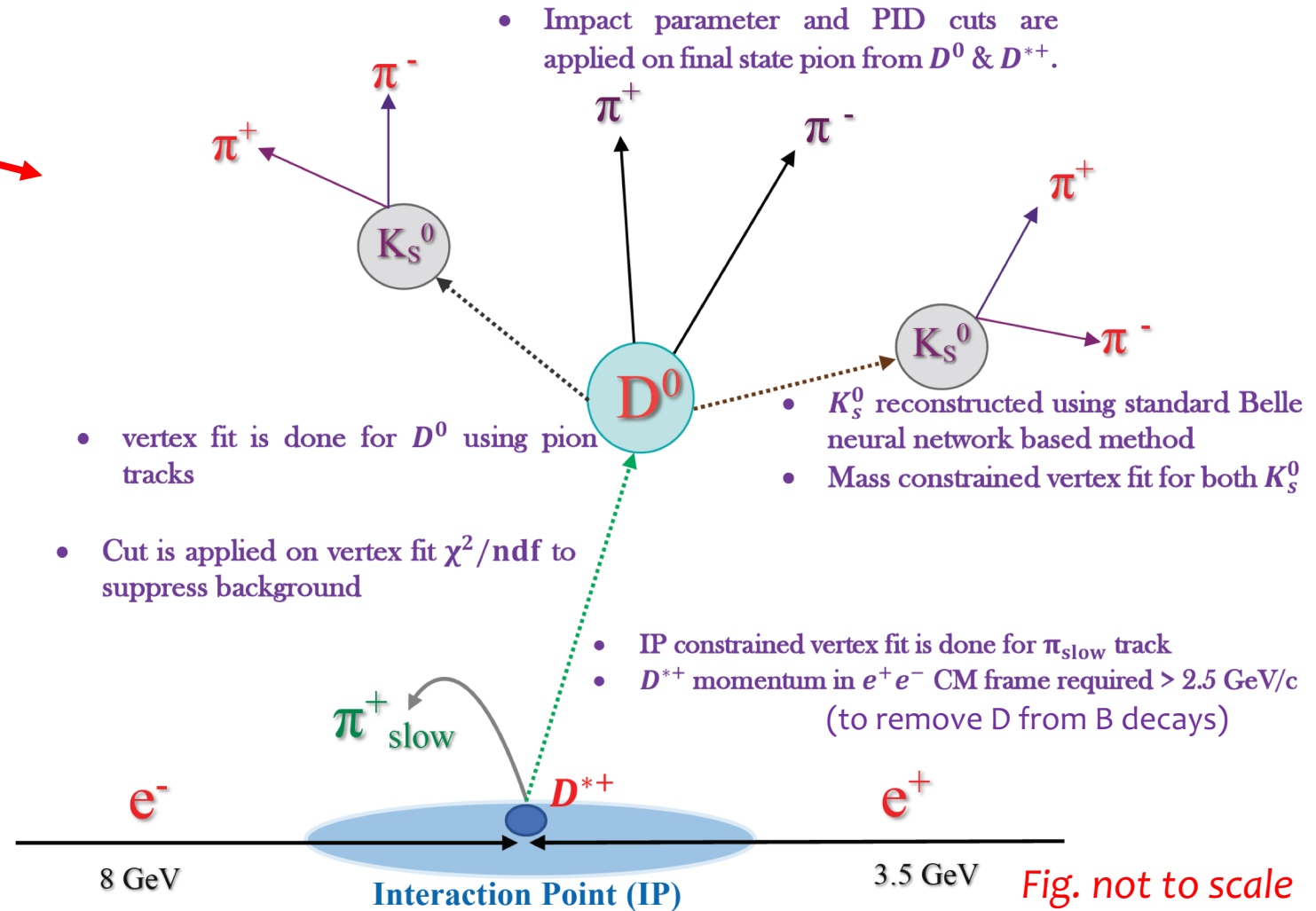
# Belle detector and data sample:

- KEKB accelerator: collided  $8 \text{ GeV } e^-$  with  $3.5 \text{ GeV } e^+$ . (<https://lib506extopc.kek.jp/preprints/PDF/1995/9524/9524007.pdf>)
- Belle detector is situated at collision point of KEKB accelerator. (*Nucl.Instrum.Meth.A* 479 (2002), 117-232)
- Belle detector had:
  - good PID
  - good vertexing capability
- For this analysis we have used data sample corresponding to  $921 \text{ fb}^{-1}$  integrated luminosity.
- Data is collected at  $e^+e^-$  COM energy equal to  $Y(4S)$ , 60 MeV below  $Y(4S)$  and  $Y(5S)$  resonances.



# Reconstruction of decay at Belle detector

- Reconstructed decay chain and the corresponding selection criteria are summarized in the figure on right.
- In case of multiple candidate events, we choose a single candidate corresponding to the lowest value for  $\sum \chi^2 / \text{ndf}$  of  $D^*$ ,  $D^0$  and  $K_S^0$  vertex fit.
- We get a reconstruction efficiency of 6.92% for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$
- We apply same set of selection criteria for normalization channel  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  and obtain a reconstruction efficiency of 14.97 %



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# Branching fraction measurement



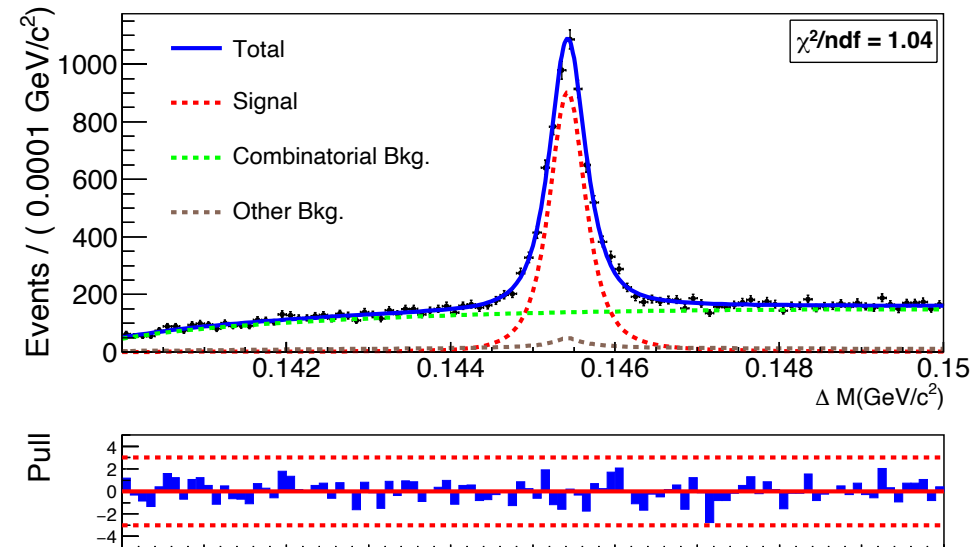
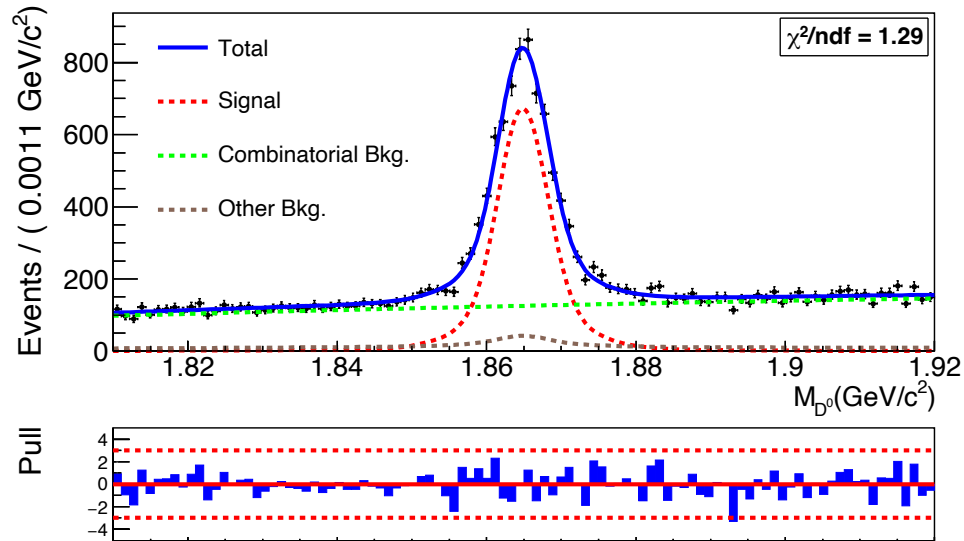
# Signal extraction for BF measurement:

- $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$ :

- To extract the signal events from data sample we have used a 2d unbinned extended maximum likelihood fit in variables:  $M_{D^0} [M(K_S^0 K_S^0 \pi^+ \pi^-)]$  and  $\Delta M [M(K_S^0 K_S^0 \pi^+ \pi^- \pi_{slow}^+) - M(K_S^0 K_S^0 \pi^+ \pi^-)]$

- Fit results from  $921 \text{ fb}^{-1}$  Belle data:

Details on signal and background pdf in backup slide #22



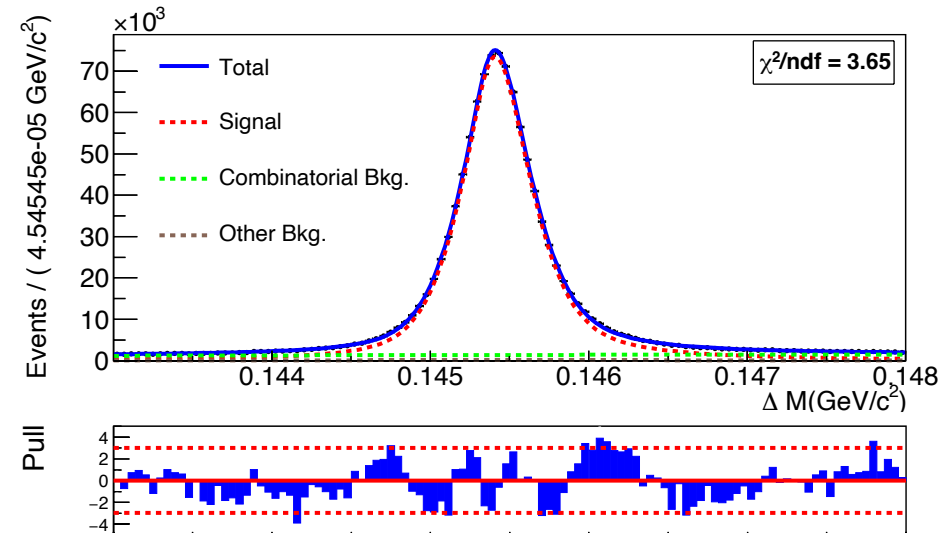
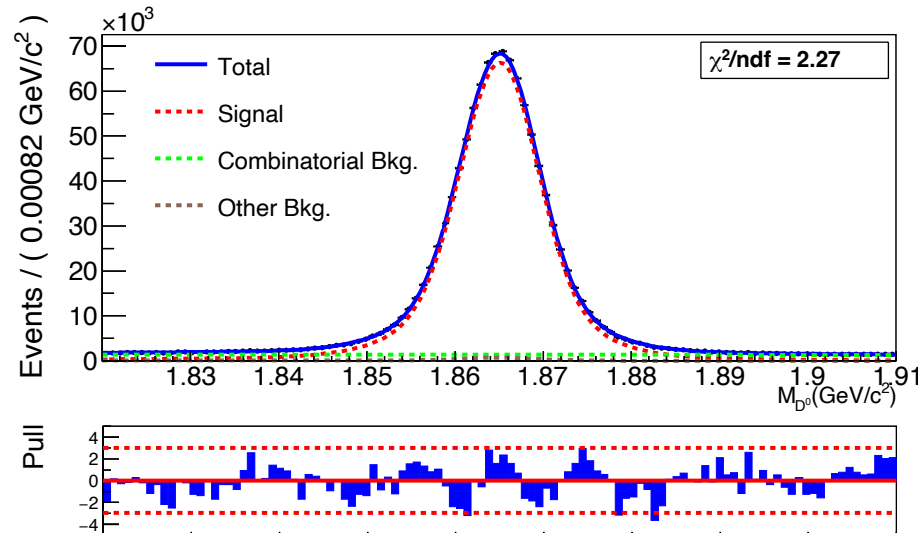
- We obtain  $6095 \pm 98$  signal events from  $921 \text{ fb}^{-1}$  of data.
- We perform the branching fraction measurement relative to normalization channel  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

# Signal extraction for BF measurement:

- $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ :

- To extract the signal events from data sample we have used a 2d binned extended maximum likelihood fit in variables  $M_{D^0}$  and  $\Delta M$
- Fit results from 921 fb<sup>-1</sup> Belle data:

Details on signal and background pdf in backup slide #22



- We obtain  $1069870 \pm 1831 D^0 \rightarrow K_S^0 \pi^+ \pi^-$  events from 921 fb<sup>-1</sup> of data.

- The measured values are:

- $\text{BF}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) / \text{BF}(D^0 \rightarrow K_S^0 \pi^+ \pi^-) = [1.72 \pm 0.03 \text{ (stat.)} \pm 0.04 \text{ (syst.)}] \%$
- $\text{BF}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = [4.82 \pm 0.08 \text{ (stat.)} {}^{+0.10}_{-0.11} \text{ (syst.)} \pm 0.31 \text{ (norm.)}] \times 10^{-4}$

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# $A_{CP}$ measurement

# Fit for $A_{CP}$ :

- The  $A_{CP}$  value obtained using below equation includes contribution from non  $CP$  violating production and reconstruction asymmetries:

$$A_{CP}^{\text{det}} = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow \bar{f})}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow \bar{f})}$$

- $A_{CP}^{\text{det}} = A_{CP} + A_{FB} + A_{\epsilon}^{\pi_s}$ 
  - $A_{CP}$  →  $CP$  violating asymmetry
  - $A_{FB}$  → Forward backward asymmetry
  - $A_{\epsilon}^{\pi_s}$  → Asymmetry due to difference in reconstruction efficiency between  $\pi_s^+$  and  $\pi_s^-$

- To account for  $A_{\epsilon}^{\pi_s}$ , we weight the  $D^0$  and  $\bar{D}^0$  events as:
 
$$w_{D^0} = 1 - A_{\epsilon}^{\pi_s}(p_T, \cos \theta_{\pi_s})$$

$$w_{\bar{D}^0} = 1 + A_{\epsilon}^{\pi_s}(p_T, \cos \theta_{\pi_s})$$

- Resulting  $A_{CP}$  now includes  $A_{CP}^{\text{cor}} = A_{CP} + A_{FB}$ .

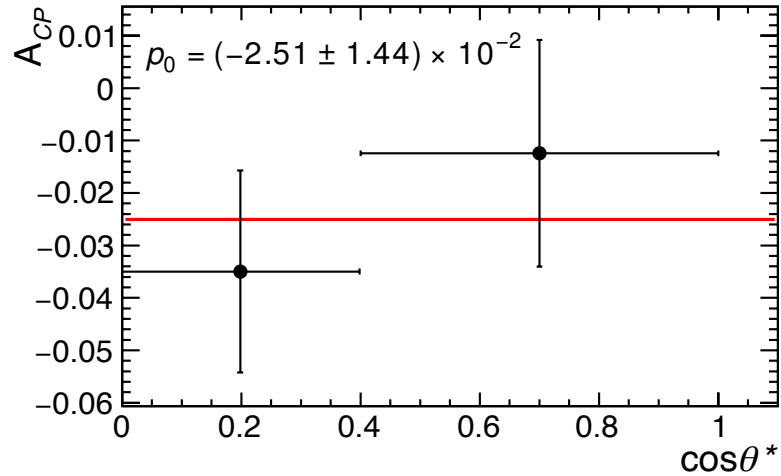
- The forward backward asymmetry is odd function of  $\cos(\theta^*)$ , where  $\theta^*$  is  $D^*$  polar angle in COM frame.

- For a given  $\cos(\theta^*)$  bin, we obtain true  $CP$  violating asymmetry:
 
$$A_{CP} = \frac{A_{CP}^{\text{cor}}(\cos \theta^*) + A_{CP}^{\text{cor}}(-\cos \theta^*)}{2}$$

- The average of all positive  $\cos(\theta^*)$  bins will be quoted as final  $A_{CP}$  asymmetry.

# $A_{CP}$ results from $921 \text{ fb}^{-1}$ Belle data:

$A_{CP}$  values as function of  $\cos(\theta^*)$ :

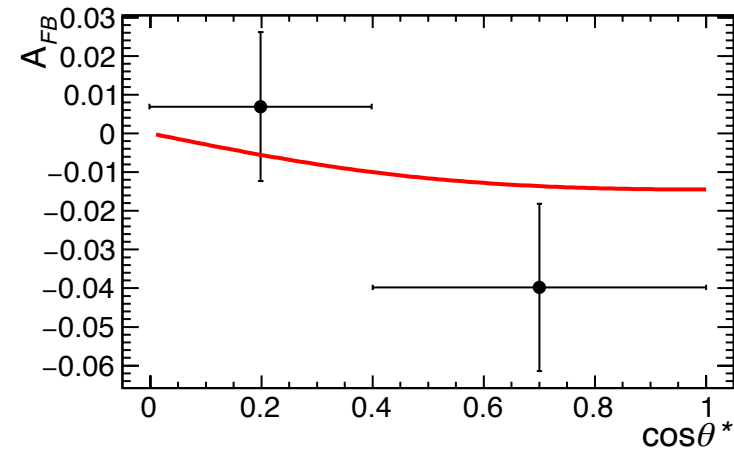


- The red line is a straight line fit to  $A_{CP}$  values

- Final  $A_{CP}$  result is:

$$A_{CP} = \left[ -2.51 \pm 1.44 \text{ (stat.) } {}^{+0.35}_{-0.52} \text{ (syst.)} \right] \times 10^{-2}$$

$A_{FB}$  values as function of  $\cos(\theta^*)$ :



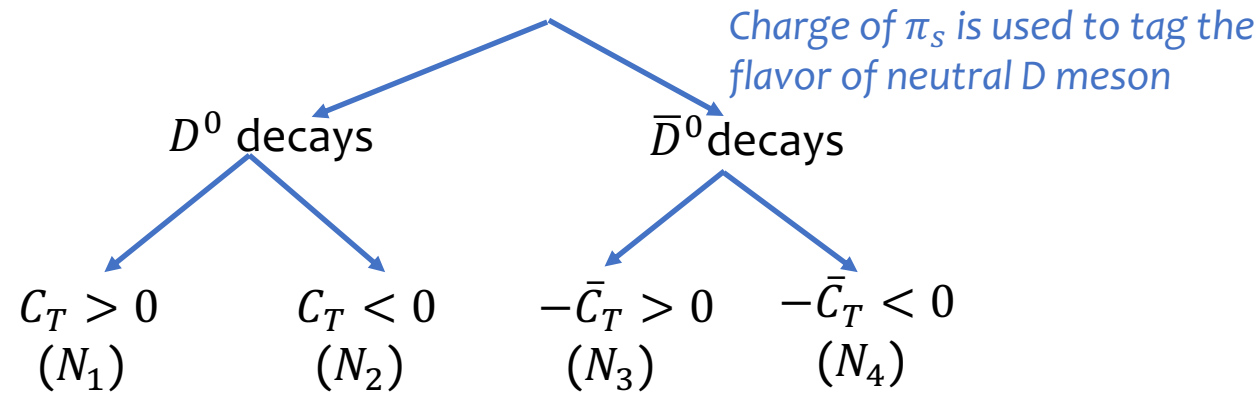
- The red line shows the expected prediction for  $A_{FB}$   
 $A_{FB} = 0.029 \cos(\theta^*) / (1 + \cos^2(\theta^*))$

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# $a_{CP}^T$ measurement

# Simultaneous fit for $a_{CP}^T$ measurement:

- To measure  $a_{CP}^T$ , data sample is divided into four categories:



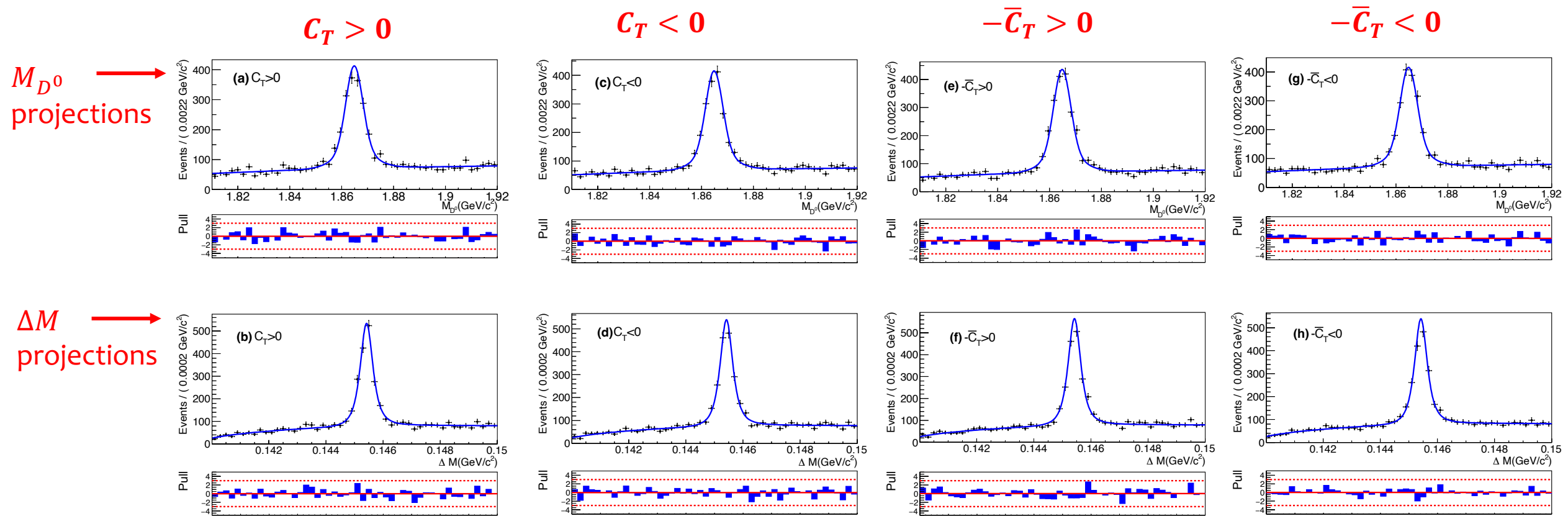
- To obtain  $a_{CP}^T$ , we perform a 2d unbinned extended maximum likelihood fit simultaneously to these four datasets.
- Instead of yields  $N_1, N_2, N_3$  and  $N_4$ , we float  $N_1, A_T, N_3$  and  $a_{CP}^T$ . This choice is made to get correct uncertainty in  $a_{CP}^T$  from fit results instead of calculating them using the uncertainty in yields.
- The expression for  $N_2$  and  $N_4$  in terms of  $N_1, A_T, N_3$  and  $a_{CP}^T$  are obtained as shown below:

$$A_T = \frac{N_1 (C_T > 0) - N_2 (C_T < 0)}{N_1 (C_T > 0) + N_2 (C_T < 0)}, \quad \longrightarrow \quad N_2 = \frac{N_1 (1 - A_T)}{1 + A_T}$$

$$\bar{A}_T = \frac{N_3 (-\bar{C}_T > 0) - N_4 (-\bar{C}_T < 0)}{N_3 (-\bar{C}_T > 0) + N_4 (-\bar{C}_T < 0)} \quad \text{and} \quad a_{CP}^T = \frac{1}{2} (A_T - \bar{A}_T) \quad \longrightarrow \quad N_4 = \frac{N_3 (1 - (A_T - 2 * a_{CP}^T))}{1 + (A_T - 2 * a_{CP}^T)}$$

# Simultaneous fit for $a_{CP}^T$ measurement:

- From 921 fb<sup>-1</sup> Belle data we obtain:
  - $a_{CP}^T = [-1.95 \pm 1.42 \text{ (stat.) } _{-0.12}^{+0.14} \text{ (syst.)}]%$
  - The result is consistent with no CP violation within uncertainties.
- Simultaneous fit projections on  $M_{D^0}$  and  $\Delta M$  for four data samples are shown below:





# Summary:

1. We have measured the branching fraction of  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  :  
$$BF(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = [4.82 \pm 0.08 \text{ (stat.) } {}^{+0.10}_{-0.11} \text{ (syst.) } \pm 0.31 \text{ (norm.)}] \times 10^{-4}$$
  - (BESIII measurement:  $= [5.30 \pm 0.90 \text{ (stat.) } \pm 0.30 \text{ (syst.)}] \times 10^{-4}$ )

*This is the world's most precise measurement for this decay mode.*

- 2> We have measured the  $CP$  violating observable  $A_{CP}$  :  
$$A_{CP} = [-2.51 \pm 1.44 \text{ (stat.) } {}^{+0.35}_{-0.52} \text{ (syst.)}] \times 10^{-2}$$

*The measured  $A_{CP}$  value is consistent with zero  $CP$  violation.*

- 3> We have measured  $CP$  violating observable  $a_{CP}^T$  :  
$$a_{CP}^T = [-1.95 \pm 1.42 \text{ (stat.) } {}^{+0.14}_{-0.12} \text{ (syst.)}] \times 10^{-2}$$

*This measurement is also consistent with zero  $CP$  violation.*

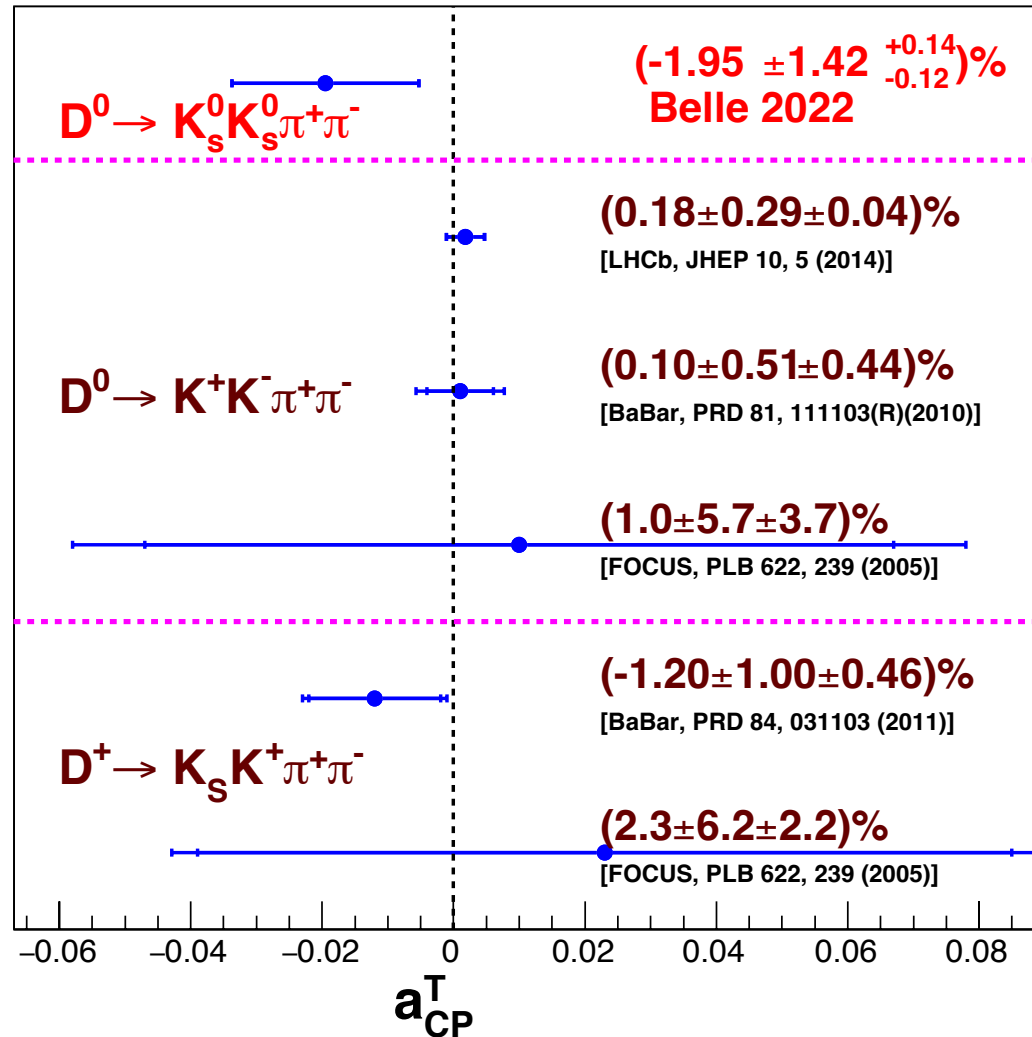
Thank You!

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# Backup

# Search for CP violation using $a_{CP}^{T-odd}$ in D decays :

## $a_{CP}^T$ measurements in SCS D decays



# Variables used for $K_S^0$ reconstruction by Belle neural network based method

- $K_S^0$  momentum in lab frame.
- Distance along the z axis between two track helices at their closest approach.
- Flight length in x-y plane.
- Angle between  $K_S^0$  momentum and the vector joining IP to  $K_S^0$  decay vertex.
- Angle between  $\pi$  momentum and laboratory frame direction in  $K_S^0$  rest frame.
- Distance of closest approach in the x-y plane between the IP and the two pion helices.
- Total number of hits in SVD (silicon vertex detector) and CDC (central drift chamber) for two pion tracks.

# Signal extraction for BF measurement:

- $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$ :
  - Using simulation, events are divided into following categories:
    - **Events with correctly reconstructed signal decays.**
    - **Random  $\pi_{\text{slow}}$  background.** (*correctly reconstructed  $D^0$  combined with wrong  $\pi_{\text{slow}}$* )
    - **Broken charm peaking background.** (*reconstruction missed one or more final state particles from a real  $D^0$  decay to a non signal final state*)
    - **$D^0 \rightarrow 3K_S^0$  peaking background** (*96% vetoed by selection on  $\pi^+ \pi^-$  invariant mass*).
    - **Combinatorial background.** (*random combination of final state particles*)
- $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ :
  - Using simulation, events are divided into following categories:
    - **Events with correctly reconstructed signal decays.**
    - **Random  $\pi_{\text{slow}}$  background.**
    - **Broken charm peaking background.**
    - **Combinatorial background.**

# Details of pdfs used to extract signal:

1>  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$ :

Component type	$M_{D^0}$	$\Delta M$
Signal decays	3 Asymmetric Gaussian (AG)	2AG + 1 student-t
Mis-reconstructed signal	2 <sup>nd</sup> order chebychev polynomial	4 <sup>th</sup> order chebychev polynomial
Random $\pi_{\text{slow}}$ background	Same as signal	$Q^{\frac{1}{2}} + \alpha Q^{\frac{3}{2}}$ ( $Q = \Delta M - M_\pi$ )
Broken charm background	2 gaussian	student-t
$D^0 \rightarrow 3K_S^0$ background	gaussian	student-t
Combinatoric background	2 <sup>nd</sup> order chebychev polynomial	$Q^{\frac{1}{2}} + \alpha' Q^{\frac{3}{2}}$

2>  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ :

Component type	$M_{D^0}$	$\Delta M$
Signal decays	3 Asymmetric Gaussian (AG)	1G + 1 Asymmetric student-t
Random $\pi_{\text{slow}}$ background	Same as signal	$Q^{\frac{1}{2}} + \alpha Q^{\frac{3}{2}}$ ( $Q = \Delta M - M_\pi$ )
Broken charm background	gaussian + 2 <sup>nd</sup> order polynomial	student-t
Combinatoric background	1 <sup>st</sup> order chebychev polynomial	$Q^{\frac{1}{2}} + \alpha' Q^{\frac{3}{2}}$

# Rearranging asymmetry equations on slide 5

- $A_T = \frac{N_1 (C_T > 0) - N_2 (C_T < 0)}{N_1 (C_T > 0) + N_2 (C_T < 0)}$ ,  $\Rightarrow N_2 = \frac{N_1 (1 - A_T)}{(1 + A_T)}$
- $\bar{A}_T = \frac{N_3 (-\bar{C}_T > 0) - N_4 (-\bar{C}_T < 0)}{N_3 (-\bar{C}_T > 0) + N_4 (-\bar{C}_T < 0)}$  and  $a_{\text{CP}}^{\text{T-odd}} = \frac{1}{2}(A_T - \bar{A}_T) \Rightarrow N_4 = \frac{N_3 (1 - (A_T - 2 * a_{\text{CP}}^{\text{T-odd}}))}{1 + (A_T - 2 * a_{\text{CP}}^{\text{T-odd}})}$



# Systematic uncertainty for BF:

Summary of systematic uncertainty for BF measurement:

Source	$K_S^0 K_S^0 \pi^+ \pi^-$ (%)	$K_S^0 \pi^+ \pi^-$ (%)
Fixed PDF parameters	0.14	0.09
$D^0 \rightarrow K_S^0 K_S^0 K_S^0$ background	0.11	–
Broken charm background	0.98	–
MC statistics	0.26	0.17
PID efficiency correction	0.80	0.74
$K_S^0$ reconstruction efficiency	0.83	0.36
Tracking Efficiency	0.70	–
$M(\pi^+ \pi^-)$ veto efficiency	+0.42 –0.93	–
Fraction of mis-reconst. signal	+0.02 –0.03	–
$D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$ decay model	0.73	–
$\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$	0.07	–
Total for $\mathcal{B}_{K_S^0 K_S^0 \pi^+ \pi^-} / \mathcal{B}_{K_S^0 \pi^+ \pi^-}$		+2.07 –2.23

The final BF results are:

$$1 > \text{BF}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) / \text{BF}(D^0 \rightarrow K_S^0 \pi^+ \pi^-) = [1.72 \pm 0.03 \text{ (stat.)} \pm 0.04 \text{ (syst.)}] \%$$

$$2 > \text{BF}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = [4.82 \pm 0.08 \text{ (stat.)} \begin{smallmatrix} +0.10 \\ -0.11 \end{smallmatrix} \text{ (syst.)} \pm 0.31 \text{ (norm.)}] \times 10^{-4}$$

- This is the world's most precise measurement for  $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$  branching fraction.

BESIII result:

$$\text{BF}(D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-) = [5.20 \pm 0.90 \text{ (stat.)} \pm 0.30 \text{ (syst.)}] \times 10^{-4}$$

# Systematic uncertainty for $a_{CP}^T$ :

Summary of systematic uncertainties evaluated for  $a_{CP}^T$ :

Source	(%)
Fixed PDF parameters	0.010
$D^0 \rightarrow K_S^0 K_S^0 K_S^0$ background	+0.000 -0.013
Broken charm background	+0.014 -0.040
Efficiency variation with $C_T, \overline{C}_T$	+0.14 -0.11
Total	+0.14 -0.12

- This yield a final result  $a_{CP}^T = [-1.95 \pm 1.42 \text{ (stat.) } {}^{+0.14}_{-0.12} \text{ (syst.)}]%$
- This result is consistent with no  $CP$  violation within uncertainties.

# Systematic uncertainty for $A_{CP}$ :

Summary of systematic uncertainties evaluated for  $A_{CP}$

Sources	(%)
Fixed PDF parameters	$\pm 0.01$
$D^0 \rightarrow K_S^0 K_S^0 K_S^0$ background	$+0.02$ $-0.03$
Broken charm background	$+0.09$ $-0.07$
Binning in $\cos \theta^*$	$+0.33$ $-0.51$
Reconstruction asymmetry $A_{\epsilon}^{\pi^s}$	$\pm 0.01$
Fixed background fractions	$\pm 0.04$
Total	$+0.35$ $-0.52$

- Final  $A_{CP}$  result is :

$$A_{CP} = \left[ -2.51 \pm 1.44 \text{ (stat.) } {}^{+0.35}_{-0.52} \text{ (syst.)} \right] \times 10^{-2}$$

# $A_{\varepsilon}^{\pi_s}$ weights for $A_{CP}$ :

$$A_{\varepsilon}^{\pi_s} = \frac{\varepsilon_f^+ - \varepsilon_f^-}{\varepsilon_f^+ + \varepsilon_f^-}$$

$\varepsilon_f^{\pm}$ : reconstruction efficiency for  $\pi_{slow}^{\pm}$

$$W_{D^0} = 1 + A_{\varepsilon}^{\pi_s} = \frac{2\varepsilon_f^+}{\varepsilon_f^+ + \varepsilon_f^-}$$

$$W_{\bar{D}^0} = 1 - A_{\varepsilon}^{\pi_s} = \frac{2\varepsilon_f^-}{\varepsilon_f^+ + \varepsilon_f^-}$$

Efficiency for  $D^0$  and  $\bar{D}^0$  become same after applying these weights

# All measurements of CP violation in charm decays using $a_{CP}^{T\text{-odd}}$ :

- [https://hflav-eos.web.cern.ch/hflav-eos/charm/cp\\_asym/charm\\_todd\\_19Sep19.html](https://hflav-eos.web.cern.ch/hflav-eos/charm/cp_asym/charm_todd_19Sep19.html)

## T-odd asymmetries in $D^0$ decays

Year	Experiment	T-odd asymmetry in the decay mode $D^0$ to $K+K-\pi+\pi-$	$A_{T\text{-odd}} = (A_T - \bar{A}_T)/2$
2019	BELLE	<a href="#">J. B. Kim et al. (BELLE Collab.), Phys. Rev. D 99, 011104 (2019).</a>	$+0.0052 \pm 0.0037 \pm 0.0007$
2014	LHCb	<a href="#">R. Aaij et al. (LHCb Collab.), JHEP 10, 5 (2014).</a>	$+0.0018 \pm 0.0029 \pm 0.0004$
2010	BABAR	<a href="#">P. del Amo Sanchez et al. (BABAR Collab.), Phys. Rev. D 81, 111103 (2010).</a>	$+0.0010 \pm 0.0051 \pm 0.0044$
2005	FOCUS	<a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 622, 239 (2005).</a>	$+0.010 \pm 0.057 \pm 0.037$
HFLAV average			$+0.0035 \pm 0.0021$
Year	Experiment	T-odd asymmetry in the decay mode $D^0$ to $K^0s\pi+\pi-\pi^0$	$A_{T\text{-odd}} = (A_T - \bar{A}_T)/2$
2017	BELLE	<a href="#">K. Prasanth et al. (BELLE Collab.), Phys. Rev. D 95, 091101 (2017).</a>	$-0.00028 \pm 0.00138 (+0.00023 -0.00076)$

## T-odd asymmetries in $D^+$ decays

Year	Experiment	T-odd asymmetry in the decay mode $D^+$ to $K^0sK+\pi+\pi-$	$A_{T\text{-odd}} = (A_T - \bar{A}_T)/2$
2011	BABAR	<a href="#">J.P. Lees et al. (BABAR Collab.), Phys. Rev. D 84, 031103 (2011).</a>	$-0.0120 \pm 0.0100 \pm 0.0046$
2005	FOCUS	<a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 622, 239 (2005).</a>	$+0.023 \pm 0.062 \pm 0.022$
HFLAV average			$-0.0110 \pm 0.0109$

## T-odd asymmetries in $D_s^+$ decays

Year	Experiment	T-odd asymmetry in the decay mode $D_s^+$ to $K^0sK+\pi+\pi-$	$A_{T\text{-odd}} = (A_T - \bar{A}_T)/2$
2011	BABAR	<a href="#">J.P. Lees et al. (BABAR Collab.), Phys. Rev. D 84, 031103 (2011).</a>	$-0.0136 \pm 0.0077 \pm 0.0034$
2005	FOCUS	<a href="#">J.M. Link et al. (FOCUS Collab.), Phys. Lett. B 622, 239 (2005).</a>	$-0.036 \pm 0.067 \pm 0.023$
HFLAV average			$-0.0139 \pm 0.0084$