



# *Semileptonic $B$ -decays to excited charmed mesons*

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Universität Siegen

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with Nico Gubernari, Alexander Khodjamirian & Thomas Mannel

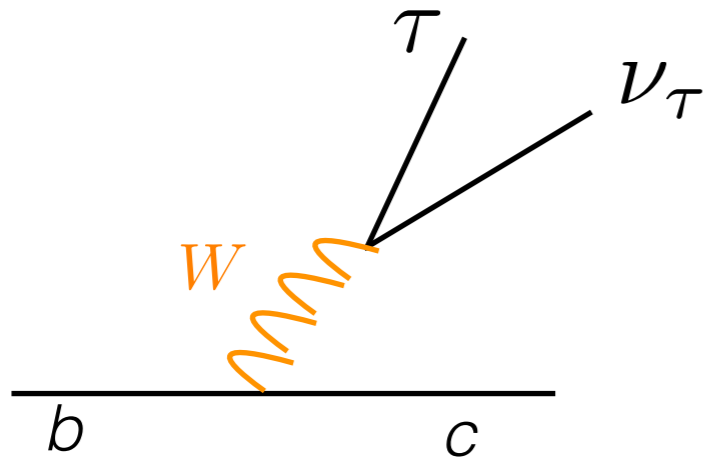


# Outline

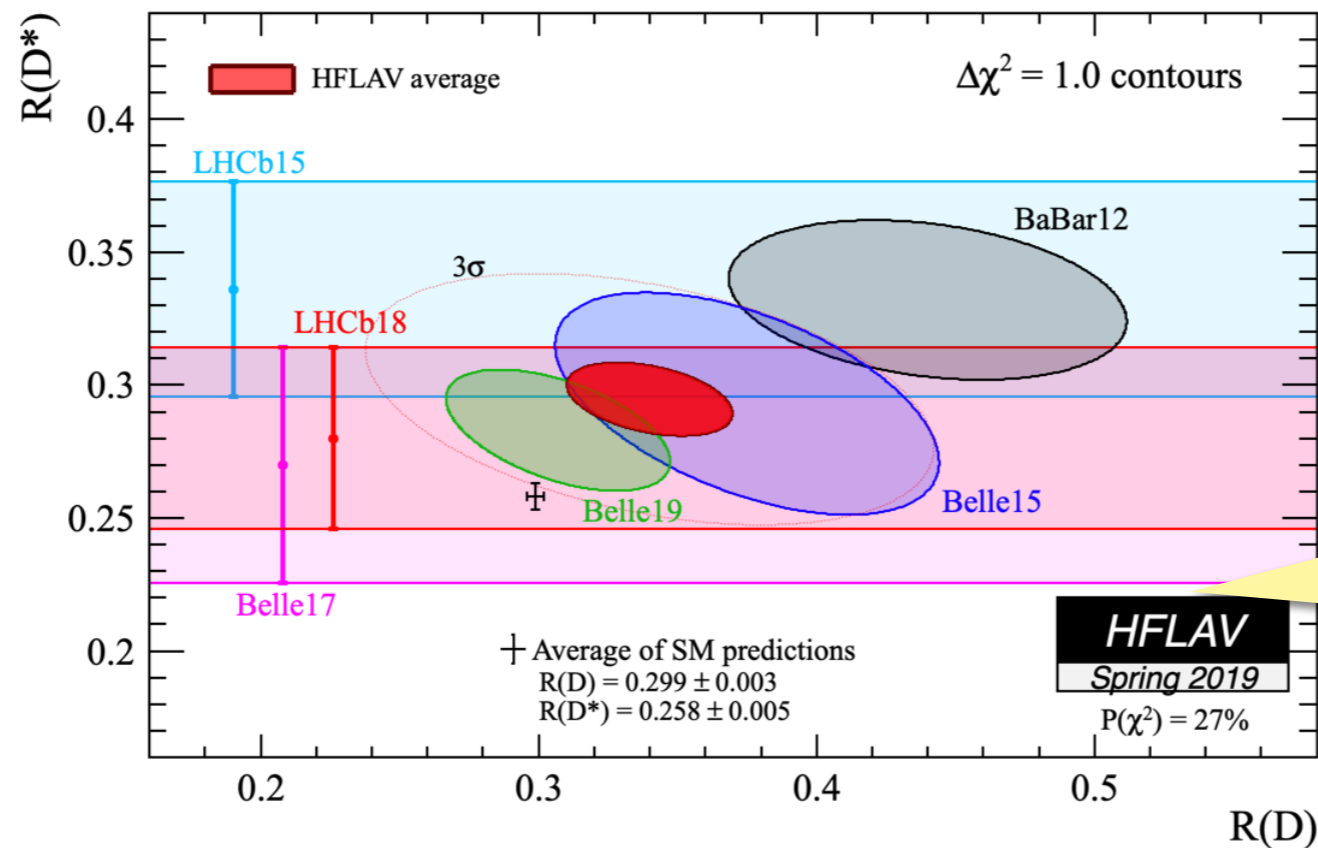
- Introduction
- QCD Sum Rules
- Results
- Summary & Outlook

# B anomalies

► Exciting discrepancies observed in charged current  $B$  decays



$$R(D^{(*)}) \equiv \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)}, \quad \ell \in \{e, \mu\}$$



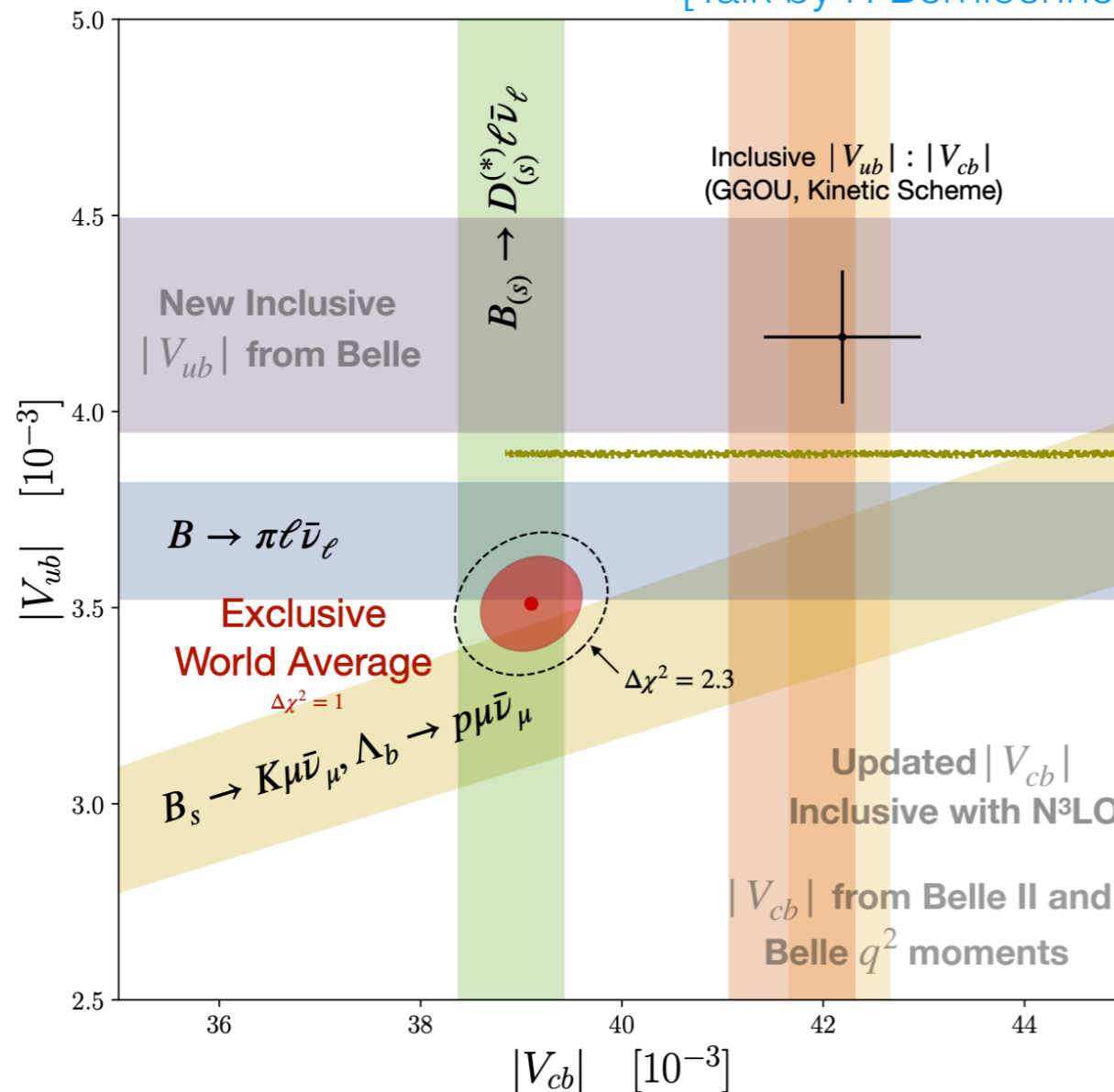
combined deviation  
 $\sim 3\sigma$



# $V_{cb}$ puzzle

► **Tension** between exclusive & inclusive determinations of  $V_{cb}$

[Talk by F. Bernlochner]



$B \rightarrow D\ell\nu, B \rightarrow D^*\ell\nu, B_s \rightarrow D_s\ell\nu$   
 measurements  
 +  
 Form Factors from  
 LCSR & several Lattice groups

# Excited charmed mesons

Meson	$j$	$J^P$	Mass [MeV]	Width [MeV]
$D_0^*(2300)$	$\frac{1}{2}$	$0^+$	$2343 \pm 10$	$229 \pm 16$
$D_1(2430) \equiv D_1'$	$\frac{1}{2}$	$1^+$	$2412 \pm 9$	$314 \pm 29$
$D_1(2420) \equiv D_1$	$\frac{3}{2}$	$1^+$	$2422.1 \pm 0.6$	$31.3 \pm 1.9$
$D_2^*(2460)$	$\frac{3}{2}$	$2^+$	$2461.1 \pm 0.8$	$47.3 \pm 0.8$

excited mesons provide complementary info.

- New extraction of  $V_{cb}$  via  $B \rightarrow D^{**}$
- Understanding backgrounds for  $R(D^{(*)})$  & extraction of  $V_{ub}$
- Gap  $\sim 25\%$  between incl.  $B \rightarrow X_c \ell \nu$  & sum of excl. branching dominated by  $D_0, D^*(2007)$

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► Estimate of form factors available only in infinite  $c$ -quark mass limit

[Bernlochner, Ligeti: '16]

► Two  $1^+$  states are very close in mass & one with large width

# QCD sum rules

► QCD Sum Rule methods for **non perturbative** estimates



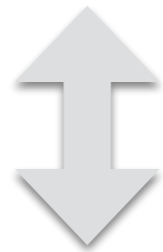
Based on **Operator product expansion**

[Shifman *et al.* '79]

**Perturbatively** calculable  
amplitudes

+

Quark & gluon **condensate**:  
characterises QCD vacuum  
or distribution amplitudes in LCSR



**Dispersion relation**

[Khodjamirian *et al.* '05, '07]

Physical hadronic parameters



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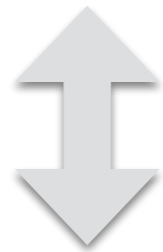
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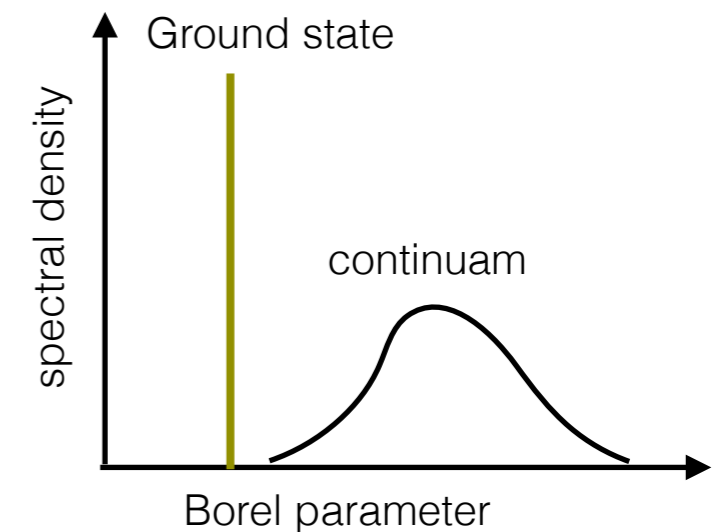


**Dispersion relation**

[Khodjamirian *et al.* '05,'07]

Physical hadronic parameters

► Limitations: hadronic parameter extraction depends on **model ansatzs** for the spectrum



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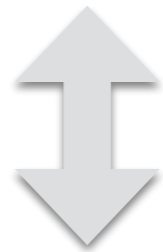
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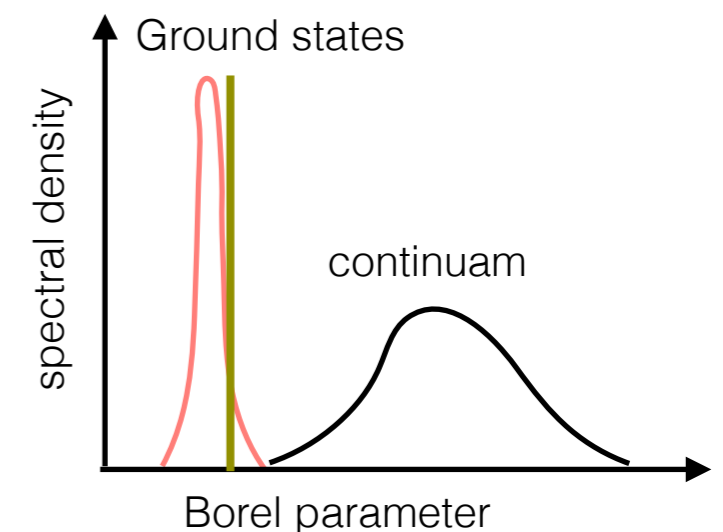


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# $D^{**}$ mesons

► Correlation function with **two independent** currents

$$\Pi_{\mu\nu}^{(ij)}(q) = i \int d^4x e^{iqx} \langle 0 | \mathcal{T} \{ J_\mu^{(i)}(x) J_\nu^{(j)\dagger}(0) \} | 0 \rangle = -g_{\mu\nu} \Pi^{(ij)}(q^2) + q_\mu q_\nu \tilde{\Pi}^{(ij)}(q^2)$$

$$J_\mu^{(1)} = (m_c + m_q) \bar{c} \gamma_\mu \gamma_5 q$$

$$J_\mu^{(2)} = i \bar{c} \gamma_5 \overleftrightarrow{D}_\mu q,$$



interpolates **both**  $1^+$   
states simultaneously

$0^-$  contribution

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➔ Hadronic representation (contains both states) convoluted with Breit-Wigner form to account for the **large width** of  $D_1'$

► Matching with OPE:  $\Pi_{\text{OPE}}^{(ij)}(q^2) = \Pi_{\text{pert}}^{(ij)}(q^2) + \Pi_{\text{cond}}^{(ij)}(q^2)$

➔ **Three** QCD sum rules with **four** decay constants

need to **rely** on **external input** e.g., Branching Fraction [BABAR '08]

# FFs with Light-cone SR

►  $B \rightarrow D_1^{(\prime)}$  hadronic matrix element in terms of form factors

$$\begin{aligned} \langle R(p, \varepsilon) | J_\mu^w | \bar{B}(p+q) \rangle = & -i\varepsilon_\mu^{(R)*} (m_B + m_R) V_1^{BR}(q^2) + i(2p+q)_\mu (\varepsilon^{(R)*} \cdot q) \frac{V_2^{BR}(q^2)}{m_B + m_R} \\ & + iq_\mu (\varepsilon^{(R)*} \cdot q) \frac{2m_R}{q^2} (V_3^{BR}(q^2) - V_0^{BR}(q^2)) - \epsilon_{\mu\nu\alpha\beta} \varepsilon^{(R)*\nu} p^\alpha q^\beta \frac{2A^{BR}(q^2)}{m_B + m_R}, \end{aligned}$$

where  $2m_R V_3^{BR}(q^2) = (m_B + m_R) V_1^{BR}(q^2) - (m_B - m_R) V_2^{BR}(q^2)$  and  $V_0^{BR}(0) = V_3^{BR}(0)$

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► Similar process to write LCSRs with correlators

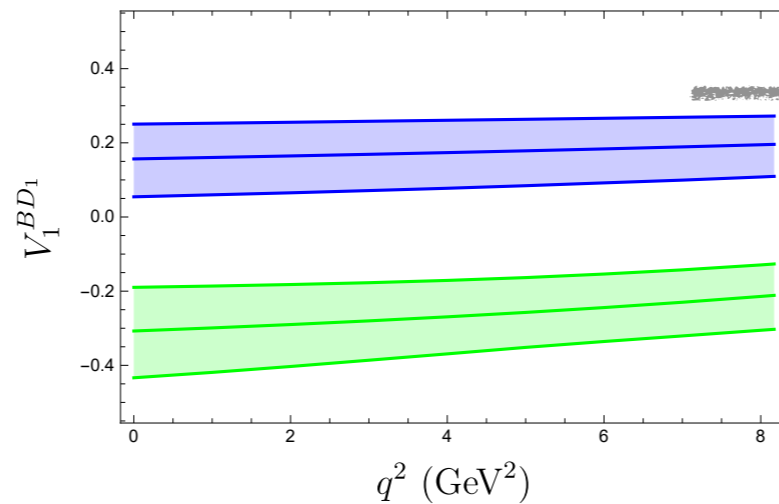
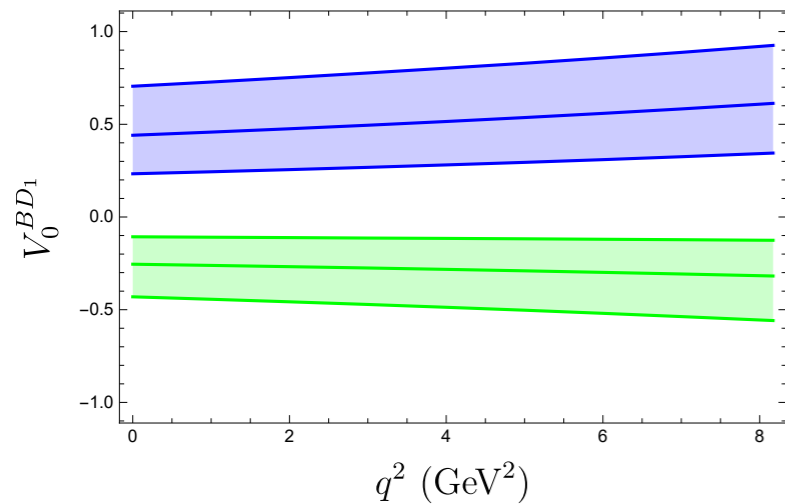
$$\mathcal{F}_{\mu\nu}^{(R)}(p, q) = i \int d^4x e^{ip \cdot x} \langle 0 | \mathcal{T} \{ J_\nu^{(R)\dagger}(x), J_\mu^w(0) \} | \bar{B}(p+q) \rangle$$

► Obtained FFs in -ve  $q^2$  extrapolated to +ve region with **z-expansion**

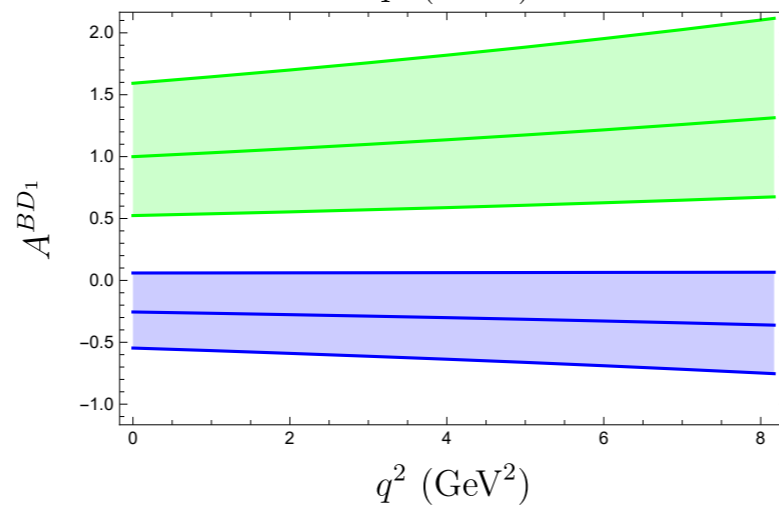
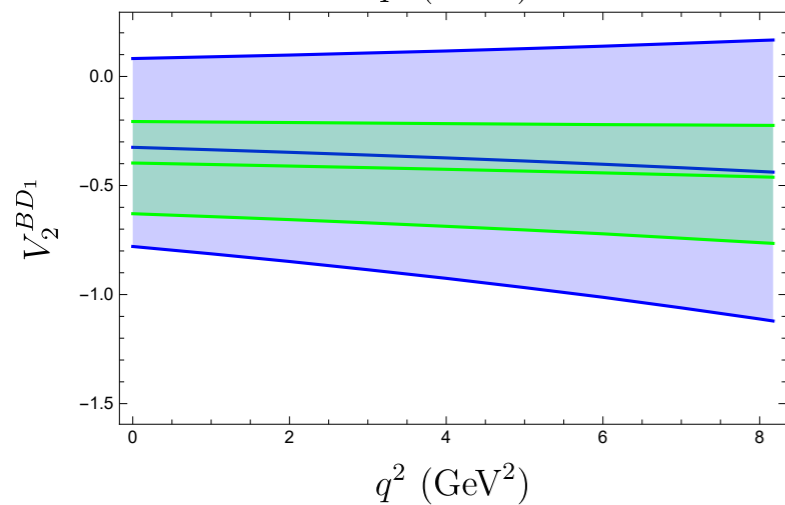
[Bourelly et al. '08]

$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}} \quad t_+ = (m_B + m_D)^2 \\ t_0 = (m_B + m_D) (\sqrt{m_B} - \sqrt{m_D})^2$$

# $B \rightarrow D_1$ Form factors

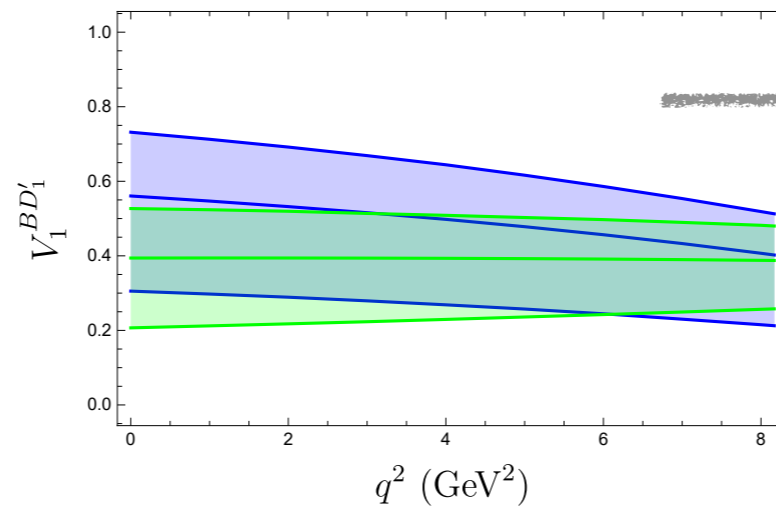
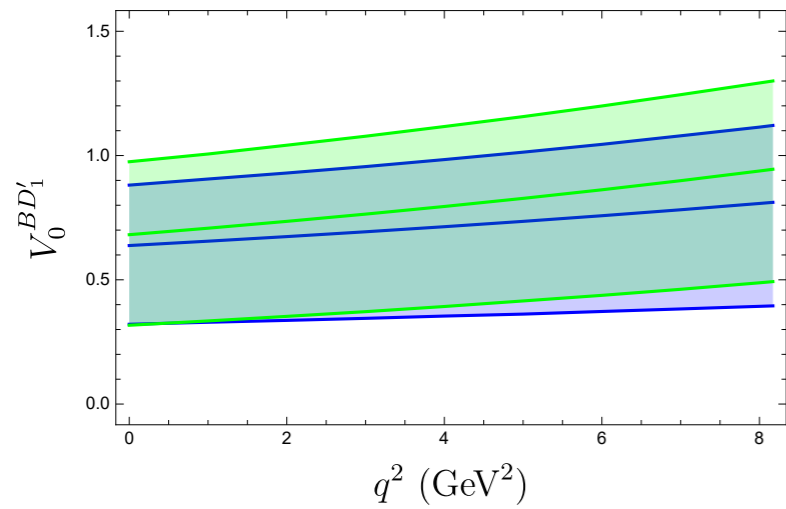


Large uncertainty  
(with 2-fold ambiguity)

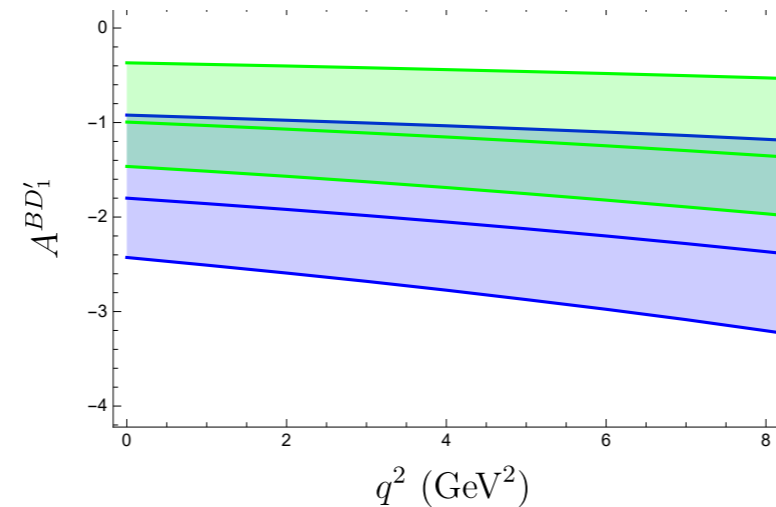
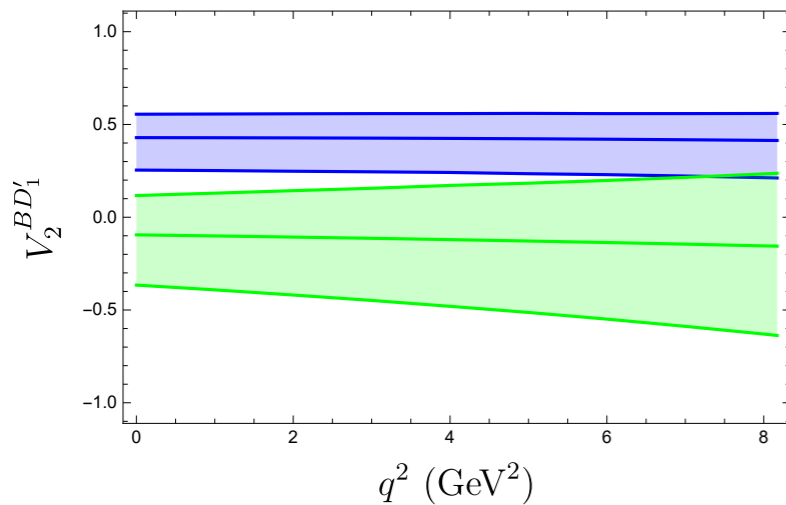


Lattice inputs on decay constant will help to reduce uncertainty/ambiguity

# $B \rightarrow D_1'$ Form factors



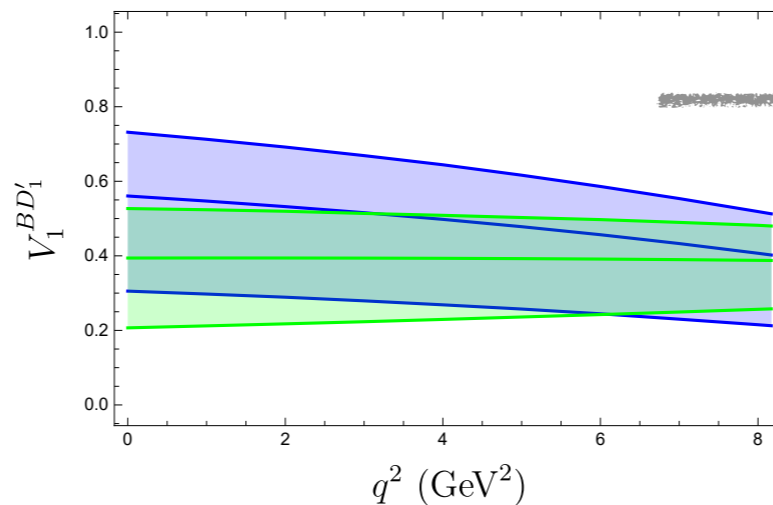
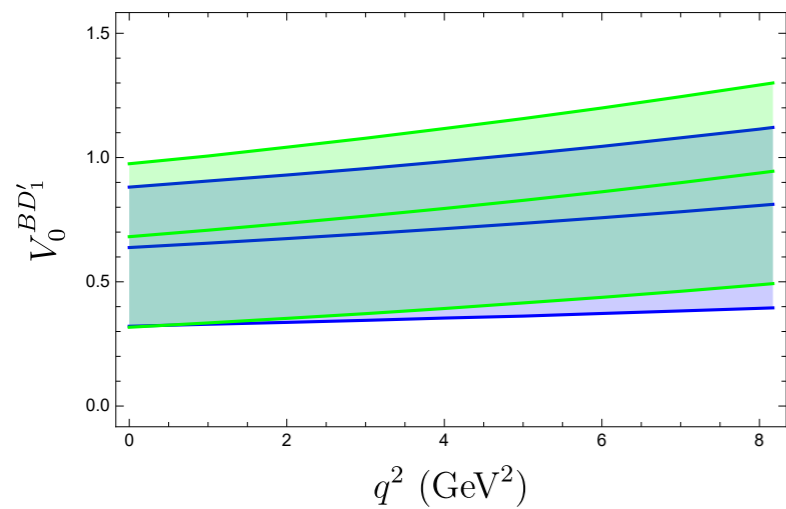
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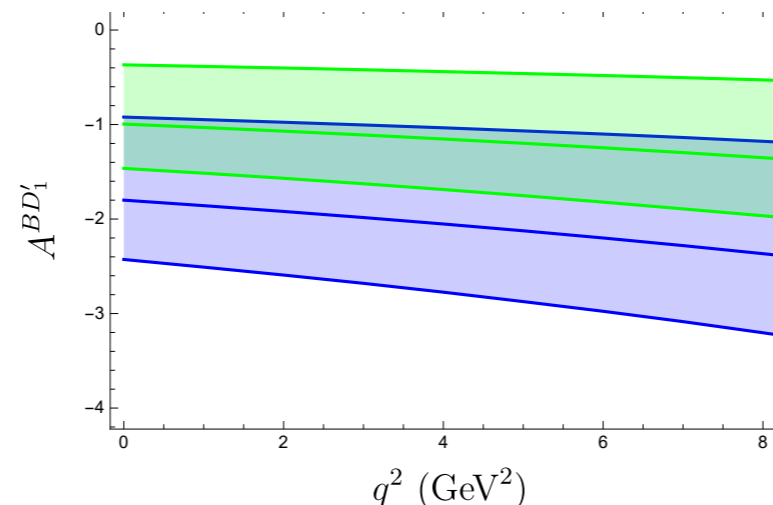
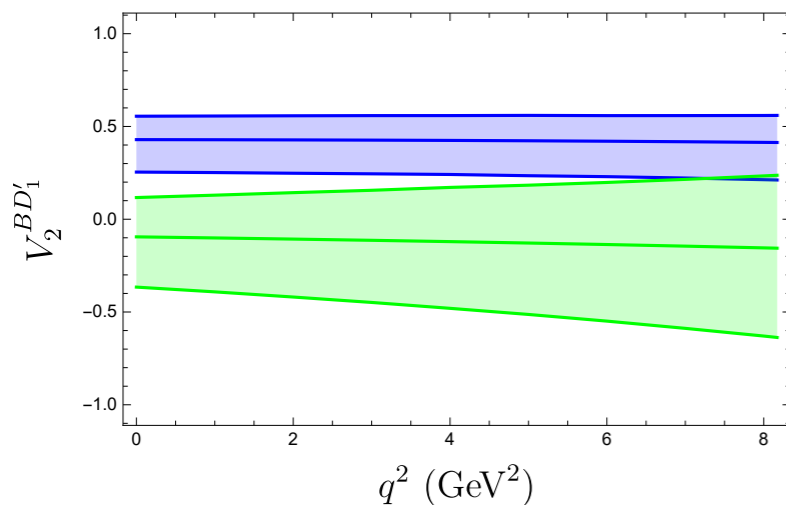
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► Ratio predictions are clean due to cancellations

$$R(D_1) = 0.10 \pm 0.02$$

$$R(D_1') = 0.10 \pm 0.03$$

# Summary & Outlook

- ▶  $B \rightarrow D^{**} \ell \bar{\nu}$  provides complimentary info.
  - new  $V_{cb}$  extraction
  - background estimation for  $R(D^{(*)})$  &  $V_{ub}$  extraction
- ➔ FF shape in full  $q^2$  is important

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► First **prediction** with finite charm mass is provided for  $B \rightarrow D_1^{(*)}$

Ongoing:  $B \rightarrow D_0^*$  FFs &  $B \rightarrow D^* \pi$  **partial wave** analysis

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► Also interesting are **charmed strange** mesons  $D_s^{**}$

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Thank you!

# Back ups

# FFs

$$F^{BR}(q^2) = \frac{F^{BR}(0)}{1 - \frac{q^2}{m_{JP}^2}} \{1 + \beta_F [z(q^2) - z(0)]\}$$

		$F^{BR}(0)$	$\beta_F$	Correlation
sol. 1	$A^{BD_1}$	$-0.27 \pm 0.29$	$-3.15 \pm 1.76$	0.03
	$V_0^{BD_1}$	$0.44 \pm 0.20$	$-3.41 \pm 1.26$	0.04
	$V_1^{BD_1}$	$0.16 \pm 0.10$	$1.69 \pm 1.38$	0.01
	$V_2^{BD_1}$	$-0.32 \pm 0.38$	$-4.19 \pm 6.29$	0.01
	$A^{BD'_1}$	$-1.69 \pm 0.77$	$-1.82 \pm 0.74$	0.04
	$V_0^{BD'_1}$	$0.60 \pm 0.32$	$-0.75 \pm 1.21$	-0.04
	$V_1^{BD'_1}$	$0.53 \pm 0.22$	$9.98 \pm 1.05$	-0.02
	$V_2^{BD'_1}$	$0.40 \pm 0.15$	$5.86 \pm 3.42$	-0.02
sol. 2	$A^{BD_1}$	$1.00 \pm 0.45$	$-1.82 \pm 0.50$	-0.06
	$V_0^{BD_1}$	$-0.26 \pm 0.15$	$-0.26 \pm 1.63$	0.02
	$V_1^{BD_1}$	$-0.31 \pm 0.12$	$9.32 \pm 1.73$	-0.02
	$V_2^{BD_1}$	$-0.39 \pm 0.19$	$2.26 \pm 2.36$	0.04
	$A^{BD'_1}$	$-0.92 \pm 0.61$	$-3.28 \pm 1.26$	-0.03
	$V_0^{BD'_1}$	$0.66 \pm 0.33$	$-3.71 \pm 2.37$	0.03
	$V_1^{BD'_1}$	$0.37 \pm 0.19$	$3.74 \pm 3.25$	0.01
	$V_2^{BD'_1}$	$-0.12 \pm 0.25$	$-5.84 \pm 4.42$	0.02